# A 500kHz ZVS Class E Type DC-DC converter with Two Anti-Series MOSFETs Topology 

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#### Abstract

Power converters powered by batteries have been widely used in many applications, such as outdoor emergency lighting, electric motorcycle charger, unmanned aerial vehicle supply and so on. This paper presents a 500 kHz zero-voltage-switching (ZVS) Class E type DC-DC converter with two anti-series MOSFETs used for battery-powered applications. The low-side MOSFET is adopted as the main switch to realize the working operation of traditional Class E resonant converter, while the highside anti-series MOSFET is used to implement the regulation of the converter output voltage based on pulse width modulation (PWM). Both active switches are ZVS operated so that a high efficiency can be achieved. By changing the high-side MOSFET duty cycle, the ac voltage of the resonant tank is also changed to regulate the output voltage consequently. The control method is simple, and the operating frequency is constant, which is beneficial for the design of the resonant components. A 100-W prototype is built to verify the validity of the proposed control method for which a $94.85 \%$ efficiency has been achieved.


Index Terms-Anti-series MOSFET, Class E converter, DC-DC converter, resonant converter.

NOMENCLATURE
$V_{\text {in }} \quad$ Input voltage;
$I_{\mathrm{f}} \quad \mathrm{DC}$ input current flowing in $L_{\mathrm{f}}$;
$I_{\mathrm{R}} \quad$ Amplitude of resonant current $i_{\mathrm{r}}$;
$L_{\mathrm{f}}\left(L_{\mathrm{f} 2}\right)$
$S_{1}$
$S_{2}$
$L_{\mathrm{r}}$
$C_{r}$
$C_{0}$
$R_{\text {ac }}$
$R_{\mathrm{dc}}$
$v_{\mathrm{ds} 1}$
$v_{\text {ds2 }}$
$v_{\text {cr }}$
$\nu_{\text {Rac }}$
$\nu_{\text {Lb }}$
$v_{\mathrm{s}}$
$v_{\text {sm1 }}$
$V_{\text {Rac1 }}$
$V_{\text {Lb1 }}$
$C_{\text {s } 1}$
$C_{\text {s } 2}$
$i_{\mathrm{cs} 1}$

Choke inductance;
Low-side power MOSFET switch;
High-side power MOSFET switch;
Resonant inductance;
Resonant capacitance;
Output capacitance;
Equivalent $A C$ resistance;
Equivalent $D C$ resistance;
Drain-source voltage of $S_{1}$;
Drain-source voltage of $S_{2}$;
Voltage across $C_{r}$;
Voltage across $R_{\mathrm{ac}}$;
Voltage across $L_{\mathrm{b}}$;
Total voltage across both switches ( $\left.v_{\mathrm{ds} 1}-v_{\mathrm{ds} 2}\right)$; Fundamental voltage of $v_{\mathrm{s}}$;
Fundamental voltage of $v_{\text {Rac }}$;
Fundamental voltage of $v_{\mathrm{Lb}}$; Drain-source capacitance of $S_{1}$; Drain-source capacitance of $S_{2}$; Current flowing through capacitor $C_{\text {s }}$;

| $i_{\mathrm{cs} 2}$ | Current flowing through capacitor $C_{\mathrm{s} 2} ;$ |
| :--- | :--- |
| $i_{\mathrm{r}}$ | Current into the resonant tank; |
| $D_{\mathrm{r} 1}$ | Output rectifier diode; |
| $D_{\mathrm{b} 2}$ | Diode of $S_{2} ;$ |
| $Q_{\mathrm{L}}$ | Quality factor; |
| $\omega$ | Angular switching frequency; |
| $\varphi$ | Initial angle of the resonant current; |
| $\theta$ | Conduction angle; |
| $P W M_{1}$ | Drive signal of switch $S_{1} ;$ |
| $P W M_{2}$ | Drive signal of switch $S_{2} ;$ |
| $P_{\mathrm{sw}}$ | Switch conduction loss; |
| $I_{\mathrm{rms}}$ | RMS current through the switch; |
| $R_{\mathrm{ds}(\mathrm{on})}$ | Drain-source branch resistor; |
| $P_{\mathrm{d}}$ | Diode conduction loss; |
| $I_{\mathrm{fd}}$ | Forward RMS current through diode; |
| $V_{\mathrm{fd}}$ | Forward voltage through diode; |
| $P_{\mathrm{r}}$ | Resonant tank conduction loss; |
| $I_{\mathrm{r}, \mathrm{rms}}$ | RMS current in resonant tank; |
| $R_{\mathrm{r}}$ | Equivalent resonant resistance. |

## I. INTRODUCTION

OWING to the increasing demand of high-power density battery-powered supplies in many applications, such as mobile phones or pad chargers, Personal-Computer (PC) power adapters, unmanned aerial vehicles, and so on, more and more applications need a small volume power supply_[1-3]. The adoption of high switching frequency can decrease the volume of passive components but decreasing switching loss- has naturally become the next interesting target of dc-dc converter design. Compared to conventional dc-dc converters, such as Buck, Buck-Boost, SEPIC and so on, resonant converters which utilize the resonance of an inductor and a capacitor can realize Zero-Voltage-Switching (ZVS) or Zero-Current-Switching operations (ZCS)[4-7]. Therefore, in high-frequency applications, resonant converters have become a priority scheme.

