

Holographic Kondo and Fano resonances

Johanna Erdmenger,^{1,*} Carlos Hoyos,^{2,†} Andy O’Bannon,^{3,‡} Ioannis Papadimitriou,^{4,§}
Jonas Probst,^{5,||} and Jackson M. S. Wu^{6,¶}

¹*Institut für Theoretische Physik und Astrophysik, Julius-Maximilians-Universität Würzburg,
Am Hubland, D-97074 Würzburg, Germany and
Max-Planck-Institut für Physik (Werner-Heisenberg-Institut),
Föhringer Ring 6, D-80805 Munich, Germany*

²*Department of Physics, Universidad de Oviedo, Avda. Calvo Sotelo 18, 33007 Oviedo, Spain*

³*STAG Research Centre, Physics and Astronomy, University of Southampton,
Southampton SO17 1BJ, United Kingdom*

⁴*SISSA and INFN—Sezione di Trieste, Via Bonomea 265, I 34136 Trieste, Italy*

⁵*Rudolf Peierls Centre for Theoretical Physics, University of Oxford,
1 Keble Road, Oxford OX1 3NP, United Kingdom*

⁶*Department of Physics and Astronomy, University of Alabama, Tuscaloosa, Alabama 35487, USA*
(Received 8 December 2016; published 12 July 2017)

We use holography to study a $(1 + 1)$ -dimensional conformal field theory (CFT) coupled to an impurity. The CFT is an $SU(N)$ gauge theory at large N , with strong gauge interactions. The impurity is an $SU(N)$ spin. We trigger an impurity renormalization group (RG) flow via a Kondo coupling. The Kondo effect occurs only below the critical temperature of a large- N mean-field transition. We show that at all temperatures T , impurity spectral functions exhibit a Fano resonance, which in the low- T phase is a large- N manifestation of the Kondo resonance. We thus provide an example in which the Kondo resonance survives strong correlations, and uncover a novel mechanism for generating Fano resonances, via RG flows between $(0 + 1)$ -dimensional fixed points.

DOI: [10.1103/PhysRevD.96.021901](https://doi.org/10.1103/PhysRevD.96.021901)

I. INTRODUCTION

The Kondo effect is the screening of an impurity spin by a Landau Fermi liquid (LFL) at low T [1,2]. A variety of techniques, such as Wilson’s RG, large- N , CFT, and more [3], have captured many characteristic Kondo phenomena. Nevertheless, many questions resist solution, for example about inter-impurity interactions, subsystem entanglement entropy (EE), nonequilibrium processes like quantum quenches, and more.

In particular, what happens when the LFL is replaced with strongly correlated electrons? For example, how does the Kondo effect change in a Luttinger liquid [4–8] or the Hubbard model [9,10]? In the latter case, experiments reveal dramatic effects of strong correlations, such as enhancement of the Kondo temperature, T_K [53]. On the theory side, although special tools like bosonization [4–8] and uncontrolled mean-field approximations [9,11–17] have provided insight, in general, reliable techniques do not yet exist to answer questions about Kondo phenomena in strongly-correlated systems.

To address all of the above, we have developed an alternative Kondo model, based on holographic duality

[18–21]. Our model replaces the LFL by a $(1 + 1)$ -dimensional CFT in which spin $SU(2)$ is replaced by *gauged* $SU(N)$, with large N and strong gauge interactions. Our model has already revealed novel strong-coupling phenomena in RG [18,19], interimpurity interactions [19] and EE [20].

Here we initiate the study of nonequilibrium phenomena in our model: we compute linear response (Green’s) functions of a charged bosonic impurity operator, \mathcal{O} , in our model. We have two main results.

First, we find a large- N manifestation of the *Kondo resonance* [2,22,23], a signature of the Kondo effect. As expected, our Kondo resonance appears only at T below the critical temperature T_c of a mean-field transition that is common to large- N Kondo models [23–27]: $\langle \mathcal{O} \rangle$ becomes non-zero when $T \leq T_c$. We thus prove unequivocally that our holographic model realizes a genuine Kondo effect, as opposed to some other impurity physics, and furthermore show that a large- N Kondo resonance can survive strong correlations essentially intact.

Second, at all T , \mathcal{O} ’s spectral function exhibits a *Fano resonance* [28,29], which occurs when a Lorentzian resonance is immersed in a continuum of states (in energy). A Fano resonance is characterized not only by its position, width, and height, like a Lorentzian, but also by an *asymmetry parameter*, q , which measures the relative strength of resonant versus non-resonant scattering. Our q increases as $T \rightarrow T_c^+$. When $T \leq T_c$, the Fano line-shape arises from our Kondo resonance, which must be

*erdmenger@physik.uni-wuerzburg.de

†hoyoscarlos@uniovi.es

‡a.obannon@soton.ac.uk

§ioannis.papadimitriou@sissa.it

||Jonas.Probst@physics.ox.ac.uk

¶jknwgm13@gmail.com

antisymmetric due to particle-hole symmetry (PHS), and hence has the special value $q = 1$.

Although Fano resonances have been observed in many impurity systems in one spatial dimension [29–32], ours arise from a qualitatively different mechanism. For instance, in side-coupled quantum dots (QDs) [29,31,32] the Lorentzian resonances are the discrete states on the QD, and the continuum comes from electronic scattering states in the leads. Coupling the two, for example by a Kondo coupling, can then produce Fano resonances.

Our model also has an impurity coupled to a continuum in one spatial dimension, i.e. the CFT. However, our model has *two* couplings: the CFT's $SU(N)$ gauge coupling and the Kondo coupling. The spectral function of \mathcal{O} inherits $(0+1)$ -dimensional scale invariance from the former, and so exhibits a continuum of states, in contrast to a QD's discrete states. The Kondo coupling then triggers an RG flow from that $(0+1)$ -dimensional fixed point, and creates a resonance that cannot escape the continuum, hence producing a Fano line shape.

