

# Mechanical Response of Polymer Epoxy/BMI Composites with Graphene and a Boron Nitride Monolayer from First Principles

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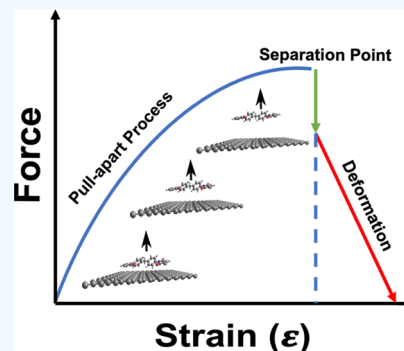
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**ABSTRACT:** Polymer composites possess an integrated combination of structures and properties associated with the host matrix and the fiber material and thus hold the potential of being high-strength materials. In general, the load transfer from the matrix to the fiber depends upon the strength of bonding at the interface, which characterizes the mechanical strength. In this work, first-principles calculations based on the density functional theory are employed to provide the molecular-level description of the interface formed by resins (i.e., diglycidyl ether of bisphenol A (DGEBA) and 4'-bismaleimidodiphenylmethane (BMPM)) or hardeners (i.e., diethyl toluene diamine (DETDA) and *o,o'*-diallyl bisphenol A (DABPA)) with graphene (or boron nitride (BN) monolayer). The results show that the interaction strength between a resin (or hardener) and graphene is mainly governed by the nature of bonding at the interface, and subsequently, the mechanical response follows the hierarchical order of the interaction strength at the interface; the transverse stiffness of BMPM/graphene is higher than that of DGEBA/graphene. Moreover, the change in the polarity of the surface from graphene to the BN monolayer improves the superior interfacial strength and thereby a higher transverse stiffness of both resin and hardener composites at the molecular level. These results emphasize the need to use computational modeling to efficiently and accurately determine molecular-level polymer/surface combinations that yield optimal mechanical performance of composite materials. This is especially important in the design and development of high-performance composites with nanoscale reinforcement.

**KEYWORDS:** *mechanical properties, epoxy, BMI, graphene, BN monolayer, density functional theory*



## 1. INTRODUCTION

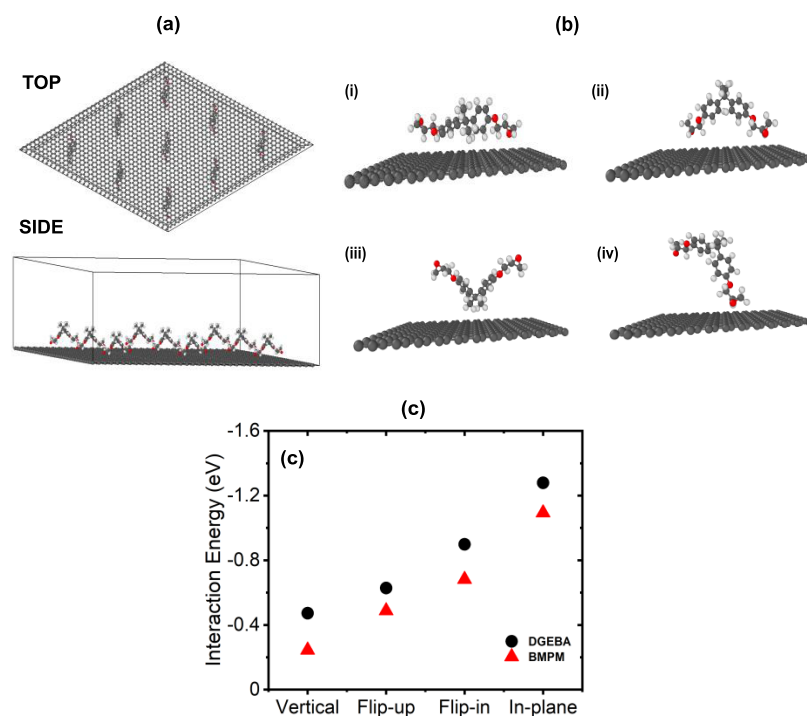
In a fiber–polymer composite system, fibers play an important role of load-bearing components, and the polymer matrix provides support to fibers by maintaining their orientations in the composite. In recent years, the use of carbon nanotubes (CNT) as a fiber element has helped to make significant advances in transport technology due to their low weight-to-stiffness ratio, resistance to environmental impact, and processability.<sup>1–3</sup> The C–C covalent bond in carbon rings, which is regarded as the most stable chemical bond in nature, endows graphitic surfaces with excellent mechanical properties,<sup>4,5</sup> thereby making them promising candidates for the next generation of high-performance composites. For example, Young's modulus of CNTs with a density of 1.33 g/cm<sup>3</sup> can be as high as 1 TPa.<sup>6–8</sup> Therefore, focused scientific efforts have been invested in engineering CNT-based composites that exploit the outstanding mechanical properties of individual CNTs. However, the stiffness and strength of individual CNTs have generally not transferred well to large-scale assemblages. To address the abovementioned challenge, both experimental<sup>9–12</sup> and theoretical<sup>13–16</sup> methods have been used to investigate the interface formed by a CNT fiber with the polymer matrix to gain insight into its role in determining the mechanical response of the composite. For example, it has

