

Viability of unidirectional radial turbines for twin-turbine configuration of OWC wave energy converters

Laudino Rodríguez^a, Bruno Pereiras^{b*}, Jesús Fernández-Oro^b and Francisco Castro^c

^a Centro Integrado de F.P. Mantenimiento y Servicios a la Producción de Langreo (C.I.F.P.M.S.P.)
Ciudad Tecnológica e Industrial Valnalón, Hornos Altos S/N, 33930, La Felguera, Spain

laudelinrg@gmail.com

^b Department of Energy, University of Oviedo
Energy Building (EDZE), Campus de Viesques s/n, 33271, Gijón, Spain

* pereirasbruno@uniovi.es; jesusfo@uniovi.es

^c Department of Energetic and Fluidmechanics Engineering. University of Valladolid
Paseo del Cauce 59, 47011, Valladolid, Spain

castro@eii.uva.es

ABSTRACT

Oscillating Water Column devices are the most widespread among Wave Energy converters, with an efficiency that is closely related to the performance of its Power Take-Off element, usually a turbine. Using unidirectional turbines requires a system of valves to rectify the bidirectional flow, so self-rectifying turbines are more convenient for an OWC device. Another recent proposal is the use of a twin turbine configuration, where an arrangement of two unidirectional turbines could perform this task, with each turbine extracting the flow energy alternately. To date, all the twin turbine configurations studied in the open literature consider unidirectional axial turbines. In this paper, the use of a radial turbine to improve the system's efficiency by enhancing flow rectification is presented for the first time. An experimentally validated numerical model has been used to analyse the flow field of the radial turbine when working in both direct and reverse modes. Interesting conclusions are extracted. Finally, a performance comparison of the twin turbine configuration using axial or radial turbines has been carried out. It is concluded that the good performance of the radial turbine working as a flow preventer makes this kind of turbine an interesting option for twin systems.

KEY WORDS: twin turbines, OWC, wave energy, radial turbine

40 NOMENCLATURE

A_R	<i>Characteristic area</i>
$C_H = \Delta P / (\rho \omega^2 D^2)$	<i>Input coefficient</i>
$C_P = T_o \omega / (\rho \omega^3 D^5)$	<i>Power coefficient</i>
D	<i>Mean turbine diameter, $=2 \cdot r_R$</i>
Q, q	<i>Flow rate</i>
Q_{max}	<i>Amplitude of flow rate in unsteady conditions</i>
ΔP	<i>Pressure drop (total-static)</i>
r_R	<i>Blade mid-chord radius</i>
T_o	<i>Output mechanical torque</i>
T	<i>Period</i>
$u_R = \omega r_R$	<i>Blade velocity at r_R</i>
u, v, w	<i>Velocity components (peripheric, absolute and relative)</i>
α, β	<i>Absolute and relative flow angle</i>
$\eta = T_o \omega / \Delta P Q$	<i>Steady efficiency</i>
η_{vol}	<i>Volumetric efficiency</i>
$\bar{\eta}_{input}$	<i>Input mean efficiency</i>
$\bar{\eta}_{tg}$	<i>Mean efficiency of twin turbines set</i>
P	<i>Air density</i>
$\phi = v_R / u_R$	<i>Flow coefficient</i>
Φ	<i>Flow coefficient in unsteady conditions</i>
Ω	<i>Rotational speed</i>
<i>Subscripts/superscripts</i>	
$1, 2$	<i>Turbine 1 or 2</i>
C, D	<i>Inner and outer rotor sections</i>
<i>Direct/reverse</i>	<i>Flow direction</i>
<i>Total</i>	<i>Sum of turbine 1 and turbine 2</i>

41

42 **1. INTRODUCTION**

43 Great efforts are being made within the wave energy field worldwide. Many researchers have the
 44 potential of this kind of renewable energy in their sights, so the presentation of new devices, or
 45 improvements to old ones, often appear in technical literature.

46 One of the most promising wave energy concepts is the so-called Oscillating Water Column (OWC),
 47 see Figure 1 top. It was one of the first solutions to be developed (Falcão, 2010) and it has currently
 48 achieved a significant level of maturity, with several projects even reaching a commercial scale
 49 (Falcão, 2010; Torre-Enciso et al., 2009). This kind of device can be placed on the shoreline, near the
 50 shore and even offshore, although most prototypes are placed onshore because this makes their
 51 installation and maintenance easier. An interesting review about OWC performance from an historical
 52 perspective and a complete list of references can be found in (Falcão and Henriques, 2016),

53 Essentially, OWC power plants are based on a simple working principle: a concrete or steel structure
 54 is semi-submerged in the sea and opened at the bottom, so the water-free surface is displaced as a
 55 piston inside the structure according to the wave period. As a consequence, the air contained in the
 56 top of the structure is compressed/decompressed and pushed outwards/aspirated inwards, generating
 57 a bidirectional air flow which is used to drive a Power Take-Off (PTO). The energy conversion from
 58 wave to pneumatic is made by the structure and the pneumatic energy is then turned into mechanical
 59 energy by means of a PTO element, typically a turbine

60 To take full advantage of the characteristics of the two-way flow generated by the OWC, the PTO
 61 element should have some special features. In the early years, a valve rectification system was used
 62 to drive a unidirectional axial turbine (Maeda et al., 2001; Setoguchi and Takao, 2006). However, the
 63 valve system would lead to maintenance and operational problems. Two alternatives were suggested
 64 to avoid the use of valves:

65 Self-rectifying turbines have been the most popular solution for the PTO element in OWC converters
66 over the last decades. There are several types of these turbines and most of them can be classified in
67 two categories: Wells turbines (Raghunathan, 1995; Wells, 1980) and impulse turbines, which can be
68 radial (Pereiras et al., 2011b; Setoguchi et al., 2002) or axial (Babintsev, 1975; Maeda et al., 1999).
69 Whatever the case, self-rectifying turbines have relatively poor efficiency, except those equipped with
70 adjustable blades/guide-vanes (Curran, R.; Denniss, Tom; Boake, 2000; Falcão and Gato, 2012;
71 Setoguchi and Takao, 2006). Unfortunately, the use of turbines with moving elements would possibly
72 lead to additional problems in the maintenance of these facilities. More information about air turbines
73 for OWC systems can be found in (Falcão and Gato, 2012)

74 a) A twin-turbine system was proposed in (Jayashankar et al., 2009; Mala et al., 2011). This
75 configuration develops the rectification concept with the use of a couple of turbines, instead of
76 control valves, as backflow preventers.

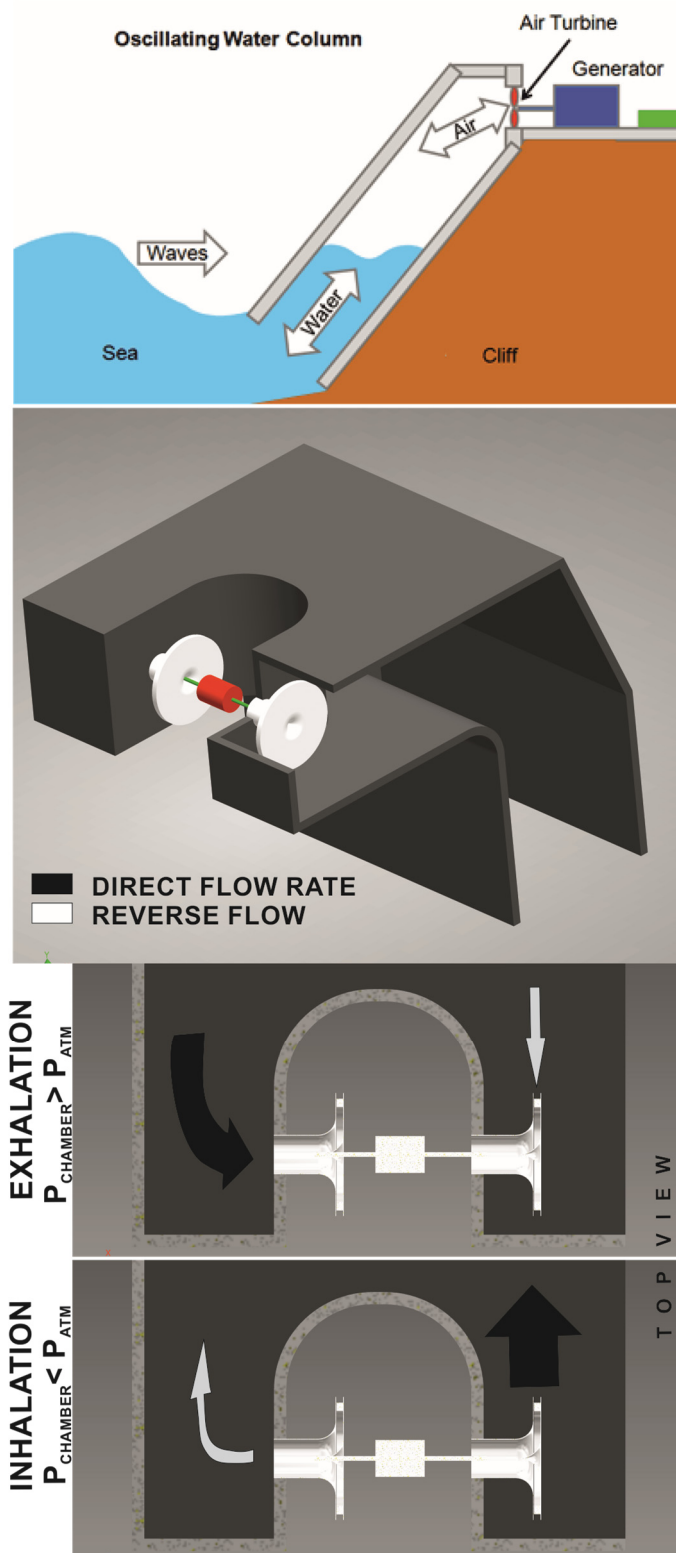
77 Recently, a third possibility has emerged due to its promising results:

78 b) A new concept of turbine equipped with rectifying valve, presented in (Falcão et al., 2015).
79 The original idea using rectifying valves is reconsidered by means of a sliding-valve in
80 combination with a finger-manifold to drive the flow. The preliminary results are encouraging
81 but the performance of this valve has yet to be tested in tough conditions.

