

1 **TITLE**

2 Radiant heating floors with PCM bands for thermal energy storage: A numerical
3 analysis.

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9 **ABSTRACT**

10 Radiant heating floors with phase change materials (PCMs) for thermal energy storage
11 (TES) represent an opportunity to achieve improvements in energy efficiency in
12 buildings. In radiant floors that include PCM in macro-capsules the thermal energy is
13 stored during melting and subsequently released during solidification. This paper
14 presents a CFD study for hydronic radiant heating floors with PCM bands embedded in
15 a concrete core in accordance with several arrangements depending on the band width
16 and position with respect to the heating pipes. The heat transfer solutions are compared
17 with those obtained for radiant floors without PCM. Other effects analysed are: the
18 thickness of a wooden cover, which represents the main thermal resistance of the floors,
19 the indoor air temperature and the heating pipe surface temperature. The results show
20 that PCM radiant floors increase thermal energy storage up to 243% and decrease the
21 maximum heat flux between 10 and 18% according to the case. They also release the
22 heat slowly when the heating is off. The time-averaged heat fluxes during the
23 solidification process are between 31.4 and 44.6 W/m² and the solidification last for
24 more than 24 hours, allowing time to start a new charge using for instance solar energy.

25 **KEYWORDS**

26 Charge-discharge; RT28HC paraffin; phase change materials; radiant heating floors;
27 thermal energy storage

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32 **NOMENCLATURE**

33	A	Area of the cell surfaces (m^2)
34	A_{mush}	Constant in Eq. (6) (kg/s m^3)
35	a	Distance between PCM bands and the centre of the pipe (m)
36	b	PCM band width (m)
37	c_p	Specific heat at constant pressure (J/kgK)
38	D	Outer pipe diameter (mm)
39	E	Energy per unit of floor surface (Wh/m^2)
40	f	Fin coefficient (m^{-1})
41	\vec{g}	Acceleration due to gravity (m/s^2)
42	h	Heat transfer coefficient ($\text{W/m}^2\text{K}$)
43	i	Specific enthalpy (J/kg)
44	j	Index indicating cells in Eq. (7-9)
45	k	Thermal conductivity (W/mK)
46	M	Spacing between the centres of the pipes (m)
47	p	Pressure
48	\dot{q}	Heat flux (W/m^2)
49	\bar{q}	Heat flux averaged over time (W/m^2)
50	R	Thermal resistance ($\text{m}^2\text{K/W}$)
51	S_m	Volumetric momentum source term (N/m^3) in Eq. (6)
52	T	Temperature ($^{\circ}\text{C}$)
53	th	Thickness (m)
54	U	Overall heat transfer coefficient ($\text{W/m}^2\text{K}$)
55	V	Volume of the cell (m^3)
56	\vec{v}	Velocity vector (m/s)
57	\vec{v}_p	Drag velocity vector of the solid phase (m/s)
58	x	Length coordinate of the floor surface (m)

59 **Greek symbols**

60	β	Volumetric liquid fraction of the PCM (-)
61	Δt	Time-step (s)
62	ΔT_{melt}	Melting range (°C)
63	ε	Constant in Eq. (6) (-)
64	η	Efficiency (-)
65	λ	Phase change enthalpy of the PCM (kJ/kg)
66	μ	Dynamic viscosity (kg/ms)
67	ρ	Density (kg/m ³)
68	$\vec{\tau}$	Shear stress tensor (N/m ²)

69 **Subscripts**

70	<i>avg</i>	Averaged
71	<i>bhp</i>	Below heating pipes
72	<i>bs</i>	Bottom surface
73	<i>c</i>	Cover
74	<i>char</i>	Charge
75	<i>conc</i>	Concrete
76	<i>dis</i>	Discharge
77	<i>fs</i>	Floor surface
78	<i>hp</i>	Heating pipes
79	<i>iair</i>	Indoor air
80	<i>ins</i>	Insulation
81	<i>liq</i>	Liquid
82	<i>pcm</i>	Phase change material
83	<i>sol</i>	Solid temperature of the PCM
84	<i>ss</i>	Steady state

85	<i>tot</i>	Total
86	<i>uhp</i>	Upper heating pipes
87	Acronyms	
88	CFD	Computational Fluid Dynamics
89	DFST	Difference Floor Surface Temperature
90	FDM	Finite Difference Method
91	FEM	Finite Element Method
92	FVM	Finite Volume Method
93	MFST	Maximum Floor Surface Temperature
94	PCM	Phase Change Material
95	STC	Spanish Technical Code
96	TES	Thermal Energy Storage
97	TSI	Denomination for the method in [37] proposed by ASHRAE

98

99 **1. INTRODUCTION**

100 Radiant heating floors are widely used in buildings as they provide advantages such as
101 efficient use of space and uniform distribution of temperature, which produces
102 improved thermal comfort. Furthermore, they can operate at low water temperatures
103 with the consequent increase in the efficiency of the thermal generators [1] and a high
104 level of self-regulation [2]. Appropriate system design is essential to maintain comfort
105 conditions with adequate heat flux at the surface of the floor and suitable surface
106 temperature distribution [3]. There are standards, scientific documents and technical
107 guides that provide design criteria for sizing radiant heating floors [4, 5], while
108 numerous studies have established the theory of radiant systems demonstrating their
109 viability to control indoor conditions in the building efficiently [6]. Thermal energy
110 storage (TES) with phase change materials (PCM) allows not only compact storage, but
111 also isothermal release of heat or cold [7] and is increasingly used in many thermal
112 systems to achieve a more efficient use of energy [8, 9]. Furthermore, PCMs may be

113 included in building elements, providing greater thermal storage within a narrow
114 temperature range [10-13].

115 As for the type of research carried out, there are mathematical and experimental
116 approaches and there is also a wide variety of applications with combinations of types
117 of radiant floors and thermal systems. Lin et al. [14, 15] numerically [15] and
118 experimentally [14] investigated an under-floor electric heating system with shape-
119 stabilized PCM plates. A full model [15] was developed using the FDM for a test room
120 with under-floor heating powered with electric heaters that included a PCM layer over
121 them. The heat transfer was considered one-dimensional and conduction-based. Results
122 showed good performance: the energy was stored overnight in the PCM using cheap
123 electricity and discharged during the day. Barzin et al. [16] experimentally studied an
124 under-floor heating system based on a gypsum board impregnated with PCM for space
125 heating developing a price-based control system which achieved electricity savings in
126 terms of consumption and cost of up to 35% and 44.4%, respectively. Cheng et al. [17]
127 theoretically and experimentally studied the effect of the thermal conductivity of the
128 PCM in an under-floor heating system with a shape-stabilized PCM layer charged with
129 cheap, nighttime electricity.

130 Jin and Zhang [18] proposed a double PCM layer, one for heating and the other for
131 cooling, for an hydronic radiant floor with one row of pipes embedded in a concrete
132 core below PCM layers. These authors studied the thermal performance of a test room
133 following an FDM conduction-based numerical approach coupled with a one-
134 dimensional radiant heating floor. Numerical results showed that the energy released by
135 the radiant floor in peak periods increased between 41.1% and 37.9% compared to
136 conventional systems. Xia et al. [19] experimentally studied a hydronic radiant floor
137 system with a double layer of PCM with two rows of heating and cooling pipes
138 embedded in two different PCMs that can work both in summer and winter.

139 Cabrol and Rowley [20] simulated a building with an air-source heat pump system
140 coupled to a simplified floor slab-embedded PCM for the purposes of the TRNSYS
141 simulation. They concluded that the PCM floor slab improves the temperature stability
142 during the heating season and reduces the risk of overheating during the summer for a
143 high-performance building. Mazo et al. [21] developed a test room model to simulate a
144 hydronic radiant floor system with the PCM embedded in it. The system was powered

145 by means of a heat pump and the savings in electricity consumption costs were close to
146 18% compared to a conventional case. Lu et al. [22] designed a new radiant floor in
147 which the circumference of the outer pipe was wrapped with a layer of PCM and
148 mathematically modeled following a one-dimensional FVM approach. This hydronic
149 radiant floor was simulated in TRNSYS coupled to a solar water heating system and
150 was validated for full-scale experiments.

151 Huang et al. [23] numerically and experimentally studied a new type of hydronic radiant
152 heating floor with capillary pipes placed above and below a concrete skeleton in which
153 the empty cavities were stuffed with macro-encapsulated PCM. A two-dimensional FEM
154 conduction-based approach was developed and implemented using ANSYS. The results
155 showed that the PCM can release 3419 kJ/m^2 for 16 h in the discharge period, which
156 represented half of the energy supplied during the charge.

157 Zhou and He [24] carried out experiments to investigate the performance of a low-
158 temperature hydronic radiant floor with two types of heating pipes (conventional poly-
159 ethylene coils and capillary mat) embedded in a sensible or latent thermal mass for heat
160 storage, using sand and PCM, respectively. In addition, these authors applied a two-
161 dimensional conduction-based model which they successfully compared with
162 experimental data. The results showed that radiant floors with a capillary mat provide a
163 more uniform temperature profile and that a shorter time was needed to reach the same
164 room temperature. Regarding the heat release, results show that it lasts double of time
165 using PCM than using sand as thermal mass.