In high-power applications, the Dual-Active-Bridge (DAB) converter with an LC or CLLC resonant cell has been widely used with all switches under soft-switching operation [8-10]. For the DAB converter, a complex control method, for example, dual-phase-shift, triple-phase-shift, model predictive control, etc., is definitely adopted to satisfy the full-load softswitching characteristic. In low-medium power applications; LLC converter is the common resonant converter which can
achieve the primary-side ZVS for the controlled switches, and secondary-side diode ZCS characteristic. But when switching frequency becomes higher than resonant frequency, especially at light-load condition, the secondary-side ZCS characteristic disappears. Moreover, the two converters above contain more components, which increases the system cost [11-13]. Besides the above-mentioned resonant converters, in high-frequency applications, the Class E type converter has some obvious advantages [14-16]: simple structure, ZVS switching feature, current-fed, low current ripples. There are more and more applications adopting the Class E resonant converter, such as radio-frequency power amplifiers, wireless power transfer, LED drivers, dc-dc bidirectional converters, etc. [17-19]. Like other resonant converters, a Pulse-Frequency-Modulation (PFM) control method is used to regulate the output voltage while the duty cycle is kept constant at 0.5 for the Class E converter. At rated working condition, the Class E converter has an excellent performance. However, at light-load condition, the changing of the switching frequency to satisfy the demand of voltage or output power, makes it difficult to design the resonant inductor and capacitor. If the switching frequency remains unchangeable, a nominal resonant working condition will be held. Generally, a PWM method is a candidate to replace the PFM control method. In [19], a PWM method is proposed to regulate a Class E converter which provides some improvement for expanding the operation range. Obviously, having only an active switch makes it too difficult to regulate the converter in a wide load range. To draw a conclusion, only one active switch restricts the regulation performance of the Class E resonant converter.


Fig. 1 Previous Class E circuit: a) converter proposed in [20], b) converter proposed in [21]

In [20], two identical Class E circuits are combined into one topology as shown in Fig. 1 a). In this structure, a phaseshift control method is adopted to regulate the output current. The control method remains the conventional Class E operation mode, and it is simple to implement without complex control logic. However, more passive components are needed in the circuit and the selection of identical specifications increases the design complexity. In [21], an active switch is series-connected
in the resonant tank cell as shown in Fig. 1 b). By changing the resonant frequency of the resonant tank, the output voltage is controlled. This method holds the switching frequency constant to simplify the design of resonant components. But the softswitching state is influenced, that is to say, ZVS operation is lost. In [22], by resetting the position of the active switch, and still changing the resonant frequency of the resonant tank, the active switch is also used as rectifier to control the output voltage. However, the ZVS state is still influenced.

In this paper, an innovative technique is presented, in which an anti-series active switch is placed to enhance the main active switch. By using Pulse-Width-Modulation (PWM) control, the drain-to-source voltage of the whole two-MOSFET switch is changed to regulate the output voltage. The contributions of this paper can be stated as follows:

1) The switching frequency of the two active switches is constant. This way, this method can simplify the design of resonant passive components.
2) The high-side switch is modulated in PWM scheme, which is easy to implement. Meanwhile, the low-side switch is operated with 0.5 duty cycle and constant working frequency, which does not change nominal working state of the traditional Class E converter and keeps ZVS feature.
3) Utilizing the body diode, or an added diode, of the highside switch, the anti-series active switch works either as a switch or as a diode, which decreases the switch driving loss.

This paper is organized as follows. In Section II, the working principle of the proposed Class E converter is discussed in detail. The analysis and design of the Class E resonant converter are elaborated in Section III. An experimental prototype is built to show the results of the proposed Class E resonant converter in Section IV. Finally, a conclusion is drawn in Section V.

## II. Working principle of proposed Class E CONVERTER

The proposed two-switch anti-series Class E converter is shown in Fig.2. It contains four function cells $\div$ First, the input cell consists of the input source and a choke inductor, which provides a constant current source; Second, anti-series two active switches are the control cell to regulate the output voltage; Third, the resonant tank is made up by a resonant inductor and a capacitor; Lastly, a half-wave or full-wave rectifier is connected to the resonant tank to supply the load.


Fig. 2 Proposed anti-series two-switch Class E dc-dc converter.
The principle of the proposed Class E converter is discussed as follows:

1) Period [0: $\theta_{1}$ ]: At the beginning, $S_{1}$ is turned off and $S_{2}$ is driven on. The drain-source voltage $v_{\mathrm{ds} 1}$ is increasing. Meanwhile, the current $i_{\text {cs1 }}$ begins to decrease from the
instantaneous peak value. At angle $\theta_{1}$, current $i_{\text {cs1 }}$ changes its flowing direction, therefore the drain-source voltage $v_{\mathrm{ds}}$ reaches the peak value. The resonant current flow loop is $C_{\mathrm{r}}-L_{\mathrm{r}}$ -$S_{2}-C_{\mathrm{s} 1}-R_{\mathrm{ac}}$, as shown in Fig. 3 a).
2) Period $\left[\theta_{1}: \theta_{2}\right]: S_{2}$ is still turned on. The drain-to-source voltage of switch $S_{2}$ retains zero clamped by $S_{2}$. But the voltage $v_{\mathrm{ds} 1}$ begins to decrease from the peak value. Meanwhile, current $i_{\text {cs1 }}$ increases in reverse direction, as shown in Fig. 3 b). At angle $\theta_{2}, S_{2}$ is turned off.
3) Period $\left[\theta_{2}: \theta_{3}\right]$ : When $S_{2}$ is turned off, $C_{\mathrm{s} 2}$ begins to be charged by resonant current $i_{\mathrm{r}}$ and $C_{\mathrm{s} 1}$ begins to discharge to $C_{\mathrm{s} 2}$. Therefore, $v_{\mathrm{ds} 2}$ begins to increase from zero and $v_{\mathrm{ds} 1}$ continues to decrease. Because both switches $S_{1}, S_{2}$ are turned off, the resonant current flow loop is $C_{\mathrm{s} 1}-C_{\mathrm{s} 2}-L_{\mathrm{r}}-C_{\mathrm{r}}-R_{\mathrm{ac}}$, as shown in Fig. 3 c ). At angle $\theta_{3}$, the $v_{\mathrm{ds} 1}$ reaches zero.