been shown that sliding occurs within the fractured fibers of long CNTs leading to a poor load transfer,<sup>17</sup> and multiwalled CNTs are often deformed and twisted, which increases their flexibility.<sup>18</sup> One weakness of CNT assemblages is the inadequate noncovalent interaction between adjacent circular CNTs, which leads to the slippage of CNTs during deformation.<sup>17</sup> Hence, it was recently proposed to fabricate self-assembled stacks of large-diameter (~10 nm) CNTs, referred to as flattened CNTs (fCNTs), which maximizes the contact area between CNTs, and thus the noncovalent type of bonding.<sup>19</sup> Therefore, it appears possible that the mechanical properties of the fCNT composite may be further enhanced by carefully engineering its interface.

Also, flattened CNTs, which are referred to as a “dog-bone”-type collapse in the scientific literature, have been linked to improved mechanical performance because of their similarity to graphitic carbon.<sup>20</sup> They can be considered as stacked layers

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**Figure 1.** (a) Top and side views of a complex. (b) Molecular orientations: (i) in-plane, (ii) flip-in, (iii) flip-up, and (iv) vertical over graphene. Atomic color codes—O (red), C (gray), and H (white). (c) Orientation-dependent interaction energy of DGEBA (red) and BMPM (black) interacting with graphene.

63 of graphene, which is a two-dimensional hexagonal monolayer  
64 with  $sp^2$  hybridized covalent bonds.<sup>21</sup> The van der Waals  
65 (vdW) interaction terms between the graphene planes provide  
66 the stability to flattened CNTs that possess reactive edges, and  
67 the curvature of which can be used to control not just chemical  
68 and mechanical properties, but thermal and electronic  
69 properties as well.<sup>22</sup>

70 Among polymers, epoxies containing epoxide groups and  
71 bis-maleimides (BMI) containing maleimide groups (Figure  
72 S1) are the most commonly used thermosetting resins<sup>23</sup> for  
73 making high-performance composites because they provide a  
74 unique balance of thermal and mechanical properties  
75 combined with extreme processing versatility.<sup>24,25</sup> It is worth  
76 mentioning that diglycidyl ether of bisphenol A (DGEBA) and  
77 4'-bismaleimidodiphenylmethane (BMPM) are some of the  
78 most widely used high-performance epoxies and BMI resins in  
79 the aerospace industry. For example, the fifth-generation  
80 combat aircraft F-35 Lightning II developed by Lockheed  
81 Martin is stated to consist of about 35% carbon fiber  
82 composites out of the entire structural weight, and the primary  
83 structural composites used in the aircraft are composed of  
84 either epoxy or BMI matrices. Although other matrices like  
85 polyethylene and polystyrene facilitate a mechanical response  
86 at room temperature that satisfies property requirements for  
87 some applications, there exist challenges in using such matrices  
88 in more rigorous applications as it does not perform well at  
89 elevated temperatures.<sup>26,27</sup> This is not the case with either  
90 epoxy (DGEBA) or BMI (BMPM) as both are stable at  
91 elevated temperatures.<sup>28,29</sup> Note that DGEBA and BMPM  
92 monomers are often crosslinked with diethyl toluene diamine  
93 (DETDA) and *o,o'*-diallyl bisphenol A (DABPA) monomers,  
94 respectively. DETDA is an aromatic amine curing agent, and  
95 DABPA is allylphenol that offers excellent toughness to the  
96 BMPM.<sup>30,31</sup>