166 Zhao et al. [25] established a two-dimensional FLUENT-based CFD model employing
167 an enthalpy-porosity approach [26, 27] to model convection-diffusion mushy region
168 phase-change for a hydronic PCM radiant floor coupled with an air cavity in which the
169 pipes were fully covered by the PCM layer. They analysed the PCM liquid fraction and
170 temperature contours, finding that the PCM thermal conductivity played a major role in
171 maintaining the air temperature of the room during solidification. Moreover, these
172 authors proposed a new floor heat storage structure based on a combination of concrete
173 and PCM in the slab to accelerate the increase in air temperature.

174 The literature review shows that several kinds of radiant floors including PCM have
175 been studied following different approaches and geometrical configurations. PCM
176 embedded in radiant heating floors allows storing energy during the phase change, thus

177 enhancing the use of cheap power [14-17, 21] or renewable energy [22-24]. However,
178 there is still a shortage in the literature about the comparison of classical methods of
179 calculating radiant floors and multidimensional methods. In addition, there is still a
180 shortage of research on the study of effects related to the use of PCM, as those
181 concerning its placement, relationship with other materials included in the hydronic
182 radiant floor (heating pipes, concrete or mortar and cover) and operating conditions that
183 affect the overall performance of the system.

184 This paper discusses the heat transfer performance of hydronic radiant floors that
185 include phase change materials using a 2D approach. In the proposed PCM radiant
186 floors, the PCM is incorporated in alternating bars, macro-capsules, embedded in a
187 concrete core. Two basic arrangements will be studied: a) long parallelepiped PCM bars
188 containing one pipe inside, and b) two narrower parallelepiped PCM bars arranged
189 symmetrically between the heating pipes without direct contact with these pipes. These
190 designs have some differences with respect to alternative designs from literature as the
191 skeleton of concrete cavities filled with PCM proposed by Huang et al. in [23] and the
192 system of pipes completely embedded PCM suggested by Lu et al. in [25]. Both
193 arrangements have been designed with a concrete core structure that takes into account
194 the relative position between the PCM and the heating pipes: PCM_A (one heating pipe
195 embedded in PCM and the other not) and PCM_B (both heating pipes integrated in
196 concrete core). An asymmetric distribution of the PCM is tested in the PCM_A design
197 to discover how heat diffuses and to find out the temperature differences observed at the
198 level of the underfloor heating surface. On the other hand, the asymmetric arrangement
199 with alternatively integrated tubes also simplifies the construction of underfloor heating.

200 The CFD enthalpy-porosity approach is used for the phase change calculations to model
201 the convective effects in the PCM subdomains. Next to this, in order to compare the
202 thermal performance with classical radiant floors, which do not contain PCM inside,
203 two classical radiant floors based on concrete or high thermal conductivity mortar will
204 be analysed. For the classical radiant floors, the heat fluxes will be compared using
205 CFD conduction-based models and ASHRAE procedures in order to increase the
206 number of cases comparing calculation methods.

207 The study will consider both the charge and discharge periods. The charge period is
208 understood as the time during which water circulates through the heating pipes (the
209 temperature of the floor starts with a constant value which is the same of the heated

210 room) and the floor is heated while the mass of PCM is melted. The period of discharge
211 corresponds to the time when the circulation of water inside the pipes is interrupted and
212 the floor releases heat until the entire PCM solidifies.

213 **2. MODELLING**

214 **2.1. Physical model**

215 A schematic view of the two-dimensional computational domains (classical and PCM
216 radiant floors) is shown in Fig. 1: a) conventional radiant floor with concrete as thermal
217 mass and the heating pipes placed near the top of the concrete; b) Conventional floor
218 with improved thermal conductivity mortar and heating pipes placed near the insulation;
219 c) PCM underfloor heating with concrete core and long PCM bands with the heating
220 pipes embedded alternately in the PCM or in concrete, PCM_A, and d) PCM radiant
221 floor with a concrete core and two narrower PCM bands arranged symmetrically
222 between the heating pipes without direct contact between the PCM and the pipes,
223 PCM_B.

224 The geometric dimensions are the following: wooden cover thickness, th_c , taking
225 values of 10 and 20 mm; thickness of the insulation, $th_{ins}=50$ mm; outer heating pipe
226 diameter, $D=20$ mm; spacing between the centres of the pipes, $M=200$ mm. Two
227 thicknesses of concrete or mortar above and below the pipes will be considered for
228 classical radiant floors, depending on whether concrete or mortar is used. Above the
229 pipes, $th_{uhp}=10$ mm and $th_{uhp}=40$ mm, which correspond to the thicknesses below
230 pipes $th_{bhp}=30$ mm and 0 mm, respectively. For the PCM radiant floors, the
231 thicknesses of concrete above or below the pipes will be $th_{uhp}=10$ mm and $th_{bhp}=30$
232 mm. For PCM_B the dimensions $a=20$ mm and $b=47.5$ mm of the PCM bands were
233 obtained by keeping the same volume of PCM in both PCM floors.

234 The melting temperature of the PCM should be below the usual temperature for water in
235 the hydronic floor, approximately 40°C, and slightly higher than the recommended
236 temperature for the floor surface, 25-26 °C. The PCM used in the study is RT28HC
237 paraffin [28, 29], with properties in [30] and that has a latent heat of 224 kJ/kg and a
238 melting temperature range between 27 and 29°C corresponding to T_{soli} and T_{liq}
239 respectively, similar temperatures are tested in [21, 31] . The properties of the PCM,

240 concrete, conductive mortar, wooden cover and XPS insulation subdomains are shown
241 in Table 1.

242 The boundary conditions are of symmetry at the right and left sides of the floor domain.
243 For the heating pipe: fixed temperature or zero heat flux at the outer surface of the pipe,
244 depending on the process, charge or discharge, respectively. The condition of fixed
245 temperature during the charge (melting of the PCM) is adequate because the high
246 convective heat transfer coefficient of the water relatively to the low conductivity and
247 the high thermal inertia of the material surrounding the pipe. The condition of zero heat
248 flux is due to the fact that, during the discharge (solidification of the PCM), the heating
249 water pumps are turned off and the heat accumulated in the water can be neglected
250 relative to the heat accumulated in the floor materials and it dissipates quickly. For the
251 heat transfer coefficient at the floor surface, $h_{fs}=10 \text{ W/m}^2\text{K}$ will be considered for
252 simultaneous natural convection and radiation in accordance with the Spanish Technical
253 Code STC [32]. At the lower surface of the insulation material, the conductance
254 considered is $U_{bs}=2 \text{ W/m}^2\text{K}$, which was calculated as the inverse of the total thermal
255 resistance: sum of one due to a 300 mm concrete base, which supports the floor, and
256 another that combines the resistances in parallel due to natural convection and radiation
257 from the room below, all in accordance with the STC.

258 In order to study the floors under different heating conditions, a parametric study was
259 performed. They were considered two values for wooden cover thickness: 10 and 20
260 mm; three temperatures during the charge for the surface of the heating pipes T_{hp} : 35, 40
261 and 45°C; and another three temperatures for the indoor air temperature T_{air} : 18, 20
262 and 22°C, the last values near the comfort temperature of 20°C. With respect to the
263 surface temperature of the heating pipes, these values were chosen to guarantee a good
264 activation of the melting process during the charge period and, with respect to the air
265 temperature, to cover small temperature oscillations of the surrounding indoor air, being
266 the typical heating set point temperature 20 ° C.

267 The conservation equations were solved using the commercial CFD software ANSYS
268 Fluent. The following energy equation, Eq. (1), was used for the solid subdomains such
269 as the wood cover, concrete, mortar and insulation.

$$\frac{\partial}{\partial t}(\rho i) = \nabla \cdot (k\nabla T) \quad (1)$$

270 In solidification only conduction influences, but in fusion natural convection become
 271 important. To obtain heat transfer rate in PCM considering natural convection, most
 272 studies apply the enthalpy-porosity method to predict temperature distributions more
 273 accurately as in [33-38] and this method is the reference one for phase change in
 274 ANSYS Fluent. On the other hand, most of the models for PCM studies in the literature
 275 only consider conduction heat transfer. This enthalpy-porosity model has been validated
 276 in the literature as in [39-41].

277 The enthalpy-porosity formulation developed by Voller et al. [26, 27] was used for the
 278 PCM subdomains. In this approach, the liquid-solid mushy zone that represents the
 279 phase change region is treated as a porous zone whose porosity is equal to the
 280 volumetric liquid fraction. The volumetric liquid fraction, β , is defined as the fraction of
 281 the cell volume that is in liquid form. Porosity ranges between 0 and 1, depending on
 282 the status of the phase change process.