The resonant current $i_{\mathrm{r}}$ is depicted in (1). According to Kirchhoff's current law, (2) can be obtained.

$$
\begin{align*}
& i_{r}(\theta)=I_{R} \sin (\theta-\varphi)  \tag{1}\\
& I_{f}=i_{c s 1}+i_{r}  \tag{2}\\
& \quad=i_{c s 1}(\theta)+I_{R} \sin (\theta-\varphi)
\end{align*}
$$

During the period [0: $\theta_{3}$ ], the expression $v_{\mathrm{ds} 1}$ is shown in (3).

$$
\begin{align*}
v_{d s 1}(\theta) & =\frac{1}{\omega C_{s 1}} \int_{0}^{\theta} i_{c s 1}(\xi) d \xi \\
& =\frac{1}{\omega C_{s 1}} \int_{0}^{\theta} I_{f}-I_{R} \sin (\xi-\varphi) d \xi  \tag{3}\\
& =\frac{1}{\omega C_{s 1}}\left\{I_{f}\left[\theta+I_{R}[\cos (\theta-\varphi)-\cos \varphi]\right\}\right.
\end{align*}
$$

4) Period $\left[\theta_{3}: \theta_{4}\right]: v_{\mathrm{ds} 2}$ still increases, meanwhile current $i_{\mathrm{cs} 2}$ decreases gradually. When $i_{\mathrm{cs} 2}$ reaches zero, $v_{\mathrm{ds} 2}$ attains its peak value. Then, $i_{\mathrm{cs} 2}$ changes the flowing direction to increase, and $v_{\mathrm{ds} 2}$ begins to decrease. Because $S_{1}$ is clamped by the $D_{\mathrm{b} 1}, v_{\mathrm{ds} 1}$ holds zero. At angle $\theta_{4}, S_{1}$ is turned on. Because $v_{\mathrm{ds} 1}$ remains zero, the ZVS soft-switching characteristic is achieved.
5) Period [ $\theta_{4}: \theta_{5}$ ]: $i_{\mathrm{cs} 2}$ continues to increase, at angle $\theta_{5}, v_{\mathrm{ds} 2}$ reaches zero too. As shown in Fig. 3 e), by changing the duty cycle $D_{2}$ of switch $S_{2}$, the whole voltage $v_{\mathrm{s}}=\left(v_{\mathrm{ds} 1}-v_{\mathrm{ds} 2}\right)$ also changes. In next Section III, the relationship between $V_{\text {Rac }}$ and $v_{\mathrm{s}}$ will be discussed.

During the period that $\theta$ belongs to [ $\theta_{2}: \theta_{5}$ ], voltage $v_{\mathrm{ds} 2}$ is also obtained just like $v_{\mathrm{ds}}$ deduction shown above, as given in (4).

$$
\begin{equation*}
v_{d s 2}(\theta)=\frac{1}{\omega C_{s 2}}\left\{I_{f} \square\left(\theta-\theta_{2}\right)+I_{R}\left[\cos (\theta-\varphi)-\cos \left(\theta_{2}-\varphi\right)\right]\right\} \tag{4}
\end{equation*}
$$

6) Period $\left[\theta_{5}: \theta_{6}\right]: S_{1}$ is still turned-on, so the voltage $v_{\mathrm{ds} 1}$ is zero. The anti-series switch $S_{2}$ is also clamped by diode $D_{\mathrm{b} 2}$, so $v_{\mathrm{ds} 2}$ is also zero. At angle $\theta_{6}$, another new cycle begins.

Because the stored energy in the choke inductor $L_{\mathrm{f}}$ is zero in one switching cycle, the input voltage $V_{\text {in }}$ is the average value of the two anti-series switch voltage $v_{\mathrm{s}}$. According to (3) and (4), $V_{\text {in }}$ is determined in (5).


Fig. 3 Working Modes of proposed Class E dc-dc converter.

$$
\begin{align*}
V_{i n} & =\frac{1}{2 \pi} \int_{0}^{2 \pi}\left(v_{d s 1}-v_{d s 2}\right) d \theta \\
& =\frac{1}{2 \pi}\left[\int_{0}^{2 \pi} v_{d s 1} d \theta-\int_{0}^{2 \pi} v_{d s 2} d \theta\right]  \tag{5}\\
& =\frac{1}{2 \pi}\left[\int_{0}^{\theta_{3}} v_{d s 1}(\xi) d \xi-\int_{\theta_{2}}^{\theta_{5}} v_{d s 2}(\xi) d \xi\right]
\end{align*}
$$

The main waveforms of voltage and current in the topology are shown in Fig.4. $v_{\mathrm{ds} 1}$ and $v_{\mathrm{ds} 2}$ both have ZVS characteristics. When the duty cycle $D_{2}$ changes, $v_{\mathrm{d} s 2}$ also changes, that is to say, $v_{\mathrm{s}}$ will also change to regulate the ac voltage $v_{\text {Rac. }}$. The detailed deduction is discussed in the following section.