82 Evidently, the lack of moving parts and valves in the second option makes this possibility the most
83 attractive in terms of maintenance costs.

84 The twin-turbine system is based on the use of two turbines, one of them working normally (direct
85 mode-outflow) while the other is working as a backflow preventer (reverse mode inflow). A sketch of
86 this system is shown in Figure 1. Basically, the air from the chamber is pushed towards the
87 atmosphere in an exhalation process, so the flow generated passes through the turbines. One of the
88 turbines is working normally, in direct mode (producing energy), whereas the other is working in
89 reverse mode (not producing energy). Once the exhalation process is over, inhalation starts. The air is
90 sucked from the atmosphere to the chamber with the result that the turbines alternate their roles. Note
91 that the flow rate distribution between the turbines, which are working under the same pressure
92 difference (chamber-ambient), is determined by the performance curve of the turbine, which is
93 different for both modes.

94 The twin system permits the use of unidirectional turbines, which are more efficient than self-rectifying
95 ones. In fact, all the proposals found in the open literature are considering axial turbines (Takao and
96 Setoguchi, 2012) although it has been shown (Pereiras et al., 2014) that flow leakage through the
97 turbine working in reverse mode is around 30% of the total flow generated by the OWC. This important
98 loss of energy hinders the total efficiency of the system, due not only to the flow rate through the
99 turbine which is not producing energy, but also to the braking torque exerted on that turbine (Pereiras
100 et al., 2014).



101

102 Figure 1. Top: OWC sketch; Middle: OWC equipped with twin radial turbines; bottom: flow distribution.

103 A fluidic diode is discussed in (Dudhgaonkar et al., 2011) as a possible solution to minimize the
 104 reversed flow increasing flow blockage, although results combining the diode with the twin turbines are
 105 not presented.

106 In the present work, a comparison of the performance of radial turbines with respect to axial turbines
 107 for twin-turbine configurations is presented. Previous studies of self-rectifying turbines (Pereiras et al.,
 108 2011b) reveal that radial turbines show an interesting feature for the twin turbine system: the greater

109 pressure drop generated predicts a significant improvement when operated as backflow preventers,
110 thus providing a minimum energy loss through the turbine working in reverse mode. To the best of the
111 author's knowledge, this is the first time that radial turbines have been proposed for use on twin
112 systems for OWC converters.

113 The performance curve of the radial turbine is required for a comparison to be made with the axial
114 turbine. For this purpose, a centrifugal turbine has been designed and its performance has been
115 assessed by means of a CFD simulation using the commercial code ANSYS Fluent®. The model has
116 been validated, and shows a good degree of congruence with the experimental results obtained in a
117 test campaign. The performance of the turbine working in both direct and reverse modes has been
118 evaluated, with special attention being paid to that obtained in reverse mode, which was key when
119 selecting a centrifugal turbine instead of a centripetal one. Finally, a numerical estimation of the
120 performance of the whole twin system has been carried out.

121 The following sections describe in detail the twin-system concept with radial turbines. First of all, in
122 section two, this brand new design is presented to the readers with sound arguments that justify this
123 particular choice. Next, details of the construction and testing of an experimental model are given.
124 Subsequently, the numerical model is fully described. The results are shown in section three, starting
125 with the CFD model validation by means of the turbine performance curves. Later, a more thorough
126 analysis of the flow pattern is conducted to find the strong and/or weak points of the design chosen.
127 Finally, some conclusions are presented in section four.

128

129 **2. EXPERIMENTAL TESTS AND NUMERICAL MODEL**

130 In this section the authors describe the main points related to the experimental tests carried out and
131 the characteristics of the numerical model used in the CFD simulations.

132 The turbine for the study has been designed as a centrifugal (direct mode) rather than centripetal
133 (reverse mode) rotor, in order to reinforce its performance as a backflow preventer. Previous studies
134 of radial turbines for OWC (Pereiras et al., 2011a, 2011b) reveal that, even in a turbine equipped with
135 guide vanes, a strong swirling appears in the elbow during centripetal performance when performing
136 off of the best efficiency. It should be noted that, unlike traditional centripetal turbines, the flow rate
137 across OWC turbines is highly variable, with a very large operational range and, as a consequence,
138 the flow angle at the rotor outlet is also continuously changing over time between a wide range of
139 values. This inherent characteristic in the performance of OWC turbines led the authors to consider
140 the use of a radial turbine as a perfect candidate in twin turbine configurations, taking advantage of
141 this feature to optimize the reverse mode.

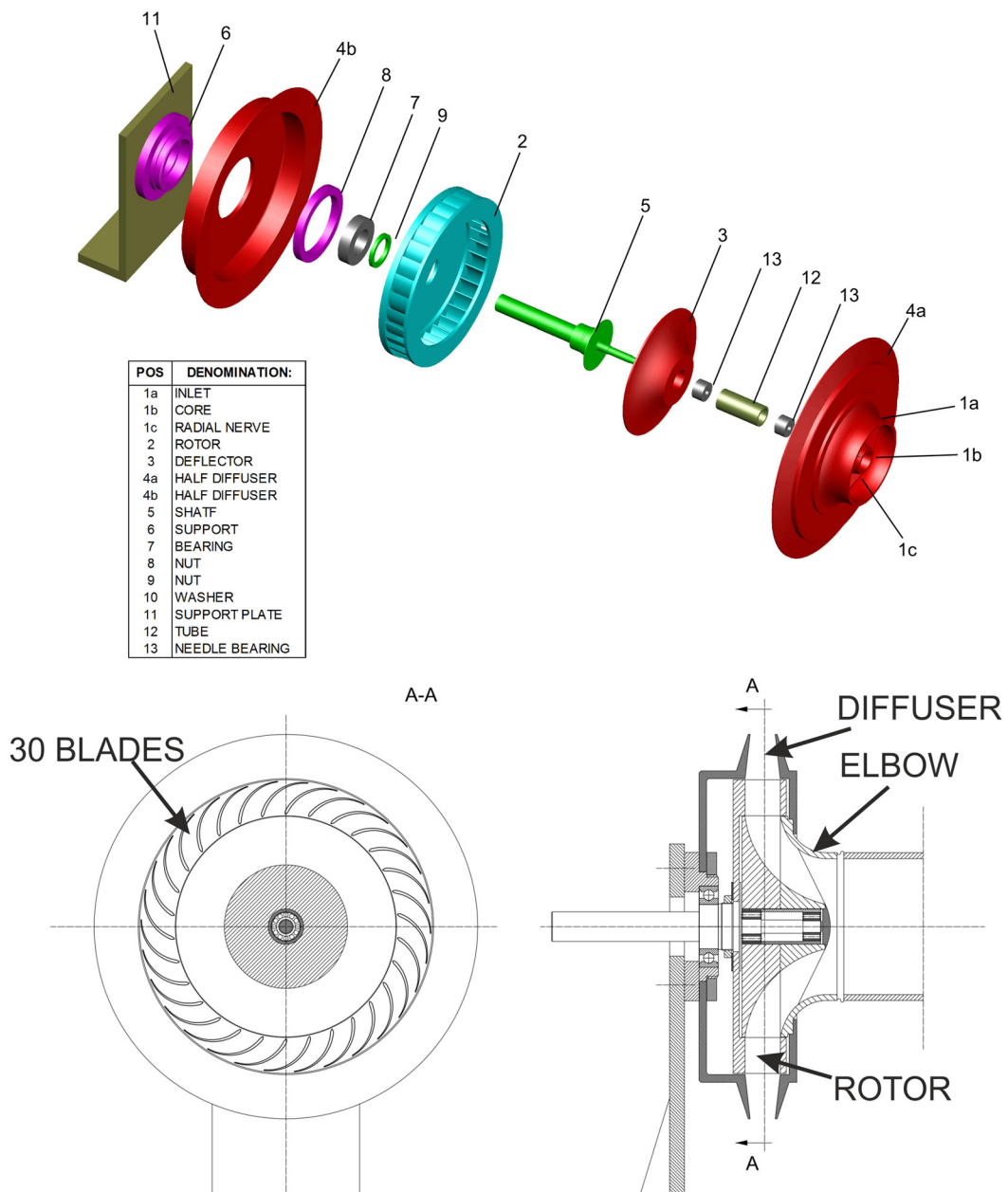
142 In line with the idea of reinforcing the reverse mode, and in spite of reducing the efficiency in direct
143 mode, the turbine is composed of a single blade row, so there are no guide vanes upstream or
144 downstream of the rotor. The inner guide vanes have been suppressed in order to maximize the swirl
145 generated in centripetal performance (reverse mode). On the other hand, their suppression generates
146 a large incidence loss at the rotor inlet during centrifugal performance (direct mode), which is
147 minimized by adjusting the inner angle of the blade. Including outer guide vanes downstream of the
148 rotor in centrifugal performance to work as a diffuser would increase maximum efficiency in direct
149 mode. However, it is also known that, off of the best efficiency point, outer fixed guide vanes are an
150 important source of incidence loss in centrifugal performance (Pereiras et al., 2011b). Moreover, the
151 presence of outer guide vanes would facilitate the flow to enter the rotor centripetally (reverse mode),
152 which it is completely undesirable if the flow blockage is to be strengthened. As a result, outer guide
153 vanes were not included in the design.

154 In the absence of guide vanes, blade design was conducted by means of one-dimensional theory for
155 turbomachines (Dixon and Hall, 2005). Several blade profiles were analyzed by 2-D simulations with
156 the ANSYS Fluent® code. Finally, a 3-D numerical model of the turbine was developed with the
157 selected blade profile. It is appropriate to underline that the design is focused on strengthening
158 blockage in reverse mode, even if that means a reduction of efficiency in direct mode, because this
159 can make the difference with respect to axial turbines for twin systems.

160

161 **2.1. Experimental tests**

162 A full 3-D turbine prototype was built, according to the scheme shown in Figure 2, in a 3-D printer: BQ
 163 Witbox, with a maximum capacity of 297x210x200 mm³ and maximum resolution of 50 μm. The rotor
 164 (Figure 2, top), made of Acrylonitrile Butadiene Styrene (ABS), is shrouded by a ring glued at the tip of
 165 the blades in order to reduce the tip flow effect. The connection of the rotor to the two-piece axial tube
 166 and the outer diffuser of the turbine was also made in the 3-D printer using Polylactic Acid (PLA)
 167 instead. All the components are supported by a central axis (Figure 2, bottom), made of aluminum in a
 168 CNC machine. The use of PLA for printing complex pieces in such experimental facilities is highly
 169 recommended due to its high degree of finish and ruggedness. Alternatively, ABS can also be used to
 170 print out, but it is strongly recommended to use a 3-D printer with a heated plate.