283 The conservation equations for mass and energy in the PCM subdomain are given in
 284 Eqs. (2, 3):

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \vec{v}) = 0 \quad (2)$$

$$\frac{\partial}{\partial t}(\rho i) + \nabla \cdot (\rho \vec{v} i) = \nabla \cdot (k \nabla T) \quad (3)$$

285 The solution of the problem is obtained following CFD methodology in ANSYS Fluent
 286 solving the continuity and energy equations, Eqs. (2, 3), and the liquid fraction
 287 equation, which follows Eq. (4), defined in terms of the temperature of the cell and
 288 range of phase change temperatures ($T_{soli} \leq T \leq T_{liq}$).

$$\begin{aligned} \beta &= 0 && \text{if } T < T_{soli} \\ \beta &= 1 && \text{if } T > T_{liq} \\ \beta &= \frac{T - T_{soli}}{T_{liq} - T_{soli}} && \text{if } T_{soli} \leq T \leq T_{liq} \end{aligned} \quad (4)$$

289 As regards the momentum equation, Eq. (5), the source term expressed by Eq. (6), \vec{S}_m ,
 290 is added due to the reduced porosity in the mushy zone:

$$\frac{\partial}{\partial t}(\rho \vec{v}) + \nabla \cdot (\rho \vec{v} \vec{v}) = -\nabla p + \nabla \cdot (\bar{\tau}) + \rho \vec{g} + \vec{S}_m \quad (5)$$

$$\vec{S}_m = \frac{(1 - \beta)^2}{(\beta + \varepsilon)} A_{mush} (\vec{v} - \vec{v}_p) \quad (6)$$

291 The term ε is a small number (0.001) to avoid division by zero, A_{mush} is the mushy
 292 zone constant, which measures the amplitude of the damping (the higher this value, the
 293 steeper the transition of the material velocity to zero as it solidifies), and \vec{v}_p accounts for
 294 the movement of the solidified material outside the domain, which is equal to 0 for this
 295 case.

296 The results calculated following Eqs. (7-9) in the cells at each time-step, were: the
 297 volume-averaged liquid fraction in the PCM subdomains, the area-weighted average
 298 temperatures and heat fluxes at the floor, bottom and heating pipe surfaces.

$$\beta_{avg} = \frac{1}{V} \int_V \beta dV = \frac{1}{V} \sum_{j=1}^n \beta_j |V_j| \quad (7)$$

$$(T_{fs}, T_{bs}) = \frac{1}{A} \int_A T dA = \frac{1}{A} \sum_{j=1}^n T_j |A_j| \quad (8)$$

$$(\dot{q}_{fs}, \dot{q}_{bs}, \dot{q}_{hp}) = \frac{1}{A} \int_A \dot{q} dA = \frac{1}{A} \sum_{j=1}^n \dot{q}_j |A_j| \quad (9)$$

299

300 2.3. Numerical procedure

301 The conservation equations were solved considering second-order implicit transient
 302 formulation. A second-order upwind scheme was used for the spatial discretization and
 303 the SIMPLE algorithm with PRESTO scheme for the pressure-velocity coupling. It was
 304 found that the solution is convergent and the minimum residue level (10^{-10} - 10^{-15}).

305 In order to define the grid size, the case of $th_c = 20$ mm, $T_{air} = 20^\circ\text{C}$, $T_{hp} = 40^\circ\text{C}$ was
 306 chosen. Floor domains were initialized at 20°C . Grid tests for solution independence
 307 were performed for the PCM radiant floors using three grids, varying the refinement
 308 level. Because of floors with PCM are more dependent on the refinement level, the grid

309 parameters obtained for the PCM floors test were also used for the conventional floors.
310 Table 2 shows the number of elements and the average and standard deviation of the
311 mesh quality, values closer to 1 indicating higher quality mesh [42]. All the grids
312 present high average quality with little deviation. Fig. 2 presents the results of the grids
313 test for a time-step, $\Delta t=0.5$ s, which value was chosen after testing several alternatives.
314 The solution becomes independent of the grid from grid refinement n° 2 onwards in
315 both PCM radiant floors; hence this grid was selected.

316 Natural convection can be the dominant mechanism of heat transfer in the melting
317 processes and its influence varies greatly with the dimensionless Rayleigh and Stefan
318 numbers, the aspect ratio of the PCM container, the location of the heating pipes and the
319 boundary conditions imposed [43]. As regards the reliability of the enthalpy-positivity
320 model, several studies have successfully compared this model with experimental data
321 [25, 39-41, 44]. For the enthalpy-porosity model, the parameter that controls the melting
322 rate in the solid-liquid transition is A_{mush} . The recommended value according to the
323 ANSYS Fluent theory guide [45] is 10^5 . This value was also used in previous papers
324 [37-38, 44-] and was therefore chosen for both geometries.

325 **2.4. Steady-state heat transfer rate calculation**

326 The heat transfer rate for classical radiant floors under steady-state conditions may be
327 calculated using Eqs.(10-13) following the method in [46], which is proposed by
328 ASHRAE [4]. This procedure is being used for design purposes and was successfully
329 compared with experimental data in [3]. The TSI model is for permanent regime and is
330 the one that is most recognized and complete that appears in the ASRHAE standards.
331 However, has the limitation of not to take into account heterogeneities in the installation
332 of the different materials and not consider non-linear thermal diffusivity. Even taking
333 into account these limitations when our proposed model reaches the steady state, the
334 TSI methodology can be adapted with better success in solidification, which is the most
335 interesting process because it is the slowest phase change process and when the heat is
336 dissipated into the room. In TSI method, the calculation of the steady-state heat flux,
337 $\dot{q}_{f,ss}$, considers the transverse heat diffusion using an equivalent fin coefficient, f ,
338 expressed in Eq. (12). The heat flux depends on the operating conditions and thermal
339 resistances above the heating pipes, $R_{uhp} = th_{uhp}/k_{uhp}$ and $R_c = th_c/k_c$, as well as
340 on the fin efficiency, η .

$$T_{hp} \approx T_{air} + \frac{\dot{q}_{fs,ss}M}{h_{fs}[M + D(1 - \eta)]} + \dot{q}_{fs,ss}(R_{uhp} + R_c) \quad (10)$$

$$\eta = \frac{2}{f(M - D)} \tanh \left[f \frac{(M - D)}{2} \right] \quad (11)$$

$$f = \left[\frac{h_{fs}}{\left(2 + \frac{R_c}{R_{uhp}}\right) (k_{uhp}th_{uhp} + k_c th_c)} \right]^{\frac{1}{2}} \quad (12)$$

$$R_{tot} = R_{uhp} + R_c + \frac{1}{h_{fs}} \quad (13)$$

341

342 Concerning the resistances above the heating pipes, k_c is the conductivity of the cover
343 and k_{uhp} the conductivity of concrete or mortar.

344 Concerning the PCM radiant floors, an equivalent thermal conductivity approach is
345 proposed for the layer of thickness th_{uhp} . This conductivity will be based on a parallel
346 resistance calculation: concrete and PCM macro-capsules. For both PCM radiant floors,
347 it was defined as the mean conductivity of the concrete and the PCM macro-capsule,
348 Eq. (14).

$$k_{uhp} = (k_{pcm} + k_{conc})/2 \quad (14)$$

349 **2.5. Application to steady and transitory regimens**

350 Steady-state and transient heat transfer in the radiant floors are analysed. For the radiant
351 floor including PCMs, during charging, the temperature at the surface of the heating
352 pipes T_{hp} is maintained and the provided energy is stored in the floor's thermal mass
353 (sensible or latent thermal energy) and is transmitted to the room. For the present study,
354 the duration of the charge will be kept at six hours for all the analysed cases, after which
355 the discharge will begin. During the discharge, the heat flux at the surface of the heating
356 pipes, \dot{q}_{hp} will be considered zero and the thermal energy stored by the floor's thermal
357 mass during the charge will be released to the room. The end of the discharge time will
358 be considered as the point at which the PCM becomes completely solidified.

359 First, the heat transfer rates for the steady-state are obtained depending on T_{hp} and th_c
360 with $T_{air}= 20^{\circ}\text{C}$. Subsequently, the transient heat transfer during the charge and the
361 discharge are analysed. They are studied the contours of the melted liquid fraction in the
362 PCM subdomains and of the temperature in the complete domains, and besides, the
363 floor surface temperature distribution for the case: $th_c=20$ mm, $T_{hp}=40^{\circ}\text{C}$ and
364 $T_{air}=20^{\circ}\text{C}$. The volume-averaged liquid fraction in the PCM subdomains and the heat
365 fluxes during the charge and discharge processes for the two cover thicknesses are
366 studied as well, along with the thermal energy balances, which allow compare the
367 radiant floors that include PCMs and the classical radiant floors for fixed operating
368 conditions of $T_{hp}=40^{\circ}\text{C}$ and $T_{air}=20^{\circ}\text{C}$ and for the two cover thicknesses th_c . Finally, a
369 parametric study for the PCM floors was performed in terms of th_c , varying the values
370 of T_{hp} and T_{air} . Melting and solidification times and time-averaged heat fluxes at the
371 floor surface during the charge and discharge processes are likewise discussed.

372

373 **3. RESULTS AND DISCUSSION**

374 **3.1. Main parameters and steady-state heat transfer rates**

375 In accordance with the previously explained calculations, Table 3 shows the main
376 parameters of the analysed PCM floors, according to Eqs. (10-14).