Fig. 4 Main Waveforms of proposed Class E dc-dc converter ${ }_{\text {I }}$

## III. PERFORMANCE ANALYSIS AND NUMERICAL SOLUTIONS

To simplify the circuit performance analysis, the following conditions are assumed:

1) The choke inductor is so large that the ac current is negligible compared with the dc current.
2) The diodes and MOSFETs are ideal to operate with instant turn on and turn-off. The drop voltage is also ignored.
3) The resonant current is close to the sinusoidal waveform. So, the quality factor is set higher than 2.5.

For the resonant inductance $L_{\mathrm{r}}$, it can be divided into two parts: inductances $L_{\mathrm{a}}$ and $L_{\mathrm{b}}$. $L_{\mathrm{a}}$ joins the resonance with the capacitance $C_{\mathrm{r}}$. $L_{\mathrm{b}}$ provides the weak inductance which does not join in the resonance. For the traditional Class E converter, the switching frequency ranges from $f_{\mathrm{r} 1}$ to $f_{\mathrm{r} 2} . F_{\mathrm{r} 1}$ is the resonance frequency of $L_{\mathrm{r}}$ and $C_{\mathrm{r}}$, and $f_{\mathrm{r} 2}$ is the resonance frequency of $L_{\mathrm{r}}$,
$C_{\mathrm{r}}$ and drain-source capacitor $C_{\mathrm{s}}$. For the proposed Class E converter, the new $f_{\mathrm{r} 2}$ is higher than the value discussed above owing to the new drain-source capacitor $C_{\mathrm{s} 2}$. Therefore, the real inductor $L_{\mathrm{r}}$ is a little higher than the theoretical result. In (6), the relation among $L_{\mathrm{a}}, L_{\mathrm{b}}$ and $C_{\mathrm{r}}$ is shown.

$$
\begin{equation*}
Q_{L}=\frac{\omega L_{r}}{R_{a c}}=\frac{\omega\left(L_{a}+L_{b}\right)}{R_{a c}}=\frac{1}{\omega C_{r} R_{a c}}+\frac{\omega L_{b}}{R_{a c}} \tag{6}
\end{equation*}
$$



Fig. 5 Vector diagram of voltage fundamental component.
In order to calculate the numerical solutions, the conduction angle boundary is set to satisfy the nominal working condition. $\theta_{2}=2 \pi D_{2}, \theta_{3}=\pi, \theta_{5}=\frac{3}{2} \pi$ are set, then $V_{\text {in }}$ is further expressed in (7).

$$
\begin{align*}
V_{\text {in }}= & \frac{(4 \sin \varphi-2 \pi \cos \varphi) \square_{R}+\pi^{2} \square I_{f}}{4 \pi \omega C_{s 1}}-\frac{\left(4 \pi D_{2}-3 \pi\right)^{2} \square \square_{f}}{16 \pi \omega C_{s 2}} \\
& -\frac{\left[4 \pi D_{2} \cos \left(\varphi-2 \pi D_{2}\right)-3 \pi \cos \left(\varphi-2 \pi D_{2}\right)\right] \square_{R}}{4 \pi \omega C_{s 2}}  \tag{7}\\
& -\frac{\left[-2 \cos \varphi+2 \sin \left(\varphi-2 \pi D_{2}\right)\right] \bigsqcup_{R}}{4 \pi \omega C_{s 2}}
\end{align*}
$$

In order to satisfy the ZVS condition of $S_{1}$, at angle $\theta_{3}, v_{\mathrm{ds} 1}=$ 0 . Setting $\theta_{3}=\pi$, the relation between $I_{\mathrm{f}}$ and $I_{\mathrm{R}}$ can be achieved in (8).

$$
\begin{equation*}
I_{f}=\frac{2 \cos \varphi}{\pi} I_{R} \tag{8}
\end{equation*}
$$

For the resonant tank, according to the fundamental analysis method, the ac voltage $V_{\text {Rac }}$, the whole switch voltage $v_{\mathrm{s}}$ and non-resonant inductor voltage $v_{\mathrm{Lb}}$ are deduced in (9) and (10).

$$
\begin{align*}
V_{R a c} & =\frac{1}{2 \pi} \int_{0}^{2 \pi}\left(v_{d s 1}-v_{d s 2}\right) \sin (\theta-\varphi) d \theta \\
& =\frac{1}{2 \pi}\left[\int_{0}^{\pi} v_{d s 1} \sin (\theta-\varphi) d \theta-\int_{\frac{\pi}{2}}^{2 \pi} v_{d s 2} \sin (\theta-\varphi) d \theta\right]  \tag{9}\\
V_{L b}= & \frac{1}{2 \pi} \int_{0}^{2 \pi}\left(v_{d s 1}-v_{d s 2}\right) \cos (\theta-\varphi) d \theta  \tag{10}\\
= & \frac{1}{2 \pi}\left[\int_{0}^{\theta_{3}} v_{d s 1} \cos (\theta-\varphi) d \theta-\int_{\theta_{2}}^{\theta_{5}} v_{d s 2} \cos (\theta-\varphi) d \theta\right]
\end{align*}
$$

Substituting (3), (4) and (8) into (7), (9) and (10), the ac resistor $R_{\mathrm{ac}}$, dc resistor $R_{\mathrm{dc}}$ and $\omega L_{b}$ can be obtained as shown in (11), (12) and (13). The resistance relationship can be calculated.