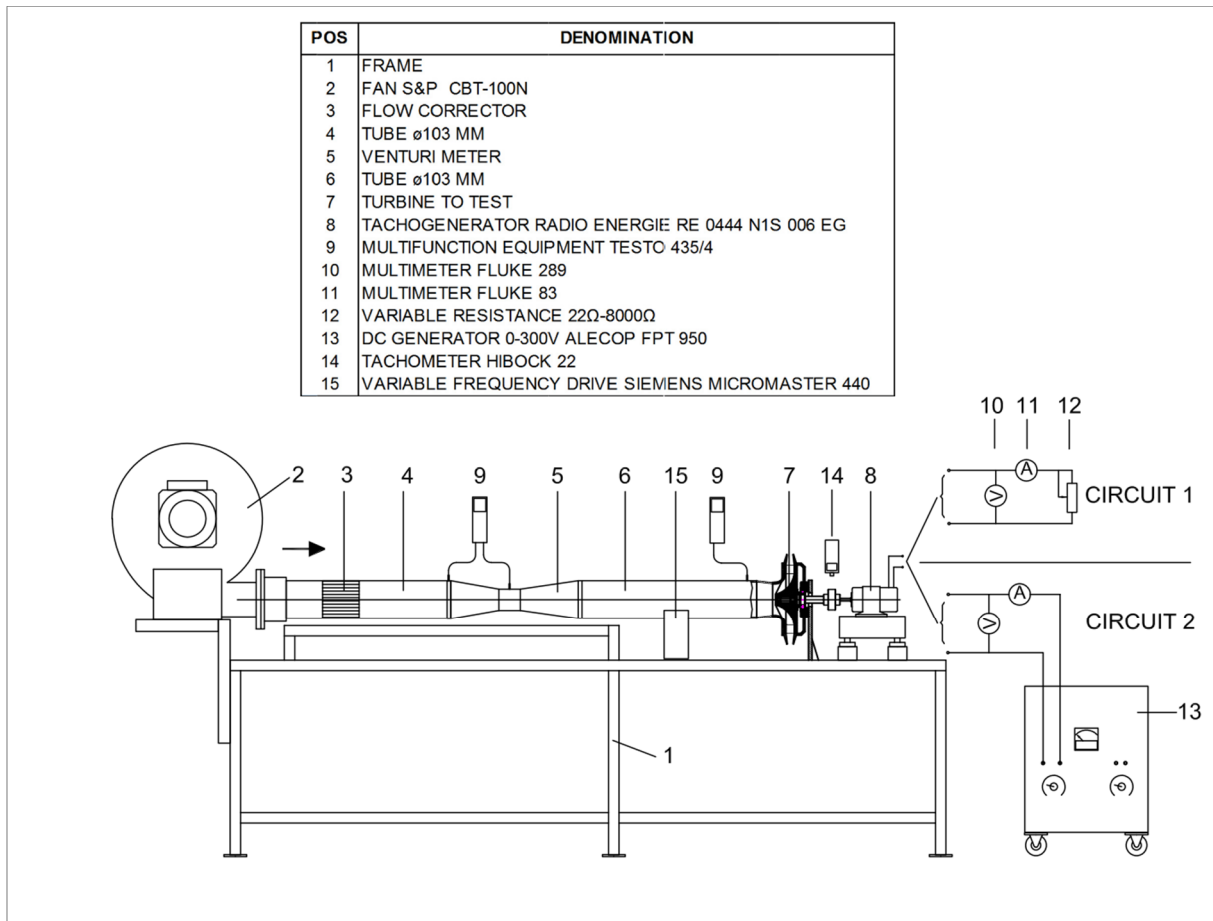
171

172

Figure 2. Turbine model

173 The inner and outer diameters of the radial turbine are 150 and 258.4 mm respectively, with a 24.4
 174 mm span for the blades. The turbine is composed of 30 blades, with inner and outer blade angles of
 175 135 and 175 degrees with respect to tangential direction (i.e. a deflection of 40 deg).

176 The turbine is mounted in a test rig, as is shown in Figure 3. Flow is generated by a centrifugal fan of
 177 0.75 kW (Soler&Palau CBT-100N). Flow rate was measured with a Venturi-meter with pressure taps
 178 connected to a differential manometer.



179

180

Figure 3. Experimental rig

181 Information regarding the measuring equipment is shown in Table 1.

182

Table 1. Information on the instruments used in the experimental tests.

ACCURACY OF MEASUREMENT EQUIPMENT		
Magnitude	Measurement equipment	Minimum accuracy
Barometric pressure	Station DAVIS VANTAGE VUE 6351	± 1 hPa
Room temperature	Testo 435/4	$\pm 0,3$ $^{\circ}$ C
Relative humidity	Testo 435/4	± 2 %
Static pressure inlet turbine	Testo 435/4	± 2 Pa
Differential pressure in Venturi tube	Testo 435/4	± 2 Pa
Angular velocity	Tachometer Hibok 22	$\pm 0,15$ rpm
Voltage DC	Multimeter Fluke 83	$\pm(0,1\%+0,1)$ V
Intensity DC	Multimeter Fluke 289	$\pm(0,15\%+0,02)$ mA
Resistance DC	Multimeter Fluke 83	$\pm(0,4\%+0,1)$ Ω
Tachogenerator terminal voltage	Tachogenerator RE 0444 N1S 006 EG	± 1 %

183

184 Turbine input power is determined by the flow rate measured through the venturi tube and the
185 pressure difference between the turbine inlet and the atmosphere.

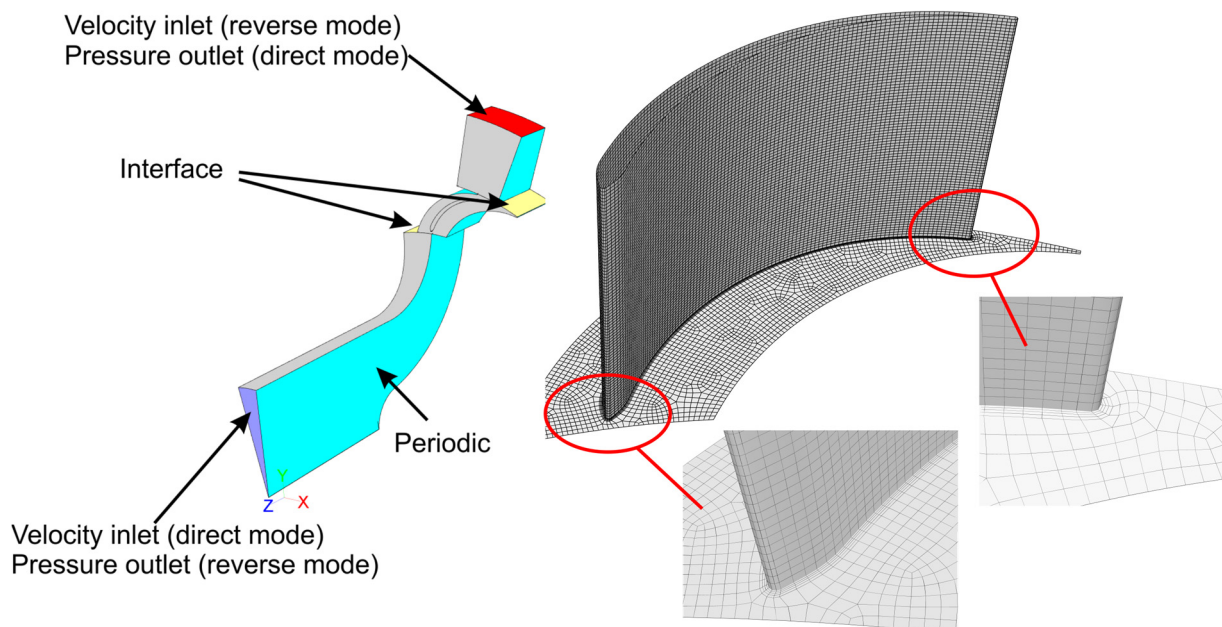
186 Assessment of output power was performed by a tachogenerator (Precilec Radio Energie - RE 0444
187 N1S 006 EG), as follows:

- 188 - First of all, electrical loss was assessed according to the data given by the manufacturer,
189 applying the classical theory of electric machines. Next, in order to find a correlation between
190 input power and rotation speed, the tachogenerator was tested alone in motor mode at
191 different constant speeds and unloaded. By discounting previously assessed electrical loss
192 from the measured input power, the mechanical loss of the tachogenerator is found.
- 193 - The second step was to assess turbine mechanical loss. Therefore, the turbine was coupled
194 to the tachogenerator to carry out tests at different constant speeds with the tachogenerator
195 running in motor mode. Both total electrical and mechanical tachogenerator loss was
196 discounted from electrical input power, by which mechanical turbine loss was obtained. From
197 these tests a correlation was established between turbine mechanical loss and rotation speed.
- 198 - Final tests were carried out to determine turbine output power. The turbine, decoupled from
199 the generator, was installed in the experimental rig, where the fan, conducted by a variable
200 frequency drive, can supply different flow rates. The unloaded turbine is allowed to rotate
201 freely until reaching steady rotation speed, the value of which depends on the flow rate. Since
202 the rotation speed is constant, the torque exerted by the flow is equal to turbine mechanical
203 loss, which can be assessed by the relation between loss and rotation speed from the
204 previous tests.

205

206 2.2. Numerical model

207 Flow simulation is solved with FLUENT v12®, which employs the finite volume numerical method
208 (FVM) to solve the Navier-Stokes equations by using a segregated solver. In order to reduce
209 computational costs, simulations were carried out in a periodic domain (Figure 4). The mesh consists
210 of $2 \cdot 10^6$ hexaedrical cells, with special refinements towards the blade surfaces, and was built in
211 GAMBIT® 2.4.