377 Fig. 3 presents the steady-state heat flux, which is the maximum heat transfer rate
378 transmitted at the radiant floor surface, for $T_{air}=20^{\circ}\text{C}$ and depending on T_{hp} and th_c .
379 These heat fluxes are obtained using the CFD model and the method proposed by
380 ASHRAE, with acronym TSI, Eqs. (10-14). This is The maximum heat flux range, 50-
381 110 W/m^2 for the classical radiant floor with the pipes embedded in the concrete, 60-
382 130 W/m^2 for the classical radiant floor with the pipes embedded in the mortar, and 45-
383 90 W/m^2 for the PCM radiant floors. This decrease in maximum heat transfer rates for
384 the PCM radiant floors is due to the low conductivity of the PCM compared to classical
385 materials (all concrete or mortar), which produces an increase in the total thermal
386 resistance, R_{tot} and a decrease in efficiency, η . Generally, the results show a good fit
387 between both calculation procedures with linear behaviour, similar slope, and small
388 offsets. However, it is important to note that with the lowest cover thickness (10mm)
389 and the lowest heating pipe surface temperature ($T_{hp} = 35^{\circ}\text{C}$), the CFD procedure

390 differs by up to 15%, showing a nonlinear trend in both configurations (PCM_A and
391 PCM_B). These results indicate that the steady state heat flux calculation for PCM
392 floors using the TSI procedure should be performed with a sufficient temperature
393 gradient between the heating pipe and the PCM melting point to decrease the effect of
394 nonlinearities, especially when PCM is poorly insulated. Another difference to consider
395 between two procedures is that TSI assumes one-dimensional heat transfer while CFD
396 is based on a two-dimensional model.

397 **3.2. Melted liquid fraction, temperature contours and floor surface** 398 **temperature distribution**

399 The liquid fraction in the PCM subdomains for both PCM radiant floors at different
400 charge times are given in Fig. 4, The liquid fraction contours are plotted for three
401 volume-averaged liquid fraction values (β_{avg}): 0.3, 0.6 and 0.95. The maximum, β_{max} ,
402 and minimum, β_{min} , values are also calculated. The aspect of the contours differs
403 substantially. For the case of PCM_A, the solid-liquid interphase progresses from the
404 heating pipe sideward and downwards with large melting zones: liquid ($\beta = 1$) in red
405 and solid ($\beta = 0$) in blue. For the case of PCM_B, the melting progresses from the hot
406 sides upwards, the contours in both PCM macro-capsules are symmetrical and the solid-
407 liquid interphase is less defined with a smoother transition.

408 The temperature contours are plotted in Fig. 5 at different charge and discharge times
409 for all the analysed radiant floors. The floor temperature field is symmetric for all the
410 floors except little differences caused by the PCM distribution in floor PCM_A. During
411 the charge, the classical floors heat faster than the PCM floors. The area-weighted
412 average temperatures at the floor surface, T_{fs} , at the end of the charge are respectively
413 26.5°C and 27.3°C for the concrete and mortar floors, and 25.6°C and 25.3°C for the
414 PCM_A and PCM_B floors. During the discharge, the classical radiant floors change
415 temperature faster than the PCM radiant floors, showing the very good accumulative
416 effect of the PCM, as the floor remains warm for a much longer time. In the last time
417 analysed, 21 h, the area-weighted average temperatures at the floor surface are
418 respectively 20.9°C and 20.7°C for the classical radiant floors (concrete and mortar),
419 and 23.1°C and 23.4°C for both PCM radiant floors.

420 The temperature distribution at points x (from 0 to 20 cm) at the floor surfaces are
421 represented against time in Fig. 6. Charge and discharge times are indicated with
422 continuous and discontinuous lines respectively. The melting progress is highly
423 influenced by the relative position of the heating pipes and PCM macro-capsules.
424 Temperature distribution results are summarized in Table 4 according to the maximum
425 floor surface temperature (MFST) and the difference between the maximum and
426 minimum floor surface temperatures (DFST). These parameters are related to thermal
427 comfort standards [3-5]: on the one hand, the MSFT must be limited; on the other, low
428 values of DFST are desired for thermal comfort. The highest MSFT value occurs at the
429 last instant of the charge (after six hours). This value is around 28°C for all the floors.
430 As to the DFST, significant differences exist between floors. The PCM floors have
431 higher DFST values than the classical floors. During the discharge, the DFST falls
432 rapidly for all floors except for PCM_A, in which the DFST first decreases and then
433 increases because the concrete cooled faster than the PCM. PCM_A is slightly less
434 recommended from the point of view of thermal comfort than PCM_B, because during
435 the discharge the DFST difference has a value of 0.3°C in PCM_B compared to a DFST
436 value of 1.4°C for PCM_A. The best performance is obtained with the mortar floor due
437 its higher conductivity, providing the greatest uniformity in temperature distribution
438 during both the charge and discharge processes.

439 **3.3. Volume-averaged liquid fraction, heat fluxes and thermal energy balance**

440 The evolution of the volume-averaged liquid fraction in the PCM floors during the
441 charge and discharge processes and of the heat flux at the surfaces of the heating pipes
442 during charging are presented in Fig. 7 for the four types of radiant floors as a function
443 of the thickness of the cover. Regarding the evolution of the volume-averaged liquid
444 fraction, the melting processes have finished before the end of the charge, which was
445 fixed at six hours. The melting is faster for PCM_A than for PCM_B, while the cover
446 thickness (10 or 20 mm) hardly influences the duration of this process (1.38 and 1.41h
447 for PCM_A and 4.21 and 4.10 h for PCB_B). Nevertheless, the influence of the cover
448 thickness during solidification is notable, the duration of the process being 24.31 and
449 31.19 h for PCM_A, and 19.56 and 25.65 h for PCM_B, respectively. Thus, decreasing
450 the cover thickness from 20 to 10 mm increases the solidification speed to 24% in floor
451 PCM_A and to 22% in PCM_ B. The heat fluxes then decrease to similar values to
452 those of the other radiant floor arrangements. The average heat fluxes at the surface of

453 the radiant floors during the charge and discharge processes are plotted in Fig. 8. The
454 heat fluxes increase during charging from zero to the maximum after six hours. At the
455 end of the charge, these values approach the heat fluxes for the steady-state. Depending
456 on the type of radiant floor and the cover thickness (10 and 20 mm), the heat fluxes
457 obtained for the classical radiant floors are 83.5 and 65.2 W/m² for the concrete radiant
458 floor and 93.6 and 73.2 W/m² for the mortar radiant floor. For the PCM radiant floors,
459 these values are 71.0. and 55.6 W/m² for PCM_A, and 70.2 and 53.4 W/m² for PCM_B.
460 Therefore, the PCM radiant floors take more time to charge and the steady-state
461 maximum heat fluxes are lower.

462 During the discharge process, the averaged heat fluxes at the surface of the floor
463 decrease from the maximum heat flux, which is reached during charging, to zero when
464 thermal equilibrium is reached. In Fig. 8, the behaviour of the PCM radiant floors was
465 plotted only until the PCM became solidified, at which point there is still sensible
466 thermal energy to release, and hence the time at which it becomes zero has still not been
467 reached. In the classical radiant floors, the heat flux falls rapidly, the heat fluxes being
468 below 20 W/m² in all the cases 10 hours after the discharge commences. In the PCM
469 radiant floors, the heat fluxes initially decrease rapidly, but then decrease slowly, due to
470 the stored latent heat, remaining at high levels during long periods (more than twelve
471 hours). The time-averaged heat fluxes during the discharge process for cover
472 thicknesses of 10 and 20 mm are respectively 37.9 and 31.4 W/m² for PCM_A and 44.6
473 and 35 W/m² for PCM_B. This behavior is highly suitable if the supplied heat fluxes are
474 enough to maintain conditions of comfort in the rooms where these floors may be
475 installed. The heat fluxes are maintained for more than 24 hours, allowing time to start a
476 new charge obtained, for instance, from solar energy.

477 Table 5 shows the thermal energy balances per unit of floor surface: supplied, released
478 and stored energies during the charge and complete discharge up to thermal equilibrium
479 (uniform floor temperature equal to indoor air temperature). The thermal energy stored
480 (TES) during the charge is calculated according to Eq.(15), the energy supplied by the
481 heating pipes being found to be 160-180% higher for the PCM floors than for the
482 classical floors. The thermal energy stored ranges between 445.5 and 552.0 Wh/m² for
483 the classical radiant floors and between 1141.0 and 1245.5 Wh/m² for the PCM radiant
484 floors. The amount of stored energy due to the PCM is 731.5 Wh/m². Hence, there is an
485 increase of 243% compared to the classical floors. The TES percentage in the last

486 column is calculated with respect to the energy supplied by the heating pipes; for the
487 classical radiant floors, this percentage ranges between 46.8-63.7%, the highest value
488 being obtained for the concrete floor and a cover thickness 20 mm. Similarly, for PCM
489 radiant floors, this percentages ranges between 74.7-82.8%.

$$TES = E_{hp} - E_{fs,char} - E_{bs,char} \quad (15)$$

490 Regarding the ratio of thermal energy transmitted to the heated room during the
491 discharge with respect to the charge period, columns fourth and sixth, the PCM radiant
492 floors have ratios ranging between 2.9 and 4.7 depending on the arrangement and the
493 cover thickness. With a cover thickness of 20 mm, PCM_B has the highest ratio, whilst
494 PCM_A, with a 10 mm cover thickness, has the lowest ratio of the PCM radiant floors.
495 For classical floors, these ratios range between 0.9 and 1.4 with the same behaviour
496 with respect to th_c , the highest ratios for the classical floors being obtained for the
497 concrete floor. The percentage of losses through the bottom surface does not fall below
498 10% for any case and fundamentally depends on the cover thickness.