In general, a detailed understanding of the interaction  
between graphene and a resin (hardener) matrix at the  
molecular level is crucial for improving the composite's  
mechanical response. This is because the adhesion between a  
resin (hardener) and graphene is related to the chemistry of  
the interface<sup>2,32</sup> which has, without any doubt, a considerable  
influence on the fracture/failure behavior of a composite,  
although it is not yet understood completely. We are aware of  
only a few theoretical studies based on atomistic modeling that  
were used to characterize the interfacial bonding in  
composites.<sup>33–35</sup> Overall, it has been recognized that the  
interface plays a significant role in the stress transfer and the  
consequent improvements in the composite stiffness and  
strength.<sup>36,37</sup>

In the following, we will present the results related to  
graphene/resins (hardeners) focusing on the characterization  
of the interface at the molecular level using a periodical  
supercell model. The mechanical response in terms of the  
separation point (or breaking point) and stiffness will be  
determined. Within this atomic framework, one can directly  
modify the interface, even with modifications that are  
extremely difficult or impossible to control in the experiment,  
to predict the consequences on the interfacial strength and  
thereby its mechanical response.

The resin (hardener) monomers, DGEBA (DETDA) and  
BMPM (DABPA), interacting with the surface of graphene are  
explored. Figure 1a shows the top and side views of a  
monomer forming a complex with graphene in a periodic  
supercell. It should be noted that our focus is not on the cured  
polymer composites, rather on individual monomers to  
provide a fundamental understanding of the structure–  
property relationship in graphene–polymer composites. More-  
over, we will also consider the cases of these monomers  
interacting with a boron nitride (BN) monolayer to benchmark

131 the results obtained for monomer/graphene complexes. Both  
132 graphene and BN monolayer are structurally similar, but  
133 electronically dissimilar materials; the covalently linked  
134 graphene is a zero-gap material, whereas the semi-ionic h-BN  
135 monolayer, which has a nearly identical honeycomb config-  
136 uration as that of graphene, is semiconducting.<sup>38</sup>

## 2. COMPUTATIONAL METHOD

137 Electronic structure calculations were performed using  
138 projector-augmented wave (PAW) potentials within the  
139 framework of the density functional theory (DFT), as  
140 implemented in the Vienna ab initio simulation package  
141 (VASP).<sup>39</sup> The exchange and correlation potentials were  
142 treated using a generalized gradient approximation (GGA)  
143 with the Perdew–Burke–Ernzerhof (PBE) functional form.<sup>40</sup>  
144 Contributions from the van der Waals (vdW) interactions,  
145 which are important for graphitic systems, were incorporated  
146 using Grimme’s semiempirical dispersive D2 term.<sup>41</sup> The  
147 energy cut-off and the convergence criterion of the energy were  
148 500 and  $10^{-5}$  eV, respectively.

149 In a supercell, the periodic boundary conditions with a  
150 lateral separation along the *c*-direction of 20 Å were employed  
151 to ensure the negligible interaction between the periodic  
152 images. The relaxation process for the equilibrium config-  
153 uration was carried out by placing a monomer on the top of  
154 graphene in various orientations, and the distances between  
155 them were set to a value that was slightly larger (or similar to)  
156 than the sum of the nearest resin (hardener) atom and  
157 covalent radii of carbon atoms. The structure was then relaxed  
158 using the conjugate gradient algorithm until the maximum  
159 forces acting on the atoms became smaller than 0.001 eV/Å.

160 The mechanical response of the complex consisting of a  
161 resin (or hardener) and graphene (or BN monolayer) was  
162 investigated in a way that mimics the “pull-apart” experimental  
163 setup commonly used for polymer composites.<sup>9,42–44</sup> In our  
164 setup, a resin, which was in the equilibrium configuration, was  
165 pulled up along the direction perpendicular to the surface of  
166 the constrained (frozen) graphene. DFT calculations were  
167 performed for each step of the pull-apart process to generate  
168 the energy surface describing the interaction of a resin  
169 (hardener) with graphene.

170 In the pull-apart setup, we define the tensile strain to be the  
171 perpendicular displacement between a resin (hardener) and  
172 the surface of the monolayer with respect to the equilibrium  
173 separation. In this way, the strain  $\epsilon$  can then be defined as  $\epsilon =$   
174  $(l - l_0) / l_0$ , where  $l$  is the displacement of the resin (hardener)  
175 with respect to the distance  $l_0$  calculated in the equilibrium  
176 configuration of the complex. The mechanical properties can  
177 then be calculated from the strain–energy relationship,  $E_s =$   
178  $E(\epsilon) - E(0)$ ; the energy difference between systems under a  
179 given strain  $\epsilon$  and no strain is associated with the equilibrium  
180 configuration.