212

213 Figure 4. Left: Numerical geometry and boundary conditions. Right: Mesh details

214 Density was assumed to be constant (1.2 kg/m^3). Once the simulations were over, it was checked that
215 Mach number was below 0.3 in the whole domain.

216 Since the computational geometry includes rotating domains ($\omega = 500$ rpm), the sliding mesh
 217 technique (SMM) was used to control the relative motion of the rotor in a purely unsteady fashion.
 218 Therefore, two interfaces were placed upstream and downstream of the rotor (Figure 4). Although
 219 SMM was not needed due to the lack of guide vanes, it was in fact used because the model was
 220 simulated in batch with other geometries which had guide vanes included.

221 The realizable $k-\varepsilon$ turbulence model, already validated in previous works (Pereiras et al., 2011a;
 222 Thakker and Dhanasekaran, 2005), was used for the turbulent closure of the numerical model. In
 223 addition, a Non-equilibrium Wall Function approach was adopted, so special care was employed in the
 224 walls to obtain y^+ values in the corrected range. The time-dependent term is approximated with a
 225 second-order implicit scheme. The pressure-velocity coupling was recreated through the SIMPLE
 226 algorithm. The high order Monotone Upwind Scheme for Conservation Laws (MUSCL) was used for
 227 convection term discretization and the classical central difference approximation for diffusion terms.

228 The time step was set to 10^{-4} s, resulting in 40 time steps per blade passing period. The residuals
 229 were set to 10^{-5} and convergence was achieved after approximately 20 iterations per time step for all
 230 the resolved equations. Six full-annulus rotations of the periodical domain were simulated to reach
 231 global convergence, with approximately 4 hours of CPU time per flow rate. The simulations were
 232 made in a cluster of 4 units with the following characteristics: intel i5 2.67GHz, 2x2 GB RAM.

233 The simulations were performed on the assumption that the turbine rotated unsteadily but under
 234 quasi-steady flow conditions. This assumption is perfectly justified on account of the reduced
 235 frequency of the turbine (the ratio between the blade passing period and the period of the wave cycle)
 236 which turns out to be 10^3 . Therefore, the boundary conditions (flow rate and rotational speed) remain
 237 constant in each simulation, although the numerical model is resolved unsteadily since the relative
 238 position of the rotor varies with time. The performance of the turbine for other through-flow conditions
 239 is obtained by adjusting the flow rate, with the modification of the inlet boundary condition.

240

241 3. RESULTS AND DISCUSSION

242 3.1. Validation and general performance

243 The usual non-dimensional coefficients are represented below to show the performance of the radial
 244 turbine. Specifically, the power and input coefficients, C_P and C_H , as well as the flow coefficient ϕ ,
 245 together with aerodynamic efficiency, are defined as:

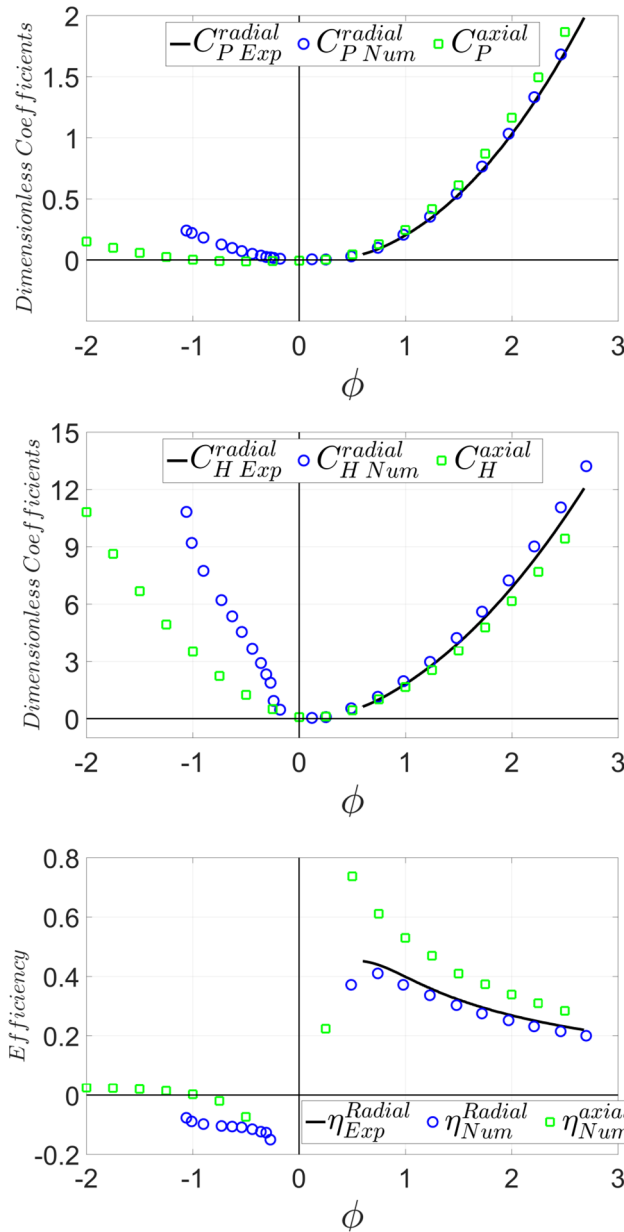
$$C_P = \frac{T_o \omega}{\rho \omega^3 D^5}, C_H = \frac{\Delta P}{\rho \omega^2 D^2}, \phi = \frac{Q/A_R}{u_R}, \eta = \frac{T_o \omega}{\Delta P Q}. \quad (1)$$

246 Here, ρ is the air density, T_o the mechanical torque, ΔP the total to static pressure difference, Q the
 247 flow rate, r_R the blade mid-chord radius, $D=2 \cdot r_R$, A_R the cross-flow area at r_R and u_R is the blade speed
 248 at r_R . Efficiency, which is the ratio of shaft power output to pneumatic power input, can be expressed in
 249 terms of the coefficients mentioned above.

250 Taking into account the data from Table 1, and following the classical formulation for uncertainty
 251 analysis, combined maximum uncertainty is 18% for the input coefficient, 5% for the flow coefficient
 252 and 8% for the power coefficient. These values are attained for maximum flow rates but are reduced
 253 to 2% in the case of low flow rates.

254 The performance of the turbine under steady flow conditions and for different flow coefficients is
 255 shown in Figure 5. Positive flow coefficients correspond to direct mode, while negative values occur
 256 for the turbine working in reverse mode. The results of the numerical model in direct mode ($\phi > 0$) are
 257 compared with the experimental tests made to validate the model. In addition, results for an axial
 258 turbine (Pereiras et al., 2014) have also been included for comparison. The numerical power
 259 coefficient matches perfectly with the experimental results for the whole range of positive flow
 260 coefficients. Also, the development of the input coefficient is accurate, with a discrepancy lower than
 261 10% for the highest flow rates only. Note that this difference is below the maximum experimental
 262 uncertainty previously mentioned. Finally, numerical efficiency confirms the excellent agreement with

263 the results in the lab tests, validating the numerical model and allowing an in-depth analysis of the
 264 CFD flow patterns.



265

266

Figure 5. Performance curves of the turbine

267 Figure 5 (bottom plot) also reveals the main drawback of the radial turbine for this application: its lower
 268 efficiency with respect to the axial turbine. In effect, previous studies of axial turbines for OWC report
 269 twin systems achieving stationary efficiencies of up to 20% higher (Pereiras et al., 2014; Takao and
 270 Setoguchi, 2012). However, the radial turbine would become competitive due to the extreme
 271 difference in the input coefficient between direct and reverse modes. The axial turbine (Figure 5 - top
 272 plot) exhibits a quite symmetrical distribution of the C_H for both positive and negative flow coefficients,
 273 whereas the radial turbine is more likely to impede the reverse flow because of its higher slope in the
 274 C_H for negative flow rates. This will be translated into a marginal loss of kinetic energy through the
 275 radial turbine, much lower than in the case of the axial turbine, with the result that the radial turbine will
 276 perform better as a backflow preventer than the latter (more information on this is provided below).

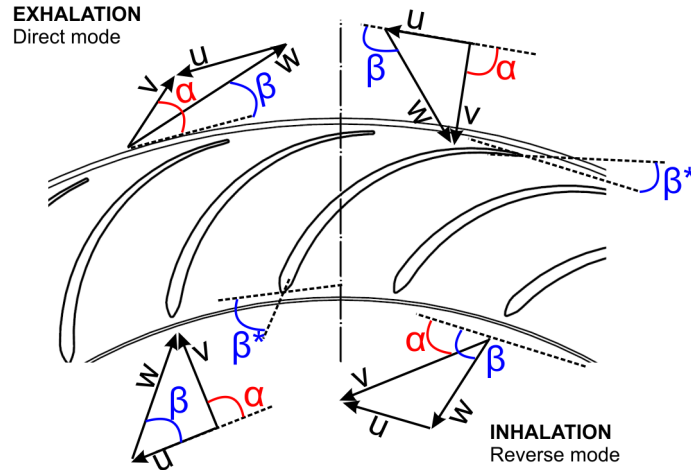
277 In addition, it must be appreciated that the braking torque for the reverse mode of the turbine is
 278 undesirable, and this negative torque is greater in the radial turbine. However, because of the superior

279 performance of the radial turbine as a backflow preventer, both flow rate and torque will be much
 280 smaller than those produced in the axial turbine.

281

282 **3.2. Flow pattern**

283 In this section, the flow patterns in the radial turbine are analysed in terms of pressure loss and
 284 change of momentum (flow angles) in the rotor. The reference angles and velocity relationships are
 285 shown in Figure 6 for both direct (centrifugal) and reverse (centripetal) modes.