499 **3.4. Performance of PCM radiant floors depending on heating conditions**

500 In this section, the PCM radiant floors are analysed under different heating conditions:
501 temperature at the surface of the heating pipes, T_{hp} , indoor air temperature of the heated
502 room, T_{iair} , and cover thickness. Melting and solidification times and time-averaged
503 heat fluxes transmitted, \dot{q}_{fs} , to the heated room at the floor surface during charging and
504 discharging are plotted in charts in Figs. 9 and 10, respectively.

505 The duration of the phase change processes shown in Fig. 9 decreases with T_{hp} and
506 T_{iair} during melting and increases during solidification with extreme T_{hp}, T_{iair}
507 operating temperatures pairs of 35, 18°C and 45, 22°C. With respect to th_c ; the melting
508 time increases very little with this parameter while, as discussed previously, the
509 solidification time decreases considerably. In each arrangement, the melting time is
510 mainly influenced by T_{hp} , whilst the solidification time depends strongly on T_{iair} and
511 th_c . As to the variations in thickness and heating conditions: for PCM_A, melting and
512 solidification last between 1.1 and 2.0 h and between 18.8 and 42.8 h, respectively,
513 while for PCM_B these times range from 2.7 to 8.4 h and from 10.3 to 36.1 h.
514 Comparing both arrangements, melting is much faster for PCM_A and solidification is
515 faster for PCM_B. Due to the non-linear performance of PCM radiant floors, these

516 differences depend strongly on the operating conditions, with rates that range from 2.6
517 to 4.2 for melting, and from 1.2 to 1.8 for solidification. Note that the melting process is
518 too slow for PCM_B when T_{hp} equals 35°C, with durations that range between 6.0 and
519 8.4 h depending on T_{iair} and th_c . This is mainly due to the distance from the heating
520 pipes and the PCM subdomains make it difficult to thermo-activate the melting process
521 at this temperature.

522 The time-averaged heat flux shown in Fig.10 increases with T_{hp} and decreases with
523 T_{iair} for charging and discharging with extreme T_{hp}, T_{iair} operating temperatures pairs
524 of 35, 22°C and 45, 18°C. The discharge time-averaged heat flux hardly varies with T_{hp} ,
525 as this temperature is the boundary conditions at the surface of the heating pipes during
526 charging and only influence the initial heat flux when the discharge process
527 commences. During this process, the boundary condition at the surface of the heating
528 pipes is zero heat flux, being the same for all cases. The influence of th_c is considerable
529 in the charge and discharge time-averaged heat fluxes, with higher values for the lower
530 thickness of 10 mm. As to the variations in cover thickness and heating; for PCM_A
531 charge and discharge time-averaged heat fluxes range from 31.5 to 82.5 W/m² and from
532 22.6 to 51.1 W/m², respectively; while for PCM_B, these heat fluxes range from 24.6 to
533 72.7 W/m² for charges and from 24.7 to 58.3 W/m² for discharges. Depending on the
534 thermal conditions and the cover thickness, heat transfer rates are between 12 and 22%
535 higher during charging and between 10 and 14% lower during discharging for PCM_A
536 than for PCM_B.

537 4. CONCLUSIONS

538 Heat transfer during charge and discharge periods for classical and hydronic PCM
539 radiant floors have been studied. In order to investigate the thermal performance, CFD
540 models were developed for classical radiant floors made of concrete and conductive
541 mortar, and for PCM floors with the PCM distributed in bands embedded in a concrete
542 core.

543 For the steady-state, the heat transfer rates obtained for the CFD models were
544 successfully compared with those calculated following the ASHRAE procedure.

545 Embedding of the PCM in the concrete core leads to a decrease in heat transfer, which
546 depends on the temperature at the surface of the heating pipes, ranging from 50-110
547 W/m^2 for classical concrete radiant floors to 45-90 W/m^2 for PCM radiant floors.

548 The thermal energy stored increases, depending on the cover thickness, ranging between
549 445.5-552.0 Wh/m^2 for classical floors and 1141.0-1245.5 Wh/m^2 for PCM floors.

550 During discharge, PCM radiant floors release the thermal energy stored with stable heat
551 fluxes near the time-averaged value during most of the discharge period.

552 Direct contact between the PCM and heating pipes, PCM_A, is essential to increase
553 melting rates. Melting is up to 4.6 times faster for PCM_A than for PCM_B. In contrast,
554 solidification is up to 1.8 times faster for PCM_B than for PCM_A.

555 The melting rates depend strongly on the temperature of the heating pipes during the
556 charge, whilst solidification rates depend mainly on the indoor air temperature of the
557 heated room and the cover thickness.

558 Heat transfer rates to the heated room are 12-22% higher for PCM_A than for PCM_B
559 during charging and are 10-14% higher for PCM_B than PCM_A during discharging.

560 The PCM radiant floors tested by varying the temperature of the heating pipes and of
561 the room provide wide ranges for the durations of the phase change processes and for
562 the heat transfer rates. This thermal performance is suitable for radiant heating floors in
563 households with different thermal qualities of the envelope.

564 **ACKNOWLEDGMENTS**

565 We wish to express our gratitude to the University Institute of Industrial Technology of
566 Asturias (IUTA), the Ph.D. programme in Energy and Processes Control, University of
567 Oviedo, and Gijon City Council for financial support under project SV-17-GIJÓN-1-22,
568 which made this research work possible.

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689 **TABLES**

690 **Table 1.** Thermal properties

Materials (cell zones)	ΔT_{melt} (°C)	ρ (kg/m ³)	c_p (J/kg·K)	k (W/m·K)	μ (kg/m·s)	λ (kJ/kg)
RT28HC (PCM)	27-29	770-880	2000	0.2	0.00239	224
Concrete	-	1800	1050	0.93	-	-
Conductive mortar	-	1600	950	2	-	-
XPS (Insulation)	-	30	1260	0.028	-	-
Wood (Cover)	-	70	2310	0.173	-	-

691

692 **Table 2.** PCM floors grid test. $\Delta t=0.5s$, $A_{\text{mush}}=10^5$, $th_c=20$ mm, $T_{\text{air}}=20^\circ\text{C}$, $T_{hp}=\$

693 40°C

Grid Refinement	Floor case	Elements	Mesh quality	
			Avg.	St. dev.
1	PCM_A	3647	0.91	0.075
	PCM_B	3775	0.90	0.071
2	PCM_A	8196	0.92	0.067
	PCM_B	8490	0.92	0.062
3	PCM_A	14836	0.92	0.063
	PCM_B	15356	0.92	0.058

694

695 **Table 3.** Main parameters of the floors for the application of the method proposed by
 696 ASHRAE

Floor case	th_c (mm)	th_{uhp} (mm)	k_{uhp} (W/mK)	R_c (m ² °K/W)	R_{uhp} (m ² K/W)	R_{tot} (m ² K/W)	f (m ⁻¹)	η (-)
CONC	10	10	0.93	0.058	0.011	0.169	20.813	0.487
	20	10	0.93	0.116	0.011	0.227	19.569	0.535
MORT	10	40	2	0.058	0.020	0.178	7.504	0.859
	20	40	2	0.116	0.020	0.236	7.578	0.869
PCM_A,B	10	10	0.565	0.058	0.018	0.176	25.086	0.413
	20	10	0.565	0.116	0.018	0.234	22.992	0.468

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702 **Table 4.** Maximum floor surface temperature (MFST) and difference between the
 703 maximum and minimum floor surface temperature (DFST) at the floor surface for
 704 $th_c = 20$ mm, $T_{i,air} = 20^\circ\text{C}$, $T_{hp} = 40^\circ\text{C}$ and several times.

CONC							
	Charge			Discharge			
t(h)	0.5	2	6	8	11	16	21
MSFT	24.5	27.3	28.0	25.2	23.5	21.8	20.9
DFST	4.5	4.9	2.5	0.05	0.08	0.04	0.02
MORT							
	Charge			Discharge			
t(h)	0.5	2	6	8	11	16	21
MSFT	22.4	26.8	27.9	25.9	23.6	21.6	20.7
DFST	1.9	1.7	0.9	0.2	0.1	0.05	0.02
PCM_A							
	Charge			Discharge			
t(h)	0.5	2	6	8	11	16	21
MSFT	24.5	27.4	28.0	24.9	24.0	23.9	23.7
DFST	4.5	3.6	3.7	0.8	0.8	1.4	1.4
PCM_B							
	Charge			Discharge			
t(h)	0.5	2	6	8	11	16	21
MSFT	24.5	26.3	28.0	24.5	24.0	23.7	23.5
DFST	4.5	4.3	4.1	0.5	0.3	0.3	0.3

705

706 **Table 5.** Thermal energies supplied, released and stored during charging and complete
 707 discharging for $T_{air}= 20^{\circ}\text{C}$, $T_{hp}= 40^{\circ}\text{C}$.