181 The calculated strain–energy curve is used to obtain the  
182 force vs strain curve, which can be used in the spinodal  
183 equation of state<sup>45</sup> to determine the critical force and critical  
184 strain of a given complex. It is worth mentioning that the  
185 spinodal equation of state, in general, applies to the bulk  
186 material, but its use has been extended to low-dimensional  
187 materials, including graphene and the BN monolayer.

188 It has been shown that the one-dimensional (1D) spinodal  
189 equation of state can reproduce stress dependence on the  
190 strain energy of a given system.<sup>45–47</sup> The equation of state can  
191 be written as

$$\sigma = \sigma_{\text{sp}} \left( 1 - \left( \frac{\epsilon_{\text{sp}} - \epsilon}{\epsilon_{\text{sp}}} \right)^{1/1-\gamma} \right) \quad (1) \quad 192$$

where  $\epsilon$  and  $\epsilon_{\text{sp}}$  represent the strain at a particular point and  
the spinodal strain, respectively.  $\gamma$  is a pseudocritical exponent  
that varies with the direction of (stretching or compressing)  
strain. Equation 1 can be written in terms of the force by  
multiplying the stress terms with the effective area as follows

$$f = f_{\text{sp}} \left( 1 - \left( \frac{\epsilon_{\text{sp}} - \epsilon}{\epsilon_{\text{sp}}} \right)^{1/1-\gamma} \right) \quad (2) \quad 198$$

An interesting feature of the proposed force–strain equation  
of state is that it can also be expressed analytically in its energy  
form. Considering the isotherm at 0 K, the force is related to  
the internal energy  $E$  and the equilibrium length  $L$  employing  
the relationship of  $f = \frac{1}{L} \frac{dE}{d\epsilon}$ . Here,  $f_{\text{sp}}$  accounts for the  
maximum force at which the system breaks and therefore  
represents the elastic limit of the material. It is referred to as  
the critical force. The value of the strain corresponding to the  
critical force is called the critical strain. In the following  
discussion, we designate the critical strength to represent (out-  
of-plane) the transverse strength and the critical strain to be  
(out-of-plane) the separation point at which the monomer  
breaks from the monolayer.  $E$  can be understood as the energy  
needed for the out-of-plane pull-apart (or separation) of the  
resin (hardener) from the surface and, therefore, to overcome  
the interatomic forces binding the complex. 194

## 3. RESULTS AND DISCUSSION

**3.1. Interaction Energy.** Initial DFT calculations were  
performed to determine the equilibrium configurations of resin  
(DGEBA and BMPM) and hardener (DETDA and DABPA)  
molecules. Figure S2 displays the structural configurations of  
these molecules, and Table S1 lists the calculated C–C and B–  
N bond lengths ( $\sim 1.42$  Å), which were in excellent agreement  
with previous reports.<sup>38,48,49</sup> 221

In calculations of the energy surface describing the  
interaction of a resin (hardener) with the monolayer, we  
allowed it to approach the surface in the direction  
perpendicular to the surface with a specific orientation while  
keeping the monolayer fixed. For example, DGEBA is oriented  
in such a way that (i) both end groups and hydrogen ends are  
oriented toward the surface—the in-plane orientation (Figure  
1b(i)), (ii) both the epoxide end groups are facing the surface,  
and the hydrogen end is away from the surface—the flip-in  
orientation (Figure 1b(ii)), (iii) both the end epoxide groups  
are aligned away from the surface, and the hydrogen end is  
close to the surface—the flip-up orientation (Figure 1b(iii)),  
and (iv) only one end group is facing the surface—the vertical  
orientation (Figure 1b(iv)). At the minimum energy distance  
associated with a specific orientation, full optimization of the  
conjugated system in which all atoms were free to relax was  
performed. 238

The characteristics of the complexes are determined in terms  
of the interaction energy, the area of contact, the population of  
atoms, Bader’s charge,<sup>50</sup> critical force, and critical strain. We  
define the interaction energy ( $\Delta E$ ) as  $E(\text{complex}) - E(\text{resin}$   
(hardener))  $- E(\text{monolayer})$ , and a negative value of  $\Delta E$   
suggests the stability of the complex.  $\Delta E$  can also be 244



245 considered as the adsorption energy of a resin (hardener) on  
 246 the monolayer. The contact area is the area of the resin  
 247 (hardener) projected on the surface of the monolayer. The  
 248 population of atoms is defined as the number of the resin  
 249 (hardener) atoms within the range 3 Å from the surface. Note  
 250 that the interplanar distance of ~3 Å can be taken as the  
 251 characteristic distance of vdW-bound systems including the  
 252 complexes considered.<sup>51</sup>