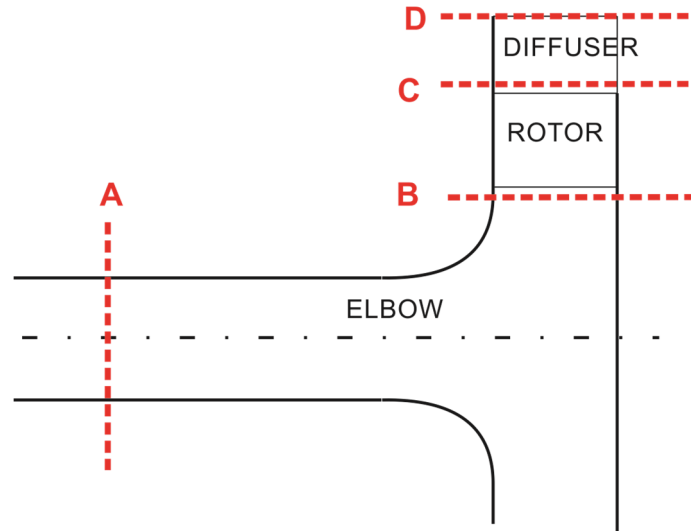


286

287 Figure 6. Reference angles and velocity relationships for both direct and reverse modes.

288 where α and β represent the angles of absolute and relative flow velocities with respect to the
 289 tangential coordinate, and β^* is the geometrical blade angle.

290 To complete the analysis of system losses, the turbine geometry has been divided into three different
 291 parts: elbow, rotor and diffuser, Figure 7. Kinetic energy has also been taken into account because of
 292 its importance, as is clearly shown in forthcoming figures.



293

294 Figure 7. Turbine partition for loss analysis.

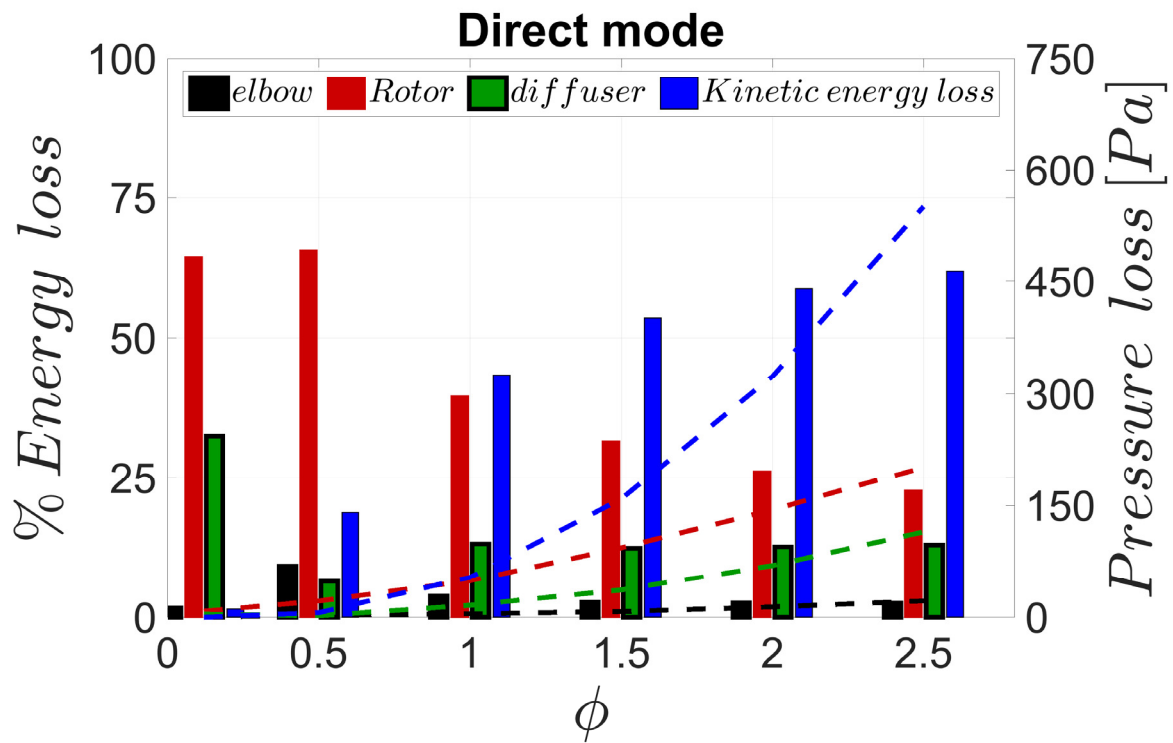
295 Note that energy loss is calculated as the total-to-total pressure difference in terms of every element,
 296 taking as references the divisions shown in Figure 7. Hence, dynamic pressure at the outlet (A in
 297 reverse mode, and D in direct mode) is considered as kinetic energy loss.

298 The loss distribution among the different elements of the turbine are shown in Figure 8 for direct
 299 mode. Here, the contributions of the elbow, rotor, external diffuser (as identified in Figure 2) and

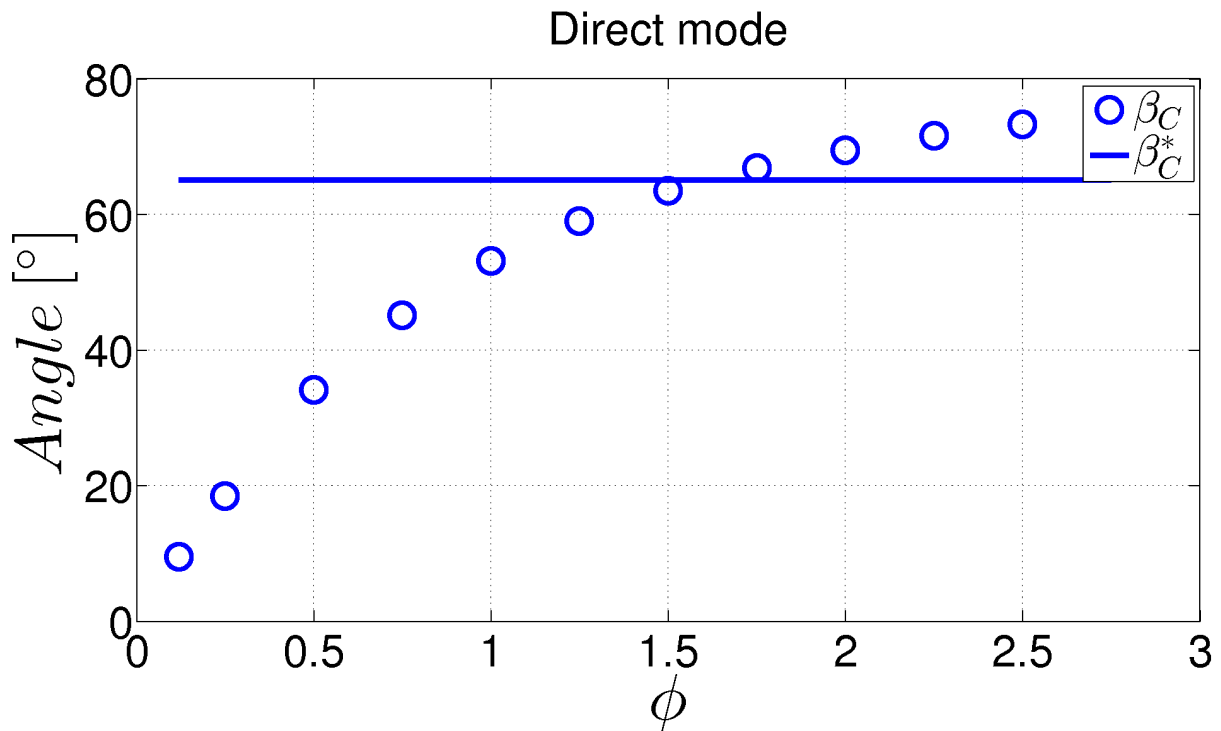
300 kinetic energy loss at the outlet are addressed separately. It is clear that the rotor accounts for the
 301 greater part of the loss for low-flow coefficients, which is mainly the result of the incidence of the flow.
 302 The difference between the flow and blade angles at the inlet is shown in Figure 9, revealing large
 303 incidence losses at the blade leading edge, which leads to a critical drop in efficiency when $\phi < 1$. Also,
 304 it can be observed that the entire turbine has its top efficiency point around $\phi = 0.7$, which does not
 305 exactly correspond to the maximum point of efficiency of the rotor (though not shown here, it is found
 306 to be around $\phi = 1$). This fact reveals that the diffuser has a critical role in the machine's efficiency,
 307 especially at large flow coefficients. In addition, Figure 8 illustrates how kinetic energy loss at the
 308 outlet increases sharply with the flow rate, following a typical parabolic development.

309 The rise in kinetic energy loss at the outlet is related not only to the flow rate, but is also conditioned
 310 by the high values of tangential velocity at the rotor outlet. Figure 10 indicates that the absolute flow
 311 angle is abruptly reduced for flow coefficients higher than 0.3, which leads to a strong tangential
 312 component and extremely high values of kinetic energies at the outlet. Consequently, this residual
 313 kinetic energy is the main source of loss at a high flow coefficient, and is even more important than
 314 incidence losses at the rotor (they are reduced for large flow coefficients - Figure 9). Furthermore, the
 315 contribution of loss in the diffuser is only important for flow rates below $\phi = 0.5$ (its relative significance
 316 being practically constant for the whole range of large flow rates), while losses at the elbow are
 317 practically negligible.

318 In summary, kinetic energy at the outlet is a critical factor that penalizes the efficiency of the radial
 319 turbine in direct mode. Future designs of radial turbines for OWC converters must take particular care
 320 with this residual energy to increase efficiencies.