$$
\begin{align*}
R_{d c} & =\frac{V_{i n}}{I_{f}}=\frac{\sin \varphi}{2 \omega \cos \varphi C_{s 1}} \\
& -\frac{4 \sin \left(\varphi-2 \pi D_{2}\right)-4 \cos \varphi+\pi\left(4 D_{2}-3\right)^{2} \cos \varphi}{16 \omega \cos \varphi C_{s 2}}  \tag{11}\\
& +\frac{8 \pi D_{2} \cos \left(\varphi-2 \pi D_{2}\right)-6 \pi \cos \left(\varphi-2 \pi D_{2}\right)}{16 \omega \cos \varphi C_{s 2}} \\
R_{a c} & =\frac{V_{a c 1}}{I_{R}}=\frac{2 \sin \varphi \cos \varphi}{\pi^{2} \omega C_{s 1}} \\
& +\frac{4 \pi \cos \varphi-\pi^{2}\left(4 D_{2}-3\right)^{2} \cos \varphi-4 \pi \sin \left(\varphi-2 \pi D_{2}\right)}{8 \pi^{2} \omega C_{s 2}}(12)  \tag{12}\\
+ & \frac{6 \pi^{2} \cos \left(\varphi-2 \pi D_{2}\right)-8 \pi^{2} D_{2} \cos \left(\varphi-2 \pi D_{2}\right)}{8 \pi^{2} \omega C_{s 2}} \\
\omega L_{b} & =\frac{V_{L b 1}}{I_{R}}=\frac{\pi^{2}-8 \cos ^{2} \varphi}{4 \pi^{2} \omega C_{s 1}} \\
& -\frac{\left(3-4 D_{2}\right) \pi^{2}+(\pi-4) \sin (2 \varphi)+4 \pi\left(4 D_{2}-3\right) \cos ^{2} \varphi}{8 \pi^{2} \omega C_{s 2}} \\
& -\frac{4(\pi-2) \cos \varphi \cos \left(\varphi-2 \pi D_{2}\right)-\pi \sin \left(2 \varphi-4 \pi D_{2}\right)}{8 \pi^{2} \omega C_{s 2}} \tag{13}
\end{align*}
$$

According to (6), the resonant capacitor $C_{\mathrm{r}}$ can be calculated in (14).

$$
\begin{equation*}
C_{r}=\frac{1}{\omega\left(R_{a c} Q_{L}-\omega L_{b}\right)} \tag{14}
\end{equation*}
$$

With the increase of $Q_{\mathrm{L}}, C_{\mathrm{r}}$ is gradually decreasing. However, a smaller value means a higher voltage stress, as shown in (15). Therefore, the value of $C_{\mathrm{r}}$ is selected by considering a limited voltage stress.

$$
\begin{align*}
V_{c r}(\theta) & =\frac{1}{\omega C_{r}} \int_{0}^{\theta} I_{R} \sin (\xi-\varphi) d \xi  \tag{15}\\
& =\frac{1}{\omega C_{r}} I_{R}[\cos \varphi-\cos (\theta-\varphi)]
\end{align*}
$$

In order to obtain ZVS operation, $\omega L_{\mathrm{b}}$ should be higher than zero, which means a weak inductive behavior. According to (13), the relationship between $\varphi$ and $C_{\mathrm{s} 2} / C_{\mathrm{s} 1}$ for different values of $D_{2}$ is shown in Fig. 5. With the increase of $D_{2}$, the peak value of $C_{\mathrm{s} 2} / C_{\mathrm{s} 1}$ decreases, at the condition that $\varphi$ ranges from 0 to 90 degrees. The peak value of $C_{\mathrm{s} 2} / C_{\mathrm{s} 1}$ is 1.5 times.


Fig. 5 Relationship between $C_{\mathrm{s} 2} / C_{\mathrm{s} 1}$ and $\varphi$ at different $D_{2}$

The equivalent circuit of the proposed resonant converter is shown in Fig.6. The secondary-side output circuit is simplified as a resistor $R_{\mathrm{ac}}$. The Capacitors $C_{\mathrm{s} 1}, C_{\mathrm{s} 2}$ are both included in the resonant loop.


Fig. 6 Equivalent circuit of proposed resonant converter
The input impedance $Z_{\text {in }}(s)$ is deduced in (16) whose Bode diagram is plotted in Fig._7. An inductive range is determined which means a soft-switching characteristic. By increasing the value of $C_{\mathrm{s} 2}$ to a limit value, the inductance range will not change. By decreasing value of $C_{\mathrm{s} 2}$, the soft-switching range narrows.


Fig. 7 Bode diagram of input impedance $Z_{\text {in }}(s)$.

$$
\begin{align*}
Z_{i n}(s) & =\frac{\left(\frac{1}{s C_{s 1}}+\frac{1}{s C_{s 2}}\right) \times\left(s L_{r}+\frac{1}{s C_{r}}+R_{a c}\right)}{\left(\frac{1}{s C_{s 1}}+\frac{1}{s C_{s 2}}\right)+\left(s L_{r}+\frac{1}{s C_{r}}+R_{a c}\right)}  \tag{16}\\
& =\frac{\left(\frac{1}{s C_{s 1}}+\frac{1}{s C_{s 2}}\right) \times\left(L_{r} s^{2}+R_{a c} s+\frac{1}{C_{r}}\right)}{L_{r} s^{3}+R_{a c} s^{2}+\left(\frac{1}{s C_{s 1}}+\frac{1}{s C_{s 2}}+\frac{1}{C_{r}}\right) s}
\end{align*}
$$

In order to guarantee the ZVS condition of $S_{1}$, the value of $C_{\mathrm{s} 2}$ is higher than the one of $C_{\mathrm{s} 1}$, on the purpose of releasing all the energy stored in $C_{\mathrm{s} 1}$. The relation among $Q_{\mathrm{L}}, v_{\mathrm{ds} 1}, v_{\mathrm{ds} 2}$, and $v_{\text {cr }}$ is shown in Fig._8. When the power quality factor $Q_{\mathrm{L}}$ increases, the peak voltage values of $S_{1}, S_{2}$ decrease as well. But the voltage stress of $C_{\mathrm{r}}$ is increasing sharply.