253 Figure 1c shows the calculated values of the interaction  
 254 energies of DGEBA and BMPM forming a complex with  
 255 graphene. The results show the in-plane orientation to be  
 256 energetically preferred, and it is followed by flip-in, flip-up, and  
 257 vertical orientations. The interaction energy steadily increases  
 258 by ~0.9 eV in going from vertical to in-plane orientations,  
 259 thereby suggesting that graphene prefers the resin to be aligned  
 260 parallel to the surface. Table S2 lists the interaction energy, the  
 261 bond distances at the interface, the area of contact, and the  
 262 population of atoms of the equilibrium configurations of the  
 263 abovementioned cases.

264 Next, we calculate the effective area of contact using the  
 265 estimated length and width of the surface covered by a resin  
 266 (hardener) using its distance of one end to the other in both *x*-  
 267 and *y*-directions. We find that the calculated area for the “in-  
 268 plane” orientation is significantly higher than those of the rest  
 269 of the orientations for both cases (Table S2). This is further  
 270 corroborated by calculations of the population of atoms by  
 271 counting the number of atoms that are within the range of ~3  
 272 Å above the surface. The results show that the in-plane  
 273 population is significantly larger than those of the other three  
 274 orientations, thereby facilitating a larger degree of interaction  
 275 between the resin atoms and graphene at the interface.  
 276 Subsequently, the in-plane orientation leads to the energeti-  
 277 cally preferred configuration for DGEBA and BMPM on  
 278 graphene. We note that our results are in line with the PBE  
 279 (DFT) results on the DGEBA/CNT complex, reporting the  
 280 preference of the longitudinal orientation over the transverse  
 281 orientation of DGEBA on a CNT.<sup>52</sup>

282 Both resins and hardeners consist of aromatic rings and side  
 283 groups containing oxygen or nitrogen atoms. However,  
 284 graphene consists of a honeycomb lattice, in which C atoms  
 285 form in-plane sp<sup>2</sup> hybridized bonds together with out-of-plane  
 286 π-bonds. The interaction of a resin (or hardener) with  
 287 graphene is, therefore, expected to be governed by π–π  
 288 noncovalent interactions with a small contribution from the  
 289 polarizable O and N atoms of the side groups. This is what has  
 290 been affirmed by the analysis of the interface in terms of the  
 291 area of contact and the population of atoms; a large effective  
 292 contact area and population of atoms yield the in-plane  
 293 orientation to be the energetically preferred configuration of a  
 294 resin (hardener) on graphene.

295 Figure S3 displays the (in-plane) equilibrium configurations  
 296 of the complexes, and the calculated values of the  
 297 corresponding interaction energy values are listed in Table 1.  
 298 For the complexes, the calculated results show that the order of  
 299 the interaction strength is DGEBA < BMPM for resins and  
 300 DETDA < DABPA for hardeners. Specifically, the difference  
 301 between the interaction strengths of DGEBA and BMPM is  
 302 noticeable and can be explained in terms of the population of  
 303 atoms, which is significantly larger for DGEBA (Table 1).  
 304 Furthermore, the polarizable O atoms (of DGEBA) induce a  
 305 hybridized state that appears in the valance band region of the  
 306 density of states, though the H (resin)–C (graphene)

**Table 1. Interaction Energy ( $\Delta E$ ), the Population of Atoms, and Bader's Charge ( $Q$ ) Calculated for Resin and Hardener Complexes**

	complex (in-plane)	$\Delta E$ (eV)	population of atoms (%)	$Q_{\text{graphene}}$ (e)
resin	DGEBA/graphene	-1.27	16	0.03
	BMPM/graphene	-1.09	10	0.05
	DGEBA/BN	-1.33	16	0.03
	BMPM/BN	-1.30	15	0.06
hardener	DETDA/graphene	-0.96	20	0.04
	DABPA/graphene	-0.74	11	0.02
	DETDA/BN	-1.24	20	0.02
	DABPA/BN	-0.86	11	0.02