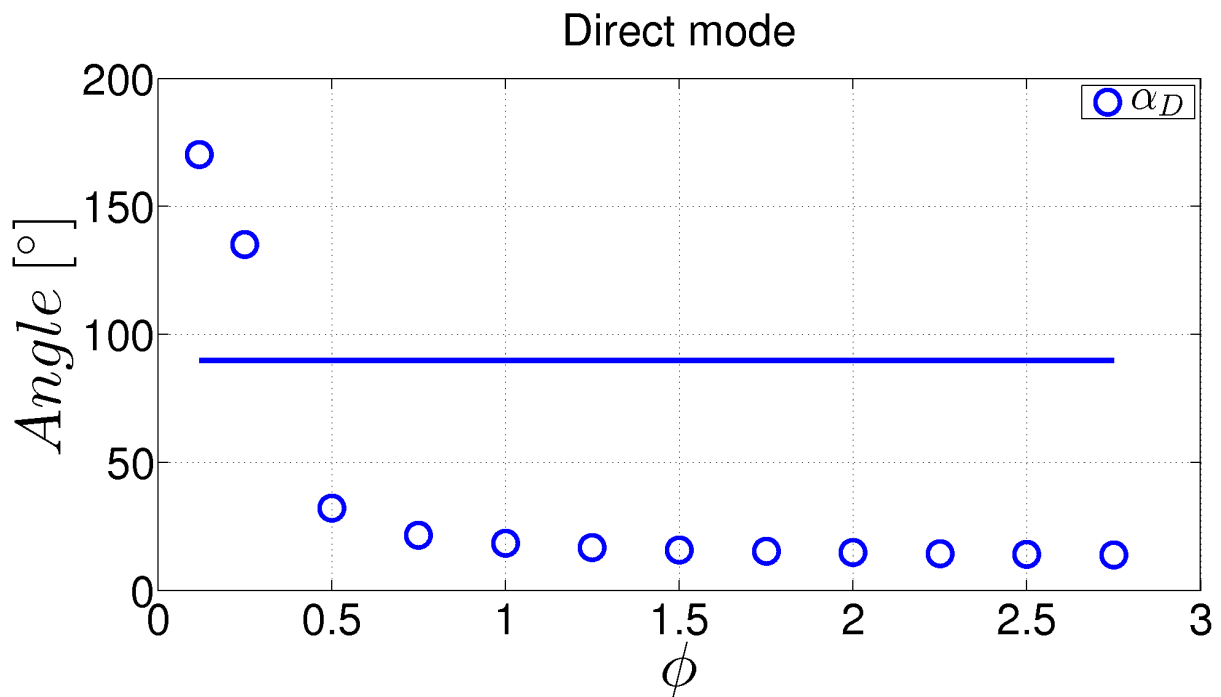


321
 322 Figure 8. Loss distribution in direct mode. Left axis: Bars, percentage value; Right axis: lines, absolute
 323 value.
 324



325
326
327

Figure 9. Relative flow angle at the rotor inlet in direct mode.



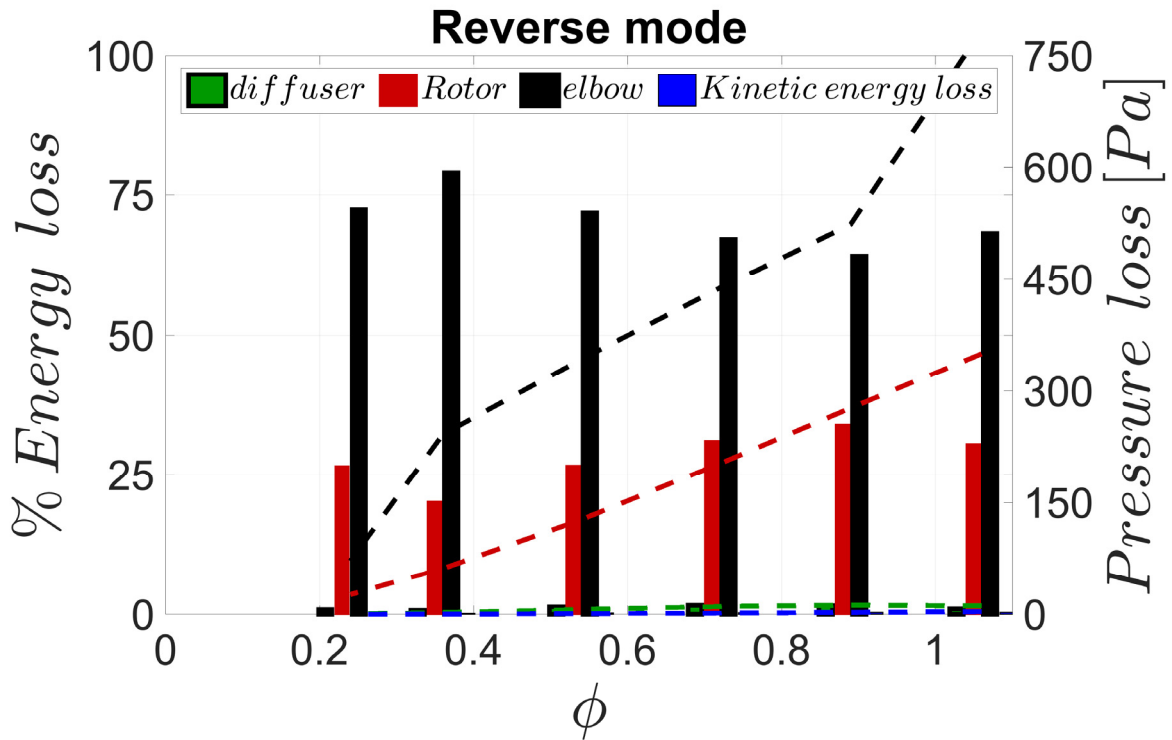
328
329
330

Figure 10. Absolute flow angle at the rotor outlet in direct mode.

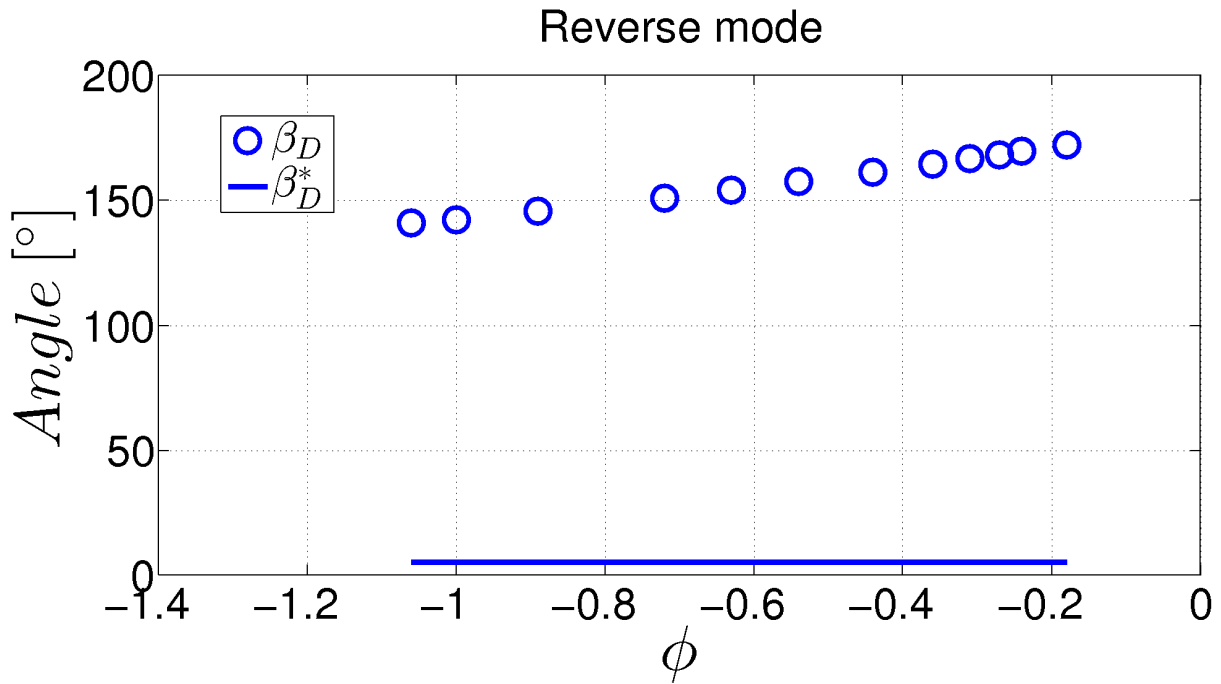
331 Loss distribution is shown for reverse mode in Figure 11. In this case, air flows through the turbine in
332 the centripetal direction, emanating from the diffuser and passing through the rotor and elbow to
333 discharge into the inner duct.

334 Figure 11 is probably the most important figure in this study, because it shows why this kind of turbine
335 might deserve further analysis. Unlike axial turbines for twin systems, where losses are mainly

336 concentrated in the rotor due to the large incidence flow angles (Pereiras et al., 2014), the main
 337 source of loss in the radial version is the elbow. The rotor also displays significant losses
 338 (approximately 25% for all the flow rates in Figure 11), on account of the large incidence angle at the
 339 inlet in reverse mode (Figure 12). However, as the flow leaves the rotor with a large tangential velocity
 340 (see Figure 13), a strong swirling effect takes place and a large amount of loss is generated at the
 341 elbow. The large flow blockage caused by the elbow in this centripetal mode demonstrates the
 342 appropriateness of employing a radial turbine with a centrifugal direct mode, instead of a traditional
 343 centripetal Francis turbine. Moreover, as a result of the large outlet section, both energy losses at the
 344 outlet are negligible. Similarly, losses at the diffuser are negligible because, in reverse mode, the
 345 incoming flow direction is centripetal.

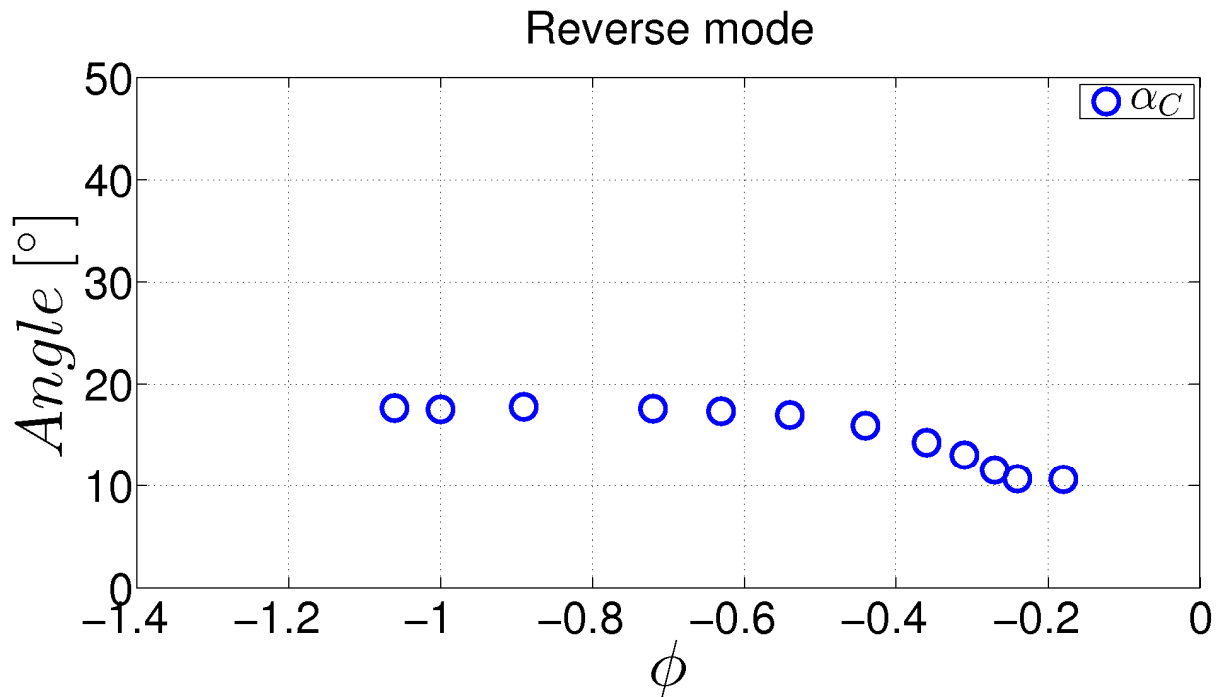


346
 347 Figure 11. Loss distribution in reverse mode. Left axis: Bars, percentage value; Right axis: lines,
 348 absolute value.
 349