Radiant Floor	th_c (mm)	E_{hp} (Wh/m ²)	$E_{fs,char}$ (Wh/m ²)	$E_{bs,char}$ (Wh/m ²)	$E_{fs,dis}$ (Wh/m ²)	$E_{bs,dis}$ (Wh/m ²)	TES (Wh/m ²)	(%)
CONC	10	908.5	395.0	27.5	446.0	40.5	486.0	53.5
	20	866.0	286.0	28.0	495.0	57.0	552.0	63.7
MORT	10	952.0	469.0	37.5	412.0	34.0	445.5	46.8
	20	893.5	340.5	38.0	465.0	49.5	515.0	57.6
PCM_A	10	1584.0	375.5	26.0	1092.0	90.5	1182.5	74.7
	20	1546.0	274.0	26.5	1121.0	124.5	1245.5	80.6
PCM_B	10	1482.0	320.0	21.0	1055.0	86.0	1141.0	77.0
	20	1440.0	227.0	21.0	1074.0	118.0	1192.0	82.8

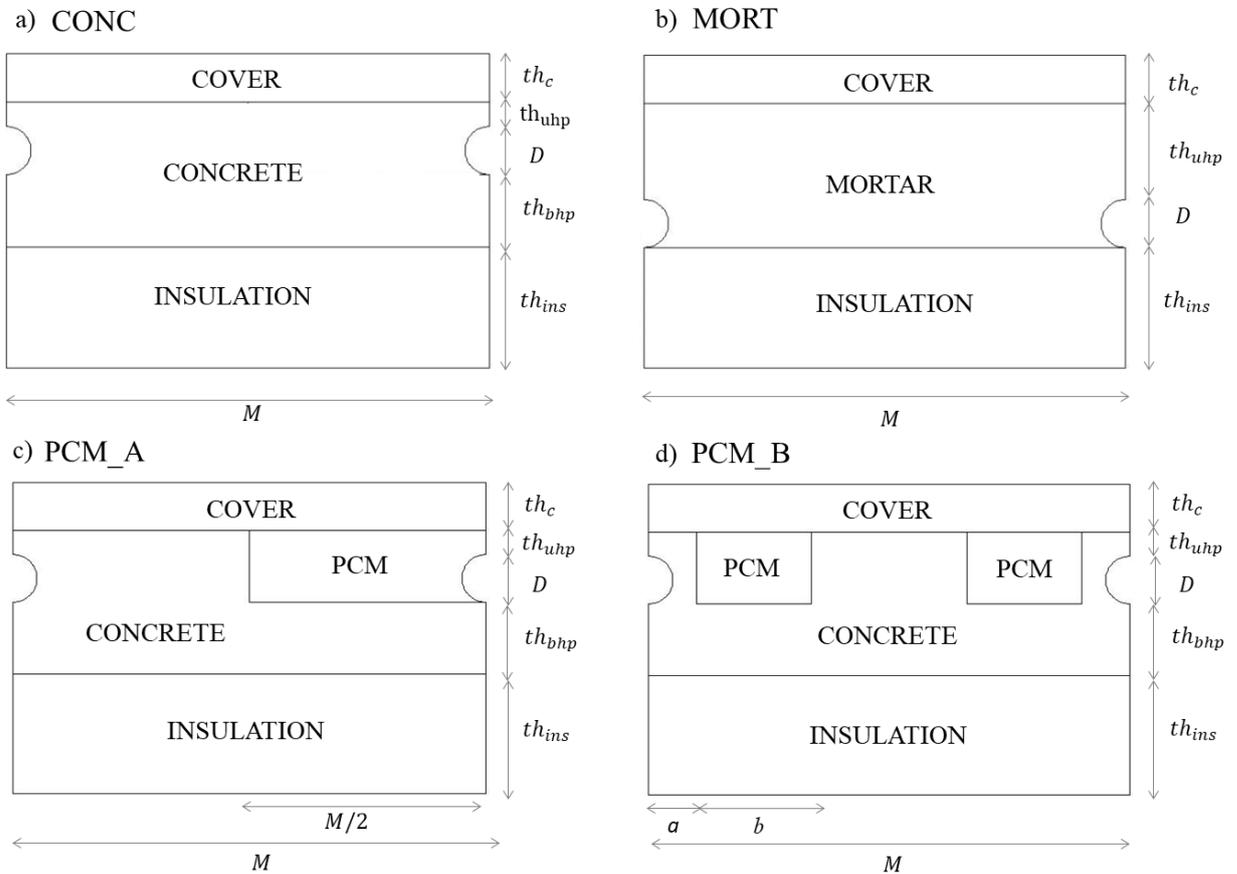
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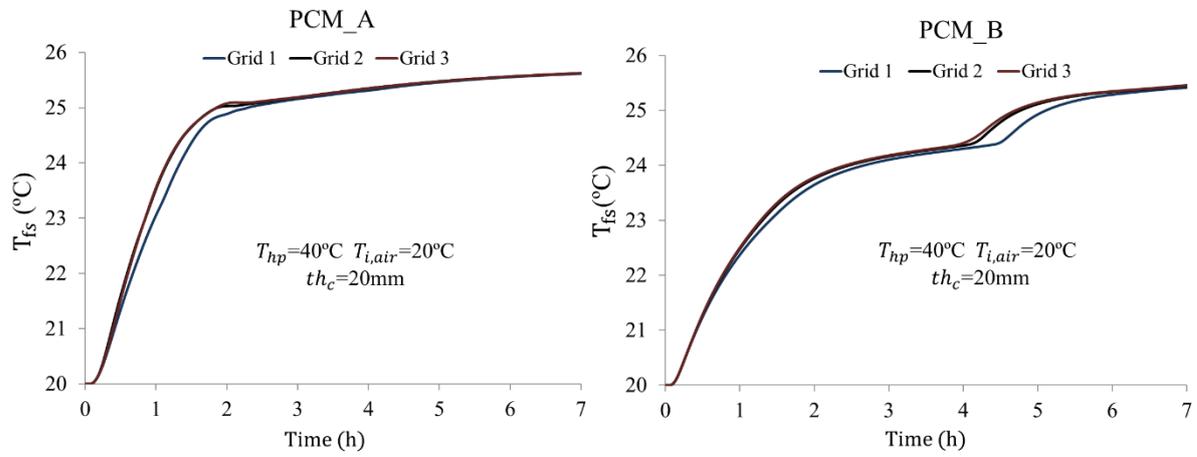
712 **FIGURES**



713

714 **Figure 1.** Computational domain: convectonal (a, b) and PCM (c, d) radiant floors.

715

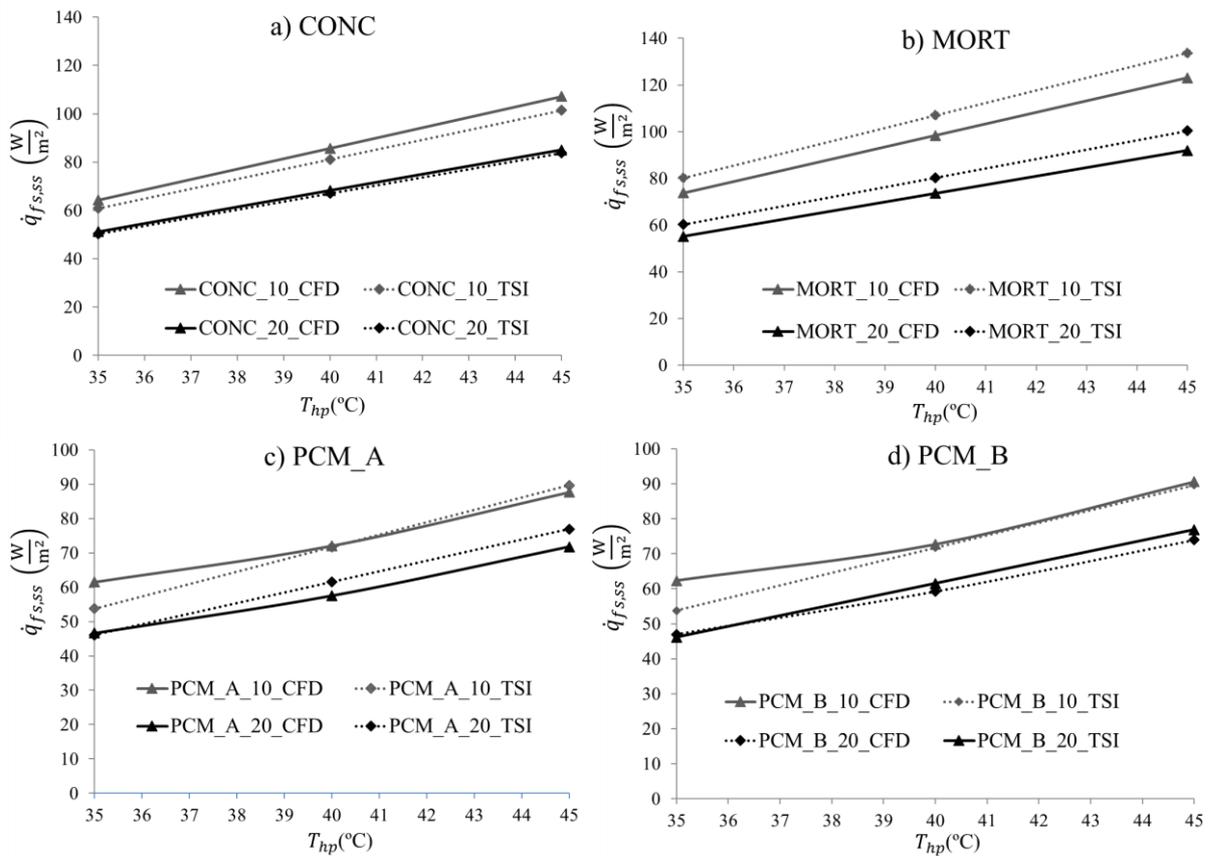


716

717 **Figure 2.** Grid test results for PCM floors for $\Delta t=0.5\text{s}$, $A_{mush}=10^5$, $th_c=20\text{mm}$, $T_{i,air}=20^{\circ}\text{C}$, $T_{hp}=40^{\circ}\text{C}$.