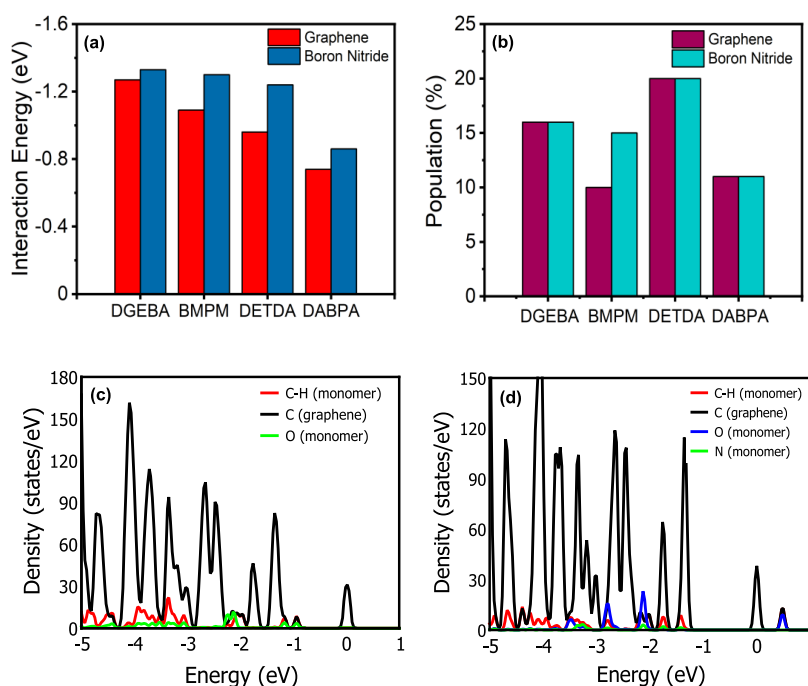
307 hybridized states dominate the valence band in both resin  
 308 complexes (Figure 2c,d).

309 For the case of the BN monolayer, we expect a small but  
 310 noticeable difference in the calculated results as compared to  
 311 those obtained for graphene. This is because the BN  
 312 monolayer being semi-ionic may induce a slightly higher  
 313 degree of electrostatic interaction with a resin (hardener)  
 314 relative to graphene. The calculated values of the interaction  
 315 energy are higher;  $DGEBA_{(\text{graphene})} < DGEBA_{(\text{BN})}$  and  
 316  $BMPM_{(\text{graphene})} < BMPM_{(\text{BN})}$  for the resin complexes and  
 317  $DABPA_{(\text{graphene})} < DABPA_{(\text{BN})}$  and  $DETDA_{(\text{graphene})} <$   
 318  $DETDA_{(\text{BN})}$  for the hardener complexes.

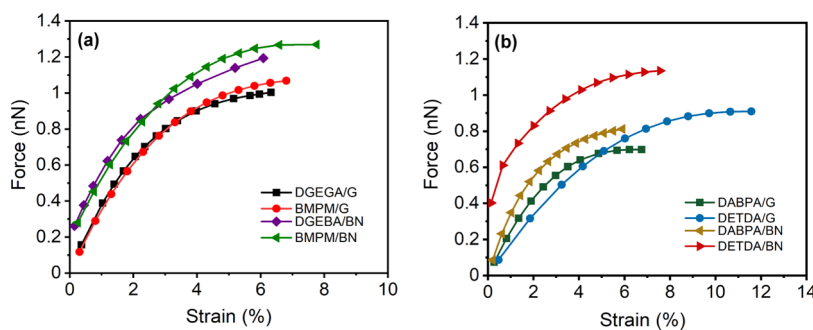
319 Moreover, the results indicate that curing agents (e.g.,  
 320 DETDA) participate effectively at the interface, which implies  
 321 that the load transfer of epoxy/graphene composites is  
 322 governed by both the resin and the hardener in this case.  
 323 The interaction energy values for DETDA and DABPA are in  
 324 line with the expectations arising from their values of the  
 325 population of atoms (Table 1). It is worth mentioning that the  
 326 aromatic ring of DETDA is aligned parallel to graphene and  
 327 thereby yielding a higher degree of the vdW interaction with  
 328 monolayers at the interface.

329 Overall, the interaction between the resin (or hardener) and  
 330 graphene (or BN monolayer) is governed by the dispersive  
 331 force like vdW in the cases considered. This is due to the fact  
 332 that the analysis of the calculated Bader charge suggests the  
 333 occurrence of a small charge transfer (<0.1 e) from graphene  
 334 (BN monolayer) to resins (hardeners) (Table 1). Moreover,  
 335 the hydrogen-bonding interactions with π electrons of  
 336 graphene (or B/N atoms of BN monolayer) at the separation  
 337 of 2.5 Å are expected to be weak.<sup>53</sup>