Fig. 8 Relation among $Q_{\mathrm{L}}, v_{\mathrm{ds} 1}, v_{\mathrm{ds} 2}$, and $v_{\mathrm{cr}}$
For the capacitance $C_{\mathrm{r}}$, a 3000 V rating voltage ceramic capacitor may satisfy the system requirements at a very high value of $Q_{\mathrm{L}}$. But a higher rating voltage also increases the cost. High $Q_{\mathrm{L}}$ means a narrow-band signal selection, which restricts the energy in other frequency bands passing through the resonant tank to the load. Likewise, small $Q_{\mathrm{L}}$ means small value of $L_{\mathrm{r}}$ which increases the conduction loss, due to a high circulating current. According to (13) and (14), $L_{\mathrm{b}}$ and $C_{\mathrm{r}}$ can be calculated. Then, $L_{\mathrm{a}}$ is derived as shown in (17).

$$
\begin{equation*}
L_{a}=\frac{Q_{L} R_{a c}}{\omega}-L_{b} \tag{17}
\end{equation*}
$$

The output stage can be generated by half-wave rectification or full-wave rectification. The relation between $R_{\mathrm{ac}}$ and $R_{\mathrm{o}}$ is depicted in (18), where $n$ is the turn ratio of primary-side to secondary-side in the transformer. When a high gain of the system is demanded, a transformer is needed.

$$
R_{a c}= \begin{cases}\frac{2}{\pi^{2}} R_{o}, & \text { half-wave rectifier }  \tag{18}\\ \frac{8 n^{2}}{\pi^{2}} R_{o}, & \text { full-wave rectifier }\end{cases}
$$

Now, the gain $M$ of the dc-dc converter is discussed as follows. The input power is shown in (19). The output power
$P_{\mathrm{o}}$ is depicted in (20). The transmission efficiency is designated as $\eta$; then, $M$ is calculated in (21).

$$
\begin{gather*}
P_{i n}=V_{i n} I_{f}=\frac{V_{i n}^{2}}{R_{d c}}  \tag{19}\\
P_{o}=V_{o} I_{o}=\frac{V_{o}^{2}}{R_{o}}  \tag{20}\\
M=\frac{V_{o}}{V_{i n}}=\sqrt{\eta \frac{R_{o}}{R_{d c}}} \tag{21}
\end{gather*}
$$

The system gain $M$ is related to the equivalent resistances $R_{\mathrm{o}}$ and $R_{\mathrm{dc}}$. For a high-gain application, the rectification circuit can employ a transformer. According to (11), (12), (18), (21), $M$ is a function of variable $D_{2}$ in (22). The relation between $M$ and $D_{2}$ is depicted in Fig.9. When $\varphi$ equals to $30^{\circ}, M$ changes non-linearly with the $D_{2}$. When $\varphi$ increases to $60^{\circ}$, the linearization becomes better which satisfies the application requirement. At different values of $\varphi$, the system $M$ changes with the $D_{2}$; for example, at the condition of $C_{\mathrm{s} 1}=6.8 \mathrm{nF}$ and $C_{\mathrm{s} 2}=12 \mathrm{nF}, \varphi=60^{\circ}, M$ is 2 at the angle of $D_{2}=0.3$. The output power $P_{\mathrm{o}}$ is also regulated by $D_{2}$ which is depicted in (23).

$$
\begin{align*}
& M=\frac{V_{o}}{V_{i n}}=\sqrt{\eta \frac{\pi^{2}}{2} \frac{R_{a c}}{R_{d c}}}=f\left(D_{2}\right)  \tag{22}\\
& P=\frac{V_{o}^{2}}{R_{o}}=\eta \frac{\pi^{2}}{2} \frac{R_{a c}\left(D_{2}\right)}{R_{d c}\left(D_{2}\right)} \frac{1}{R_{o}} V_{i n}^{2} \tag{23}
\end{align*}
$$



Fig. 9 Relation of $M$ and $D_{2}$ at different $Q_{\mathrm{L}}$.
The main parameters in this topology are $L_{\mathrm{r}}, ~ C_{\mathrm{r}}, ~ C_{\mathrm{s} 1}, ~ C_{\mathrm{s} 2}$. The basic parameter calculation procedure can be summarized as follows.

Firstly, the quality factor $Q_{\mathrm{L}}$ needs to be chosen as a suitable value. It influences the voltage stress and value of $L_{\mathrm{r}}$. A high $Q_{\mathrm{L}}$ will increase the voltage stress of $C_{\mathrm{s} 1}$ and $C_{\mathrm{s} 2}$, and a high value of $L_{\mathrm{r}}$ which is good for decreasing conduction loss. Therefore, it is a trade-off for stress and efficiency.

Secondly, once the power factor $Q_{\mathrm{L}}$ is determined, according to the definition of $Q_{\mathrm{L}}=\left(\omega L_{r}\right) / R_{a c}$, the value of $L_{\mathrm{r}}$ can be calculated. In order to simplify the calculation, assuming that $C_{\mathrm{r}}$ resonates with $L_{\mathrm{r}}$, a value of $C_{\mathrm{r}}$ can be obtained. In fact,
part of $L_{\mathrm{r}}$ is definitely $L_{\mathrm{a}}$ which participates in resonance with $C_{\mathrm{r}}$. Therefore, as a last step, the value of $C_{\mathrm{r}}$ should be revised.