350
351
352

Figure 12. Relative flow angle at the rotor inlet in reverse mode



353
354
355

Figure 13. Absolute flow angle at the rotor outlet in reverse mode

3.3. Non-steady performance

357
358
359
360
361

Once the analysis of the flow pattern inside the turbine has been completed, it is necessary to evaluate the performance of the whole system in non-stationary conditions. This is achieved by coupling overall turbine performance (the curves shown in Figure 5) with the behaviour of the OWC converter. For this purpose, it has been assumed that the flow rate generated by the OWC device is a sinusoidal function of time (Pereiras et al., 2014; Takao et al., 2011), according to which:

362
$$Q_{total} = Q_{max} \sin(2 \pi t / T) \tag{2}$$

363
$$\omega = \omega_1 = \omega_2 \tag{3}$$

364
$$Q_{total} = q_{direct} + q_{reverse} \tag{4}$$

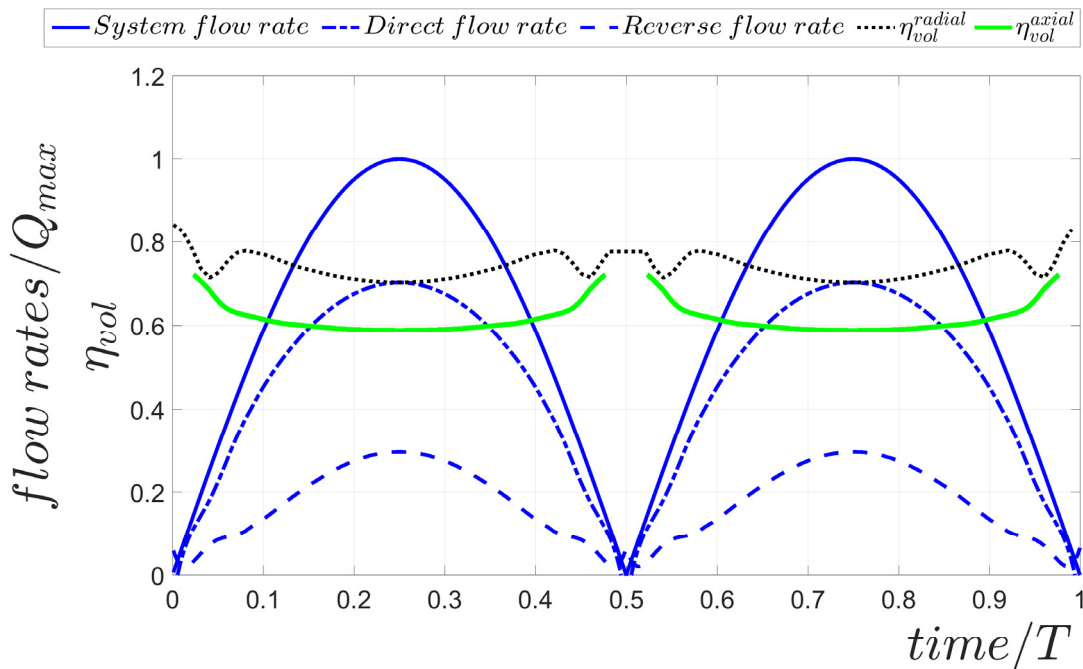
365
$$\Delta P = \Delta P_1 = \Delta P_2 \tag{5}$$

366
$$\Phi = (Q_{max}/A_R)/u_R \tag{6}$$

367 Here Q_{total} , Q_{max} , t and T represent the total flow rate throughout the whole system, the amplitude of
 368 the Q_{total} , time and the period of the OWC motion; q is the flow rate through a turbine and subscripts
 369 *direct* and *reverse* denote the performance mode of the turbine; ω and ΔP are the rotation velocity and
 370 drop in pressure, both being equal for the two turbines of the twin turbines system. Φ represents the
 371 dimension-less form of the flow coefficient amplitude for the whole system (including both direct and
 372 reverse flows).

373 Note that this non-steady analysis is made using a total-to-static pressure drop between the inlet and
 374 outlet sections of the turbine ($P_{total}^{in} - P_{static}^{out}$), rather than the total pressure differences the authors
 375 used in previous studies (Pereiras et al., 2014). Therefore, kinetic energy losses at the outlet are taken
 376 into account.

377 The performance of OWC turbines is commonly considered quasi-steady when working on an OWC
 378 converter (Inoue et al., 1988; Setoguchi and Takao, 2006; Takao et al., 2011). This reasonable
 379 assumption permits a non-steady comparison between turbines based on steady performance data.
 380



381
 382 Figure 14. Flow rate distribution under sinusoidal total flow rate ($\Phi = 1.5$).
 383

384 After the previous resolution of the equation system (2) to (5) using the performance curve of the
 385 radial turbines, it is possible to represent the periodic behavior of the flow rate, as well as other
 386 variables of interest. In Figure 14, both sinusoidal distributions of the instantaneous flow rate for both
 387 turbines in direct and reverse modes are compared with the total flow rate in the chamber. The flow

388 rates are made non-dimensional with the maximum flow rate in the OWC system, Q_{max} , and the time is
 389 divided by the wave period. In addition, volumetric efficiency, defined as $\eta_{vol} = q_{direct} / Q_{total}$, is plotted for
 390 both axial and radial turbines.

391 Since the η_{vol}^{radial} is over 70%, less than 30% of the flow generated by the OWC escapes through the
 392 turbine working in reverse mode; this is lower than the flow leakage produced in a twin turbine
 393 equipped with axial turbines, which reaches values up to 42%. It is important to underline, as was
 394 mentioned before, that this leakage is not only untapped energy; note that larger flow rates through
 395 turbines in reverse modes imply larger breaking torques (Figure 5).

396 Evaluation of the system's performance is in terms of the mean efficiency, which is defined as:

$$397 \quad \bar{\eta}_{system} = \frac{\frac{1}{T} \int_0^T \omega T_{total} dt}{\frac{1}{T} \int_0^T \Delta P_t Q_{total} dt} = \frac{\frac{1}{T} \int_0^T \Delta P_t q_{direct} dt}{\underbrace{\frac{1}{T} \int_0^T \Delta P_t Q_{total} dt}_{\bar{\eta}_{input}}} \frac{\frac{1}{T} \int_0^T \omega (T_{direct} + T_{reverse}) dt}{\underbrace{\frac{1}{T} \int_0^T \Delta P_t q_{direct} dt}_{\bar{\eta}_{tg}}} \quad (7)$$

398 where T_{total} is the total torque on the electricity generator. Therefore:

$$399 \quad \bar{\eta}_{system} = \bar{\eta}_{input} \bar{\eta}_{tg} \quad (8)$$

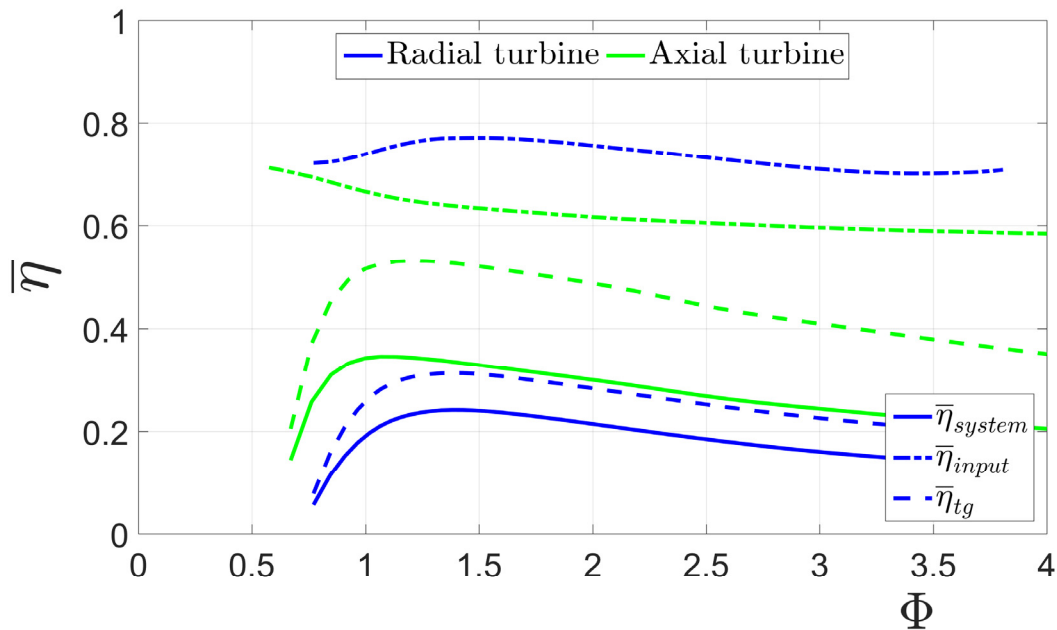
400 Mean input efficiency, η_{input} , is a parameter closely related to the volumetric efficiency of the system
 401 (Figure 14), whereas twin-turbines efficiency, η_{tg} , is the efficiency of the twin turbine group, calculated
 402 with regard to the flow rate, which is supposed to produce energy (q_{direct}).