**3.2. Mechanical Response.** The (out-of-plane) mechan-  
 338 ical response of the complexes was calculated using the setup  
 339 and by applying the load in only the “z”-direction, which is  
 340 perpendicular to the surface starting from its equilibrium  
 341 separation to the separation of ≈3.8 Å with a step-size of 0.02  
 342 Å (Figure S4). DFT calculations were performed at each step  
 343 generating the energy surface of the resin (DGEBA or BMPM)  
 344 and the hardener (DABPA or DETDA) forming complexes  
 345 with graphene (or BN monolayer) (Figure S5). The strain (or  
 346 separation)-energy surfaces were then used to calculate force  
 347 vs strain curves, as shown in Figure 3. Subsequently, the force  
 348 vs strain curve was used in the 1D spinodal equation of state  
 349 (eq 2). We noted that two parameters,  $f_c$  and  $\epsilon_c$ , defined the  
 350 shape of each curve, which was used to characterize the 351



**Figure 2.** (a) Calculated interaction energy of resins (DGEBA and BMPM) and hardeners (DABPA and DETDA) with graphene (red) and the BN monolayer (blue). (b) Calculated population of atoms within the range of 3 Å distance above the monolayer. Atom-projected density of states for (c) resin DGEBA with graphene and (d) resin BMPM with graphene.



**Figure 3.** Calculated force vs transverse strain curves of the (a) resin (DGEBA or BMPM) and (b) hardener (DABPA or DETDA) forming complexes with graphene (or BN monolayer).

transverse strength and the separation point of the conjugated  
monomers considered (Table 2).  $\gamma$  is the 1D correspondence  
of the pseudocritical exponent  $\beta$ , which, in general, takes a  
value of 0.85 associated with the volumetric compression of

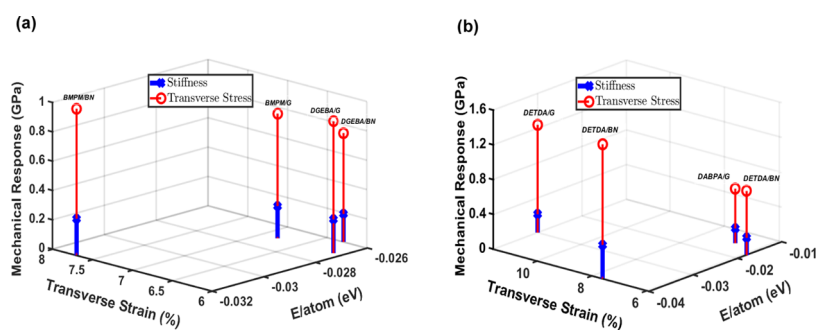
**Table 2.** Calculated Values of the Transverse Strength and (Out-of-Plane) the Separation Point of the Complexes

	complex	transverse strength $f_c$ (nN)	(out-of-plane) separation point $\epsilon_c$ (%)
resin	DGEBA/graphene	1.0	6.3
	BMPM/graphene	1.1	6.8
	DGEBA/BN	1.2	6.1
	BMPM/BN	1.3	7.7
hardener	DETDA/graphene	0.9	11.6
	DABPA/graphene	0.7	6.7
	DETDA/BN	1.1	7.6
	DABPA/BN	0.8	5.9

solids.<sup>54,55</sup> In the case presented,  $\gamma$  varies between 0.5 and 0.8  
(Table S3).

It is worth mentioning that the equation of state (e.g., eq 1),  
in general, is used to investigate the constitutive responses of a  
bulk-like system. In the case presented, we have used the  
spinodal equation of state to differentiate the (out-of-plane)  
mechanical response of quasi-three-dimensional (3D) com-  
plexes consisting of a resin (hardener) and graphene (BN  
monolayer). Therefore, in the following discussion, we use  
“transverse” to describe the out-of-the-plane and designate the  
critical strength to represent the transverse strength and the  
critical strain to be (out-of-plane) the separation point at  
which the monomer apart from the monolayer (Figure S6).

The calculated results show that the resin (hardener)  
forming complexes with the BN monolayer exhibit a slightly  
higher transverse strength than the corresponding complexes  
with graphene. Among resins, BMPM exhibits a slightly higher  
transverse strength relative to that of DGEBA. This is not the  
case with the separation point values for which we find the  
order to be DGEBA/graphene  $\approx$  DGEBA/BN < BMPM/  
graphene < BMPM/BN. Interestingly, the hardener DETDA



**Figure 4.** Interaction energy/atom vs transverse strain and stiffness for the (a) resin (DGEBA or BMPM) and (b) hardener (DABPA or DETDA) forming complexes with graphene (or BN monolayer).