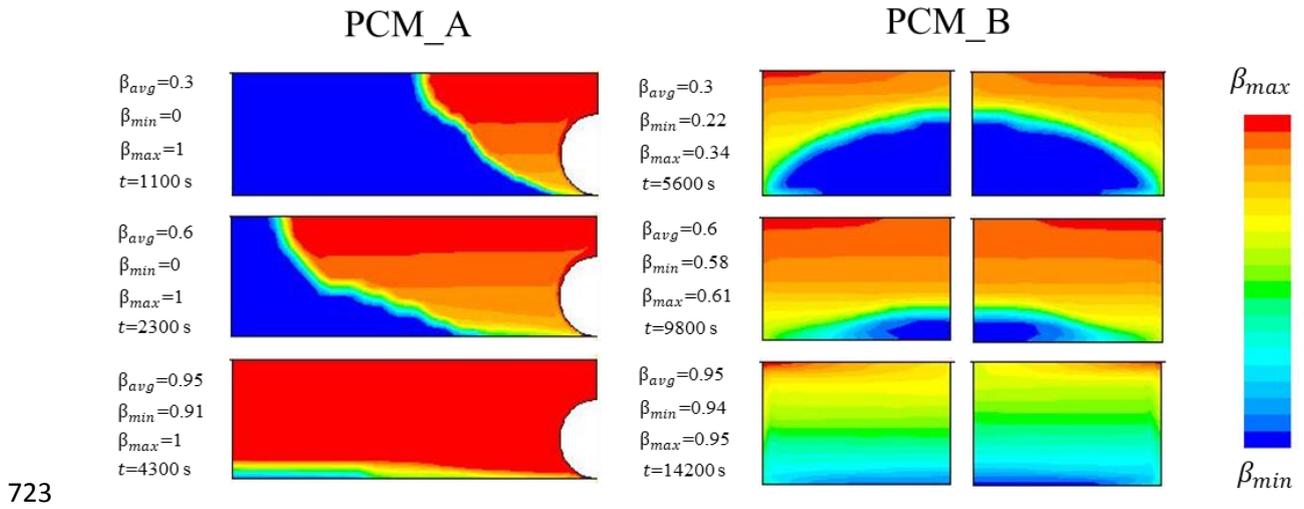
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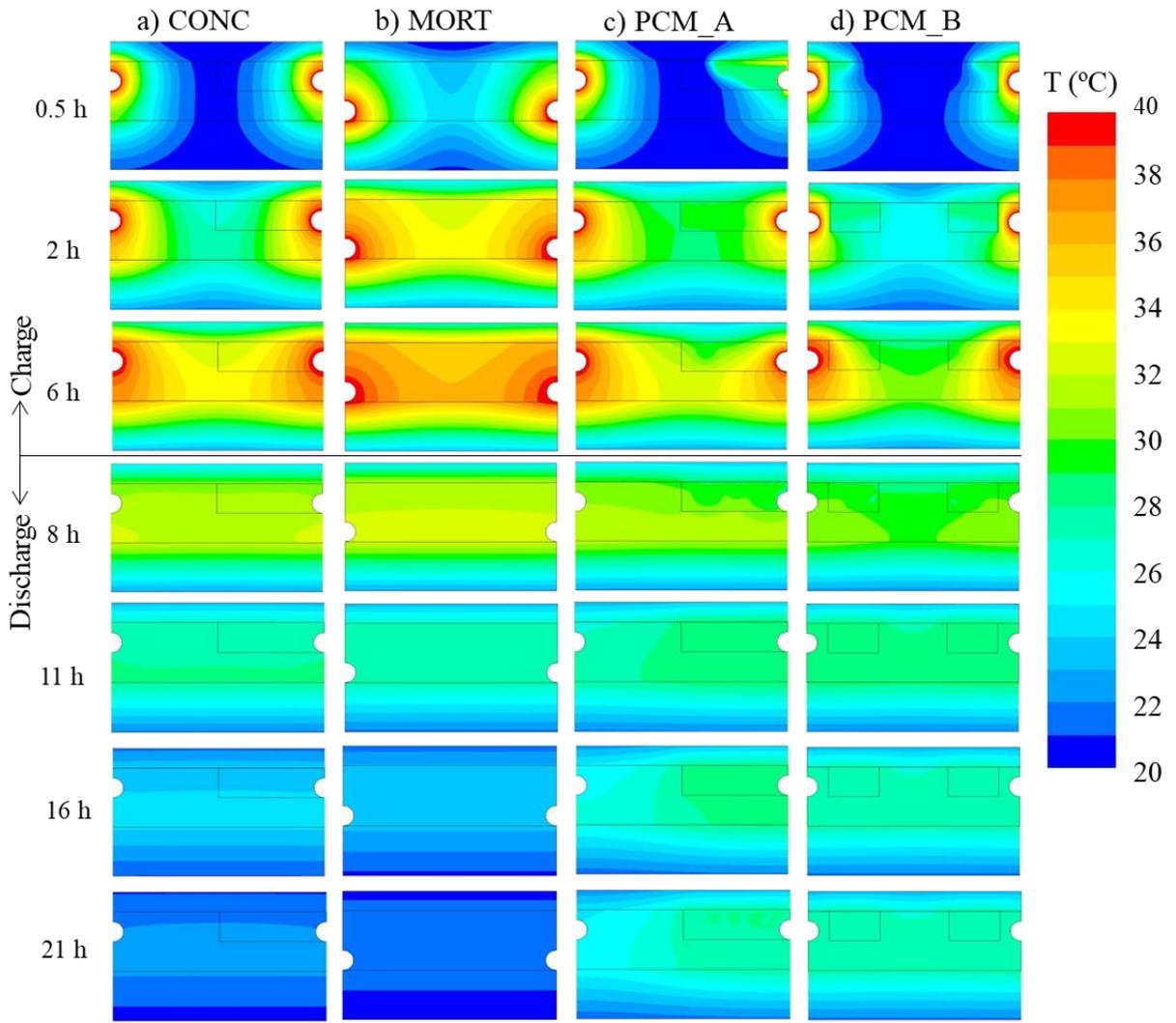


720

721 **Figure 3.** Steady-state heat transfer rates computed by CFD and TSI (proposed by
 722 ASRHAE) procedures for $T_{i\text{air}}=20^\circ\text{C}$.



724 **Figure 4.** Melted liquid fraction in PCM subdomains for $th_c=20\text{ mm}$, $T_{i\text{air}}=20^\circ\text{C}$,
 725 $T_{hp}=40^\circ\text{C}$.

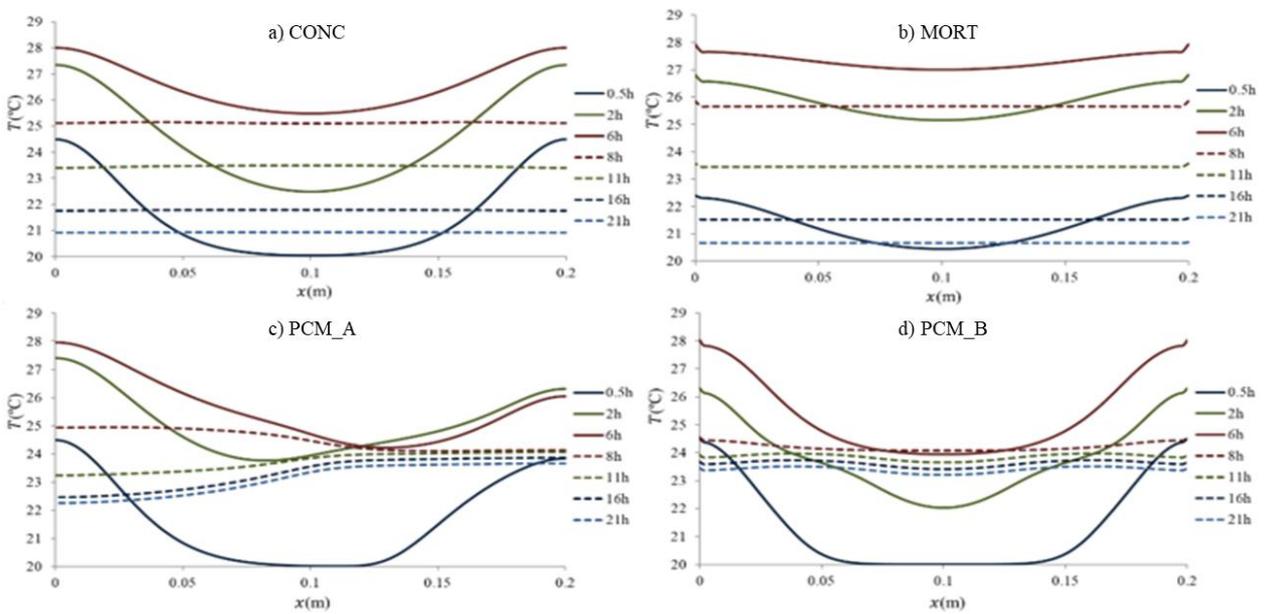


726

727 **Figure 5.** Temperature contours in the materials of the radiant floors for the charge and