Thirdly, in order to satisfy the ZVS characteristic of $S_{1}$, the input impedance seen from the switch $S_{1}$ can be deduced. The angle $\varphi$ is higher than zero, the ZVS range can be achieved, and since a weak inductance is guaranteed, the condition of $\omega L_{b}>0$ is also satisfied. Combining the voltage stress among $C_{\mathrm{s} 2}, C_{\mathrm{s} 1}$ and $C_{\mathrm{r}}$, the values of $C_{\mathrm{s} 1}$ and $C_{\mathrm{s} 2}$ can be achieved.

Finally, these values will influence the voltage gain. Further, the values of four components are done with minor correction.

## IV. DESIGN CONSIDERATIONS AND COMPONENT SELECTION

In this paper, a 100 W prototype is built whose nominal input voltage is 48 V with a range from 30 Vdc to 60 Vdc , rated output voltage/current $50 \mathrm{~V} / 2 \mathrm{~A}$. And the switching frequency is 500 kHz for both $S_{1}, S_{2}$. The choke inductor $L_{\mathrm{f}}$ is calculated as shown in (24). The main specifications and parameters of the proposed converter are listed in Table I. A digital signal processor TMS320F28377 is adopted as the main controller.

$$
\begin{equation*}
L_{f}=2\left(\frac{\pi^{2}}{4}+1\right) \frac{R_{a c}}{f_{s}} \tag{24}
\end{equation*}
$$

Fig. 9 shows the schematic diagram of the laboratory prototype. The experimental prototype is shown in Fig. 10. CoolMOS MOSFET IPP60R022S7 was selected to implement the active switches. The rectifier cell adopts the conventional Class E rectifier circuit which consists of one diode $D_{\mathrm{r} 1} . D_{\mathrm{r} 1}$ is implemented by an ultra-fast recovery diode STPS20200C. In order to improve the current capability of $S_{2}$, a diode $D_{\mathrm{b} 2}$ is connected in parallel with $S_{2}$. The resonant inductor $L_{\mathrm{r}}$ is set to $23 \mu \mathrm{H}$, and the resonant capacitor $C_{\mathrm{r}}$ consists of six 1 nF units and one 660 pF unit in parallel. Meanwhile five $2.2 \mu \mathrm{~F}$ capacitors in parallel are used to build the output capacitor $C_{0}$.


Fig. 9 Schematic diagram of the laboratory prototype.
TABLE I
SPECIFICATION AND PARAMETERS OF PROPOSED CONVERTER

| Component | Value | Device Models |
| :---: | :---: | :---: |
| $L_{\mathrm{f}}, L_{2 \mathrm{f}}$ | $68 \mu \mathrm{H}$ | WurthElektronik744375292036 |
|  |  | 80 |
| $S_{1}, S_{2}$ | $600 \mathrm{~V} / 23 \mathrm{~A}$ | IPP60R022S7 Cool- MOS |
| $L_{\mathrm{r}}$ | $23 \mu \mathrm{H}$ | $0.1 \mathrm{~mm} * 200 \mathrm{P}-22$ Turns |
| $C_{\mathrm{r}}$ | 6.66 nF | $1 \mathrm{nF} / 3000 \mathrm{~V}, 660 \mathrm{pF} / 3000 \mathrm{~V}$ |
| $C_{\mathrm{o}}$ | $11 \mu \mathrm{~F}$ | $2.2 \mu \mathrm{~F} / 250 \mathrm{~V}$ |
| $D_{\mathrm{r} 1}, D_{\mathrm{b} 2}$ | $200 \mathrm{~V} / 10 \mathrm{~A}$ | STPS20200C |
| Drive IC |  | $1 \mathrm{ED} 3124 \mathrm{MU} 12 \mathrm{HXUMA1}$ |
| Auxiliary |  | F0524S-2WR2 |
| Power |  |  |



Fig. 10 Experimental prototype of proposed converter topology,
At the rated output power, the waveform of $V_{\mathrm{ds} 1}$ and $V_{\mathrm{ds} 2}$ are shown in Fig. 11. As can be seen, ZVS characteristic can be achieved.


Fig. 11 Waveforms of drain-source voltage and drive signal in $S_{1}$ and $S_{2}$

By modulating the duty cycle of $S_{2}$, the output voltage can be regulated. When $D_{2}$ equals 0.5 , the output voltage $V_{0}$ is changed as illustrated in Fig._12. By adjusting $D_{2}$, the output voltage and current is also changed. Because the duty cycle $D_{1}$ is 0.5 constant, $V_{\text {ds1 }}$ is still under ZVS operation. At the condition of $D_{2}=0.7, V_{\mathrm{ds} 2}$ changes to nearly zero, as depicted in Fig. 13. The output voltage is regulated by changing the voltage $V_{\mathrm{ds} 2}$ adopting the PWM method.


Fig. 12 Waveforms of $V_{\mathrm{ds} 2}$ and output voltage at $D_{2}=0.5_{\text {: }}$


Fig. 13 Waveforms of $V_{\text {ds } 2}$ and output voltage at $D_{2}=0.7$.
The waveforms of current in $L_{\mathrm{f}}$ and input voltage $V_{\text {in }}$ are shown in Fig.14. The ripple in current is rather small so that the input port is regarded as a constant current source.


Fig. 14 Waveforms of input voltage $V_{\text {in }}$ and current $I_{\text {t }}$

[Times: $8 \mathrm{~ms} / \mathrm{div}$ ]
Fig. 15 Waveforms of output voltage $V_{0}$ and current $I_{0}$.
The waveforms of output voltage and current are shown in
Fig. 15 at the rated working condition. Fig. 16 shows the
waveform of $v_{\mathrm{cr}}$ which demonstrates that a low rating voltage capacitor can be adopted for $C_{\mathrm{r}}$.