403 There are references (Takao et al., 2011) where the η_{tg} is calculated by not taking into account the
 404 torque of the turbine in reverse mode, despite the fact that the flow through the turbine in reverse
 405 mode is being considered. This common hypothesis is a reasonable assumption if the turbine running
 406 in reverse mode is disconnected from the rotating axis with some disrupting element. In this study, and
 407 in order to be conservative, the torque in reverse mode has been preserved in the definition.

408 Figure 15 shows the different efficiencies for the twin-turbine configuration for both radial and axial
 409 turbines. The results show that maximum total efficiency of the system (η_{system}) is 24% in the case of
 410 the radial turbine. As expected, the axial turbine (using performance data from (Takao et al., 2011))
 411 has a significantly higher value, reaching 34% at $\Phi = 1$ (solid green line). If only efficiency of the
 412 turbines is considered, the superior performance of the axial machine is demonstrated, with
 413 enhancement of η_{tg} by up to 20% in the case of axial turbines. However, the strong feature of the
 414 radial turbines is the remarkable η_{input} , close to 80% for the optimal range of flow coefficients (around
 415 $\Phi = 1.4$). Therefore, the poor efficiency of the radial turbine in direct mode is significantly balanced by a
 416 superior performance in reverse flow conditions.

417 Consequently, radial turbines can be an interesting option for an OWC device with a twin turbine
 418 configuration, provided that more developments are carried out with regard to turbine blades; this
 419 would increase the efficiency of the turbine itself (with the current design, the difference in η_{tg} is still
 420 excessively favorable for axial turbines).

421 Bridging this gap, the greater volumetric efficiency of the radial turbines, combined with the sharp
 422 reduction in flow leaking through the reverse mode turbine, may be key factors to justify the
 423 development of a new generation of twin-turbine prototypes with radial architecture.



425

426 Figure 15. Mean efficiencies of the twin turbine system with radial turbines compared to axial turbines
 427 (data taken from (Takao et al., 2011)).
 428

429 4. CONCLUSIONS

430 This paper studies the performance of OWC devices, based on a twin turbine configuration, with radial
 431 turbines. To the best of the authors' knowledge, the use of a radial turbine to enhance flow rectification
 432 in twin turbine systems is presented for the first time in the open literature.

433 Firstly, a CFD model of the radial turbine has been validated and employed to assess turbine
 434 performance in both modes of operation: direct (centrifugal) and reverse (centripetal). It is shown that
 435 the large pressure drop generated in reverse mode implies enhanced exploitation of the energy
 436 produced by the OWC because only a reduced part of the total flow rate leaks through the turbine
 437 working in reverse mode. Despite of the lower efficiencies found in radial turbines, their improved
 438 performance as backflow preventers in comparison with axial machines makes radial turbines a
 439 promising option for being installed in twin turbines systems.

440 To be fully competitive, the major challenge is to close the gap in the performance of radial turbines for
 441 direct mode. In particular, a greater effort regarding design is needed to reduce the large kinetic
 442 energy loss of radial turbines at the outlet. An improvement in the blade profiles, combined with a
 443 reduction in flow deflection, could reduce this detrimental effect and improve efficiency in direct mode.
 444 Alternatively, performance in reverse mode could be preserved, because the main amount of loss,
 445 namely, the swirl at the elbow, is not dependent on the blade's external angle.

446 In summary, although much work is still required to improve the performance of radial turbines in
 447 centrifugal operation, this research demonstrates that radial turbines can be a suitable option for use
 448 in twin turbine configurations for OWC power plants.

449

450 5. ACKNOWLEDGEMENTS

451 The authors acknowledge the support provided by "Centro Integrado de F.P. Mantenimiento y
 452 Servicios a la Producción de Langreo", with special mention to its Director, Mr. F. Fanjul.

453

454 **6. REFERENCES**

- 455 Babintsev, I.A., 1975. Apparatus for converting sea wave energy into electrical energy. Patent nº US
456 3922739.
- 457 Curran, R.; Denniss, Tom; Boake, C., 2000. Multidisciplinary design for performance ocean wave
458 energy conversion, in: Proceedings of the 10th International Offshore Polar Engineering
459 Conference. Seattle.
- 460 Dixon, S.L., Hall, C.A., 2005. Fluid mechanics and thermodynamics of turbomachinery, 5th ed.
461 Elsevier Butterworth–Heinemann, Oxford.
- 462 Dudhgaonkar, P. V., Jayashankar, V., Jalihal, P., Kedarnath, S., Setoguchi, T., Takao, M., Nagata, S.,
463 Toyota, K., 2011. Fluidic components for oscillating water column based wave energy plants, in:
464 ASME-JSME-KSME 2011 Joint Fluids Engineering Conference: Volume 1, Symposia – Parts A,
465 B, C, and D. ASME, Hamamatsu, Japan, pp. 1979–1983. doi:10.1115/AJK2011-07035
- 466 Falcão, A.F. de O., 2010. Wave energy utilization: A review of the technologies. *Renew. Sustain.*
467 *Energy Rev.* 14, 899–918. doi:10.1016/j.rser.2009.11.003
- 468 Falcão, A.F.O., Gato, L.M.C., 2012. Air Turbines, in: Sayigh, A.A. (Ed.), *Comprehensive Renewable*
469 *Energy*. Elsevier, Oxford, pp. 111–149. doi:10.1016/B978-0-08-087872-0.00805-2
- 470 Falcão, A.F.O., Gato, L.M.C., Henriques, J.C.C., Borges, J.E., Pereiras, B., Castro, F., 2015. A novel
471 twin-rotor radial-inflow air turbine for oscillating-water-column wave energy converters. *Energy*
472 93, 2116–2125. doi:10.1016/j.energy.2015.10.046
- 473 Falcão, A.F.O., Henriques, J.C.C., 2016. Oscillating-water-column wave energy converters and air
474 turbines: A review. *Renew. Energy* 85, 1391–1424. doi:10.1016/j.renene.2015.07.086
- 475 Inoue, M., Kaneko, K., Setoguchi, T., Saruwatari, T., 1988. Studies on the Wells turbine for wave
476 power generation (turbine characteristics and design parameter for irregular wave). *JSME Int. J.*
477 31, 676–682. doi:10.1299/jsmeb1988.31.4_676
- 478 Jayashankar, V., Anand, S., Geetha, T., Santhakumar, S., Jagadeesh Kumar, V., Ravindran, M.,
479 Setoguchi, T., Takao, M., Toyota, K., Nagata, S., 2009. A twin unidirectional impulse turbine
480 topology for OWC based wave energy plants. *Renew. Energy* 34, 692–698.
481 doi:10.1016/j.renene.2008.05.028
- 482 Maeda, H., Santhakumar, S., Setoguchi, T., Takao, M., Kinoue, Y., Kaneko, K., 1999. Performance of
483 an impulse turbine with fixed guide vanes for wave power conversion. *Renew. Energy* 17, 533–
484 547. doi:10.1016/S0960-1481(98)00771-X
- 485 Maeda, H., Takao, M., Setoguchi, T., Kaneko, K., Kim, T.H., 2001. Impulse turbine for wave power
486 conversion with air flow rectification system, in: Proceedings of the 11th International Offshore
487 and Polar Engineering Conference. Stavanger, Norway.
- 488 Mala, K., Jayaraj, J., Jayashankar, V., Muruganandam, T.M., Santhakumar, S., Ravindran, M., Takao,
489 M., Setoguchi, T., Toyota, K., Nagata, S., 2011. A twin unidirectional impulse turbine topology for
490 OWC based wave energy plants - Experimental validation and scaling. *Renew. Energy* 36, 307–
491 314. doi:10.1016/j.renene.2010.06.043
- 492 Pereiras, B., Castro, F., el Marjani, A., Rodríguez, M. a., 2011a. Tip clearance effect on the flow
493 pattern of a radial impulse turbine for wave energy conversion. *J. Turbomach.* 133, 41019.
494 doi:10.1115/1.4002409
- 495 Pereiras, B., Castro, F., Marjani, A. el, Rodríguez, M.A., 2011b. An improved radial impulse turbine for
496 OWC. *Renew. Energy* 36, 1477–1484. doi:10.1016/j.renene.2010.10.013
- 497 Pereiras, B., Valdez, P., Castro, F., 2014. Numerical analysis of a unidirectional axial turbine for twin
498 turbine configuration. *Appl. Ocean Res.* 47, 1–8. doi:10.1016/j.apor.2014.03.003
- 499 Raghunathan, S., 1995. The Wells air turbine for wave energy conversion. *Prog. Aerosp. Sci.* 31, 335–
500 386. doi:10.1016/0376-0421(95)00001-F
- 501 Setoguchi, T., Santhakumar, S., Takao, M., Kim, T.H., Kaneko, K., 2002. A performance study of a

502 radial turbine for wave energy conversion. Proc. Inst. Mech. Eng. Part A J. Power Energy 216,
503 15–22. doi:10.1243/095765002760024917

504 Setoguchi, T., Takao, M., 2006. Current status of self rectifying air turbines for wave energy
505 conversion. Energy Convers. Manag. 47, 2382–2396. doi:10.1016/j.enconman.2005.11.013

506 Takao, M., Setoguchi, T., 2012. Air turbines for wave energy conversion. Int. J. Rotating Mach. 2012.
507 doi:10.1155/2012/717398

508 Takao, M., Takami, A., Okuhara, S., Setoguchi, T., 2011. A twin unidirectional impulse turbine for
509 wave energy conversion. J. Therm. Sci. 20, 394–397. doi:10.1007/s11630-011-0486-1

510 Thakker, A., Dhanasekaran, T.S., 2005. Computed effect of guide vane shape on performance of
511 impulse turbine for wave energy conversion. Int. J. Energy Res. 29, 1245–1260.
512 doi:10.1002/er.1117

513 Torre-Enciso, Y., Ortubia, I., López de Aguilera, L.I., Marqués, J., 2009. Mutriku wave power plant:
514 from the thinking out to the reality, in: 8th European Wave and Tidal Energy Conference
515 (EWTEC 2009). Uppsala, Sweden, pp. 319–328.

516 Wells, A.A., 1980. Rotary transducers. Patent n° US4221538 A.

517