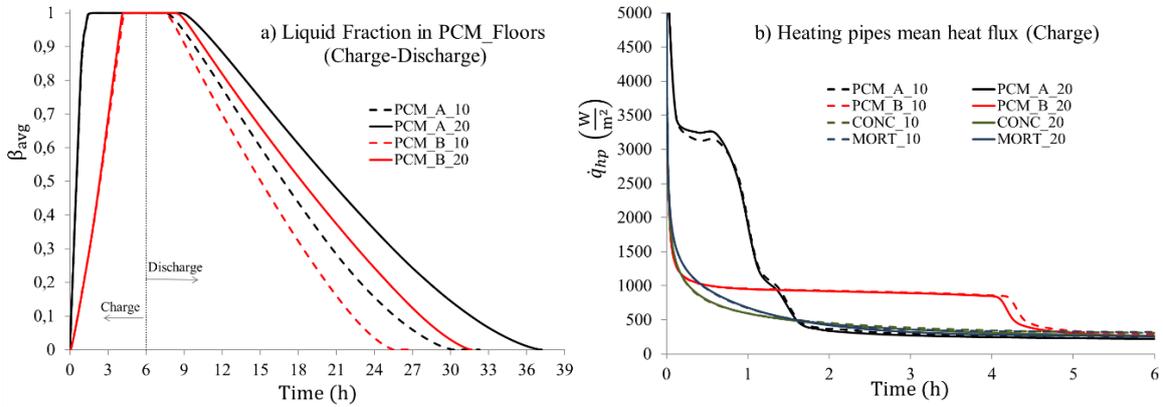
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the discharge for $th_c = 20$ mm, $T_{iair} = 20^\circ\text{C}$, $T_{hp} = 40^\circ\text{C}$.



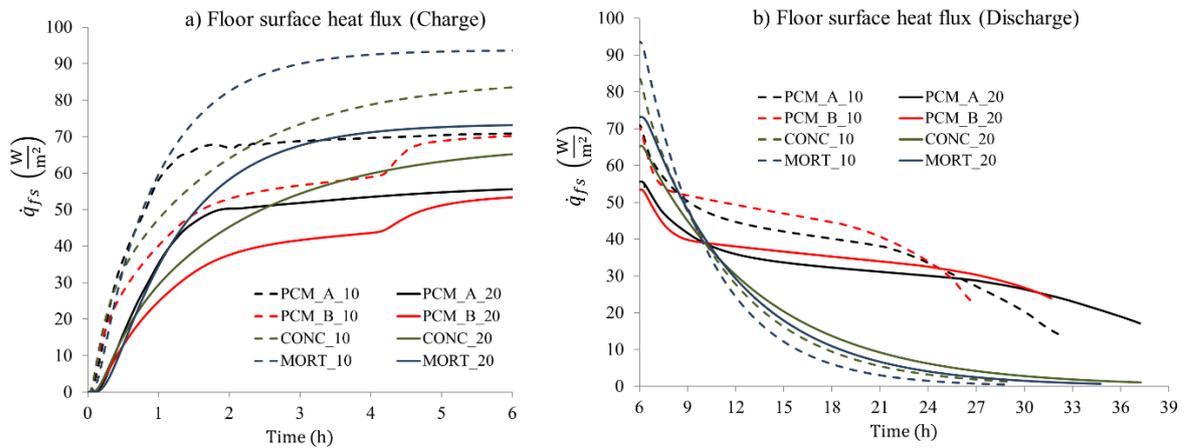
729

730 **Figure 6.** Temperature distribution during the discharge at points on the surface of the
 731 radiant floors for $th_c = 20$ mm, $T_{i\text{air}} = 20^\circ\text{C}$, $T_{hp} = 40^\circ\text{C}$.



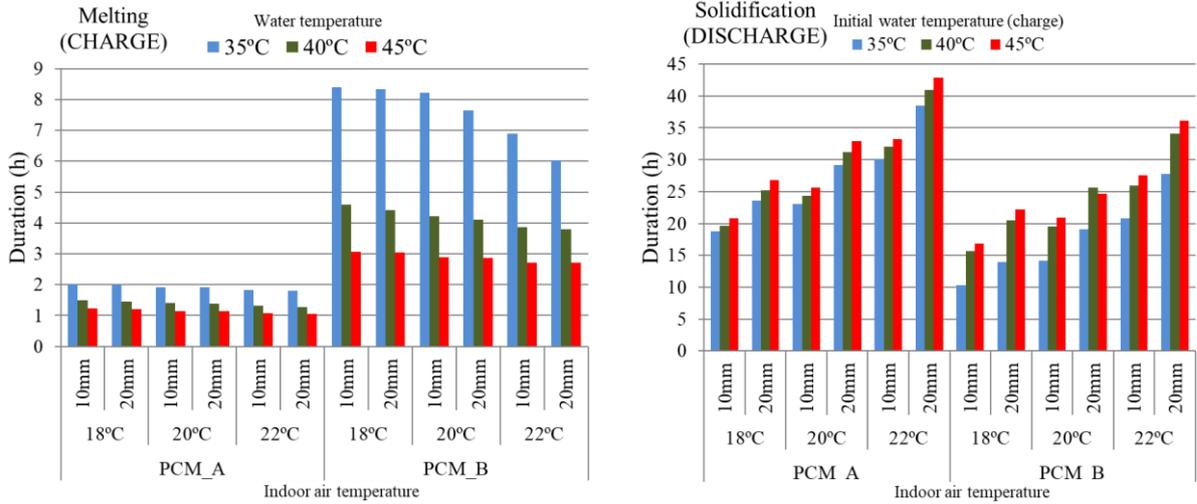
732

733 **Figure 7.** Evolution of averaged variables for $T_{i\text{air}} = 20^\circ\text{C}$ and $T_{hp} = 40^\circ\text{C}$ as a function
 734 of the cover thickness: a) liquid fraction for PCM floors during charging and
 735 discharging, and b) heat fluxes for the four radiant floors at the surface of the heating
 736 pipes during charging.



737

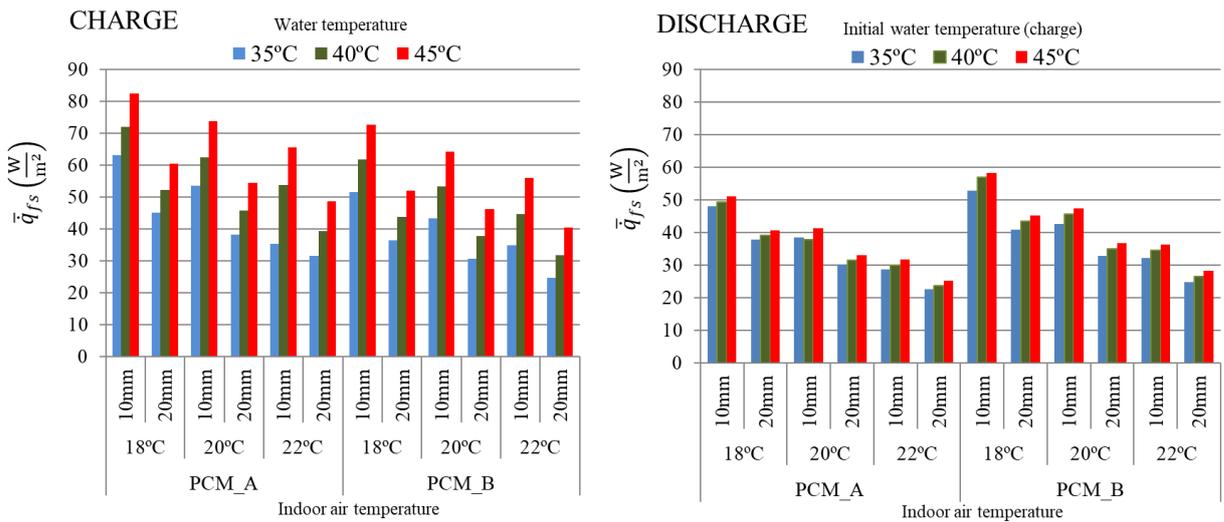
738 **Figure 8.** Evolution of the averaged heat fluxes at the surfaces of the radiant floors for
 739 $T_{i\text{air}} = 20^\circ\text{C}$ and $T_{hp} = 40^\circ\text{C}$ as a function of the cover thickness: a) charging b)
 740 discharging.



741

742 **Figure 9.** Melting and solidification times for PCM floors according to the temperature of
 743 the water inside the pipes, room temperatures and cover thickness.

744



745

746 **Figure 10.** Time-averaged heat fluxes at floor surface during charging and discharging
 747 for PCM floors depending on conditions: the temperature of the water inside the pipes,
 748 room temperatures and cover thickness.

749