Fig. 16 Waveforms of resonant capacitor $C_{\mathrm{r}}$ voltage $V_{\text {cr }}$ and $V_{\text {ds } 1}$ at the rated condition.

Fig. 17 shows the system loss breakdown at rated output power. The system loss mainly contains MOSFET loss (including conduction and switching loss), magnetic loss, and diode loss (rectifier loss and reverse recovery loss). Because the proposed converter has soft-switching characteristic, the loss of the switch is the conduction loss. Using (25), the switch loss $P_{\text {sw }}$ can be calculated. Owing to the fact that an ultrafast recovery diode is adopted, the reverse recovery loss is neglected. Using (26), the conduction loss in a diode can be obtained.

$$
\begin{gather*}
P_{s w}=I_{d s, r m s}^{2} \square R_{d(o n)}  \tag{25}\\
P_{d}=I_{f d} V_{f d} \tag{26}
\end{gather*}
$$

Because the value of $L_{\mathrm{f}}$ reaches mH level, the resistor is relatively high which cannot be ignored. The series resistance loss in $L_{\mathrm{f}}$ is shown in (27).

$$
\begin{equation*}
P_{f}=I_{f, r m s}^{2} \square R_{f} \tag{27}
\end{equation*}
$$

Resistive loss $P_{\mathrm{r}}$ in the resonant tank is calculated in (28). $R_{\mathrm{r}}$ is the equivalent resistance in resonance tank.

$$
\begin{equation*}
P_{r}=I_{r, r m s}^{2} \square R_{r} \tag{28}
\end{equation*}
$$

System loss breakdown (W)


Fig. 17 System loss breakdown at rated output power
Lastly, the magnetic loss is discussed in detail. The magnetic material is NPX106019, which has 23.232 uH at a current of 0 A and 22.7 uH at a current of 10 A . The volume of magnetic core is $4.154 \mathrm{~cm}^{3}$ and cross-sectional area of magnetic core Ae is $0.654 \mathrm{~cm}^{2}$. The relationship between core loss $P_{\mathrm{cv}}$ and flux density $B$ is shown in Fig. 18.


Fig. 18 Relation between core loss $P_{\mathrm{cv}}$ and flux density B.
Fig. 19 shows the efficiency curve at different output powers. The peak efficiency can reach $94.85 \%$ at rated output power. Moreover, at different output power, the efficiency is higher than $84 \%$.

The comparison among the existing converters based on Class E circuit is shown in Table II. This research works adopt constant switching frequency. [20] mirrors Class E converter which eases the control method by phase shift method, but it has more components which increase the cost and decrease the power density. [22] adopts a new switch used as a rectifier diode to change the output voltage which also increases the system cost. [23] proposes a combined structure of Class DE and Class E which is regulated by phase shift method. But it still has no cost-advantage.


Fig. 19 Efficiency curve of Class E converter at different output power
TABLE II
Comparison of other research works and proposed converter

|  |  | [20] | [22] | [23] | Proposed <br> converte <br> r |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of Component S | Switche <br> s | 2 | 3 | 2 | 2 |
|  | Diodes | 2 | 2 | 1 | 1 |
|  | Caps | 4 | 2 | 3 | 2 |
|  | Inductor <br> S | 5 | 2 | 2 | 3 |
| Switching |  | 500 kH | 1 MHz | 1MH | 500 kHz |
| frequency |  | Z |  | Z |  |
| Power |  | 12W | 22.5 W | 2.5 W | 100W |
| Efficiency |  | 1 | 1 | 84\% | 94.5\% |
| Control method |  | Phase <br> Control | Controlled -Cap | Phase Contro 1 $\qquad$ | PWM |

## V. Conclusion

This paper proposed a 500 kHz anti-series two-switches Class E dc-dc converter. It has some advantages of constant working switching frequency and easy regulation of the output voltage. The proposed technique makes it possible to increase the operating frequency, thus allowing for an improvement of the converter power density. By changing the duty cycle of the additional switch $D_{2}$, ZVS operation for both active switches is achieved. Meanwhile the traditional Class E operation mode is not changed, and the components are easy to design.

The improvement of the proposed converter can be summarized as follows.

First, anti-series two switches structure can be integrated into one module which is good for high frequency working. The drive circuit is able to be added into this module. The parasitic capacitor and inductor have the least influence on high frequency drive.

Second, the control method can be simplified. Especially in resonant converter, duty cycle of low-side switch can be kept constant; an oscillating circuit (high frequency) can be utilized instead of a drive signal and drive IC. By regulating the highside switch, the output voltage can be controlled. Moreover, two switches can be? extended to phase shift control method.

Thirdly, the high-side switch keeps zero-voltageswitching characteristic, which is also good for high frequency application.

Finally, at the rated 100 W working condition, the peak efficiency can reach $94.85 \%$. However, in order to increase the system voltage gain, a transformer has better to be added.

It is also fair to highlight some drawbacks of the proposed converter. The high-side switch needs to adopt an isolated drive circuit, and the body diode of the high-side switch must be capable of handling the large resonant current. Normal Si-based MOSFETs are not competent. Wide band gap devices have more advanced thermal characteristic, high-frequency switching characteristic, higher withstanding voltage, etc. Therefore, adopting SiC or GaN device is the next research direction. In addition, magnetic design is another aspect to improve, which highly contributes to increase power density and efficiency.

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