377 exhibits a relatively high value of the separation point  
378 suggesting that, as a curing agent, it is likely to improve the  
379 interfacial load transfer of the epoxy/graphene composite. It is  
380 worth noting that the calculated transverse strength of  
381 DGEBA/graphene is comparable to the calculated value of  
382 DGEBA/CNT; MD calculations reported the value of the  
383 force to be  $\sim 3.8$  nN, which breaks a DGEBA strand from a  
384 CNT,<sup>29</sup> whereas we find the value of  $\sim 1$  nN to break the  
385 DGEBA from graphene (Table 2).

386 In general, the (out-of-plane) stiffness can be taken as a  
387 measure of the quasi-3D Young's modulus suggesting that a  
388 higher value of the stiffness leads to a higher Young's modulus,  
389 which is one of the desired characteristics of an engineered  
390 composite.

391 Table S4 lists the values of the transverse stress and the  
392 stiffness calculated from the stress–strain curve displayed in  
393 Figure S7 for which the area is estimated by projecting the  
394 length and width of the resin (hardener) over graphene (or BN  
395 monolayer). The results show that BMPM/graphene (or  
396 BMPM/BN) is stiffer than the corresponding DGEBA  
397 complexes. Among the hardeners considered, DETDA having  
398 a (graphene-like) planar structure is predicted to have higher  
399 stiffness than DABPA in the complexes considered. Next, we  
400 benchmark our stiffness values to the values calculated for  
401 bilayer graphene employing a similar pull-apart setup. The  
402 elastic stiffness of bilayer graphene is calculated to be 24 GPa,  
403 an order of magnitude higher than what is predicted for the  
404 resin (or hardener) forming complexes with graphene. This is  
405 in line with the expectation of the occurrence of a relatively  
406 high degree of vdW interactions at the interface with a 100%  
407 population of atoms for the case of bilayer graphene.

408 Finally, Figure 4 summarizes the result of the present study  
409 displaying the predicted relationship between the interaction  
410 strength at the interface and the mechanical response in terms  
411 of stiffness obtained at the molecular level for epoxy and BMI  
412 composites. The results show that the mechanical response is  
413 directly related to the degree of the interface adhesion, though  
414 it can also be influenced by the nature of the chemical bonds at  
415 the interface in the polymer composites.

#### 4. SUMMARY

416 We performed an atomistic investigation of the representative  
417 polymer composites employing the density functional theory  
418 to establish the relationship between the nature of the interface  
419 and its mechanical response. Specifically, DGEBA (DETDA)  
420 and BMPM (DABPA) were considered to represent resin  
421 (hardener) components of the epoxy and BMI, respectively.  
422 The calculated results indicated that the interfacial adhesion

was highly influenced by the orientation of the resin 423  
(hardener) on graphene due to van der Waals interactions 424  
being dominated at the interface. Next, we used the strain– 425  
energy relationship to extract force vs strain curves, which were 426  
then used in the 1D spinodal equation of state to determine 427  
the mechanical response of a complex. We found that the 428  
mechanical response in terms of stiffness follows the 429  
hierarchical order of the interaction strength at the interface; 430  
elastic stiffness of BMPM/graphene was higher than that of 431  
DGEBA/graphene. The change in polarity of the surface from 432  
graphene to the BN monolayer improved the interfacial 433  
strength and thereby the elastic stiffness due to the presence of 434  
covalent polar bonds at the interface. Furthermore, the 435  
presence of aromatic rings in the hardener DETDA yielded a 436  
significantly higher mechanical response relative to the one 437  
exhibited by the DABPA hardener suggesting that DETDA, as 438  
a curing agent, was likely to improve the interfacial load 439  
transfer of the epoxy/graphene composite. Overall, the results 440  
predicted that a small degree of polarity at the interface 441  
dominated by van der Waals interactions can help in improving 442  
its mechanical response. In light of the intricate molecular-level 443  
simulations based on first-principles methods, predicting the 444  
interfacial properties of composites is challenging but can 445  
provide an insight to experimentalists in tailoring composites 446  
properties as demanded by aerospace applications. 447

#### ■ ASSOCIATED CONTENT

##### Supporting Information

The Supporting Information is available free of charge at  
<https://pubs.acs.org/doi/10.1021/acsapm.0c01306>.

Epoxide and maleimide groups; structural configurations 452  
and geometrical parameters of resin and hardener 453  
monomers; orientation-dependent properties of com- 454  
plexes; pull-apart force mechanism; mechanical response 455  
of the complexes simulated in a periodic supercell 456  
(PDF) 457

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477 **Notes**

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