To our knowledge, such a mechanism for producing Fano resonances is novel, and moreover is easy to generalize to any RG flow between $(0+1)$ -dimensional fixed points, as follows. Scale invariance implies that any spectral function will be a featureless continuum, which in $(0+1)$ dimensions means a power law (or logarithm) in frequency. A relevant deformation can then explicitly break scale invariance, trigger an RG flow to an IR fixed point—in which case we expect the continuum to survive—and may also produce resonances. In higher dimensions, the resonances would not have to be within the continuum, for example the two could be separated in momentum space. However, in $(0+1)$ dimensions the resonances have no place to escape the continuum, and hence must produce Fano line shapes.

In fact, such a mechanism was at work in some previous cases, such as the large- N Kondo model at sufficiently low T [33], and holographic duals of $T = 0$ charged black branes [34–36]. However, the resulting Fano resonances went unidentified, leaving crucial physics overlooked, namely the relative strength of resonant versus non-resonant scattering, as measured by q . Our results not only provide a novel perspective on these cases, but also predict Fano resonances in RG flows between other $(0+1)$ -dimensional fixed points, such as Sachdev-Ye-Kitaev fixed points [36–43].

Further results of our model, including details of holographic renormalization useful for holographic impurity models in general, will appear in [44].

II. HOLOGRAPHIC KONDO MODEL

We first briefly review some essential features of the CFT and large- N approaches to the Kondo model, and how our model builds upon and extends them.

The CFT approach [45] is based on s-wave reduction of LFL fermions about the impurity, plus linearization of the dispersion relation. In/out-going s-waves become relativistic left/right-moving fermions, ψ_L and ψ_R , in the radial direction, r . Reflecting ψ_R to $r < 0$ and relabeling $\psi_R \rightarrow \psi_L$ leads to ψ_L alone on the entire r axis, with impurity at $r = 0$. The ψ_L form a $(1+1)$ -dimensional chiral CFT with $SU(2)_1 \times U(1)$ spin and charge Kac-Moody currents, respectively. In the Hamiltonian, the Kondo interaction is $\delta(r)g_K S^A J^A$, with coupling constant g_K , impurity spin S^A , and spin current J^A , $A = 1, 2, 3$. An antiferromagnetic coupling, $g_K > 0$, is marginally relevant, and triggers an RG flow to an IR chiral CFT characterized by a phase shift of ψ_L and impurity screening [45].

The large- N approach begins by replacing spin $SU(2) \rightarrow SU(N)$, followed by $N \rightarrow \infty$ with $\lambda_K \equiv Ng_K$ fixed [3,23,46,47]. We will only consider S^A in totally antisymmetric $SU(N)$ representations of rank \mathcal{Q} , and introduce Abrikosov pseudofermions χ via $S^A = \chi^\dagger T^A \chi$, with $SU(N)$ generators T^A , $A = 1, \dots, N^2 - 1$. Doing so introduces an auxiliary $U(1)$ acting only on χ , but with charge fixed by projecting onto states with $\chi^\dagger \chi = \mathcal{Q}$. At large N , $S^A J^A = -\mathcal{O}^\dagger \mathcal{O}/2$ with $\mathcal{O} \equiv \psi_L^\dagger \chi$ [19], which is charged under both the charge and auxiliary $U(1)$'s.

Our holographic model [18] begins by *gauging* $SU(N)$, thus introducing the 't Hooft coupling, λ . We then add degrees of freedom to make the gauge theory a $(1+1)$ -dimensional CFT with sparse operator spectrum when N and λ both $\rightarrow \infty$, but whose details otherwise are irrelevant. The theory is then holographically dual to Einstein-Hilbert gravity in $(2+1)$ -dimensional anti-de Sitter space, AdS_3 [48]. The charge $U(1)$ Kac-Moody current is dual to a $U(1)$ Chern-Simons gauge field, A , the auxiliary $U(1)$ is dual to a Maxwell field a on an AdS_2 defect at $r = 0$, and \mathcal{O} is dual to a complex scalar field Φ also in AdS_2 , charged under both A and a . As long as the stress-energy tensor is finite, at large N we can neglect backreaction of A , a , Φ (dual to fundamental fields) on the geometry (dual to adjoint fields). When $T > 0$, the bulk metric is thus the BTZ black brane,

$$ds^2 = \frac{1}{z^2} (h^{-1}(z) dz^2 - h(z) dt^2 + dr^2),$$

with $h(z) = 1 - z^2/z_H^2$ where $z_H = 1/2\pi T$, and unit AdS radius. The fields a and Φ are localised to the asymptotically AdS_2 subspace at $r = 0$, with induced metric g_{mn} ($m, n = z, t$). We describe the dynamics of A , a , and Φ by the simple quadratic action [18],

$$S = -\frac{N}{4\pi} \int_{BTZ} A \wedge dA + S_{AdS_2}, \quad (1a)$$

$$S_{\text{AdS}_2} = -N \int_{x=0} dz dt \sqrt{-g} \left(\frac{1}{4} f^{mn} f_{mn} + (D^m \Phi)^\dagger (D_m \Phi) + M^2 \Phi^\dagger \Phi \right), \quad (1b)$$

with field strength $f = da$, covariant derivative $D_m \Phi = (\partial_m + iA_m - ia_m)\Phi$, and mass-squared M^2 . At the horizon $z = z_H$ we require regularity of all fields. At the boundary $z = 0$, a 's leading mode, $a \sim Q/z$, is related to Q : $Q \neq 0$ breaks χ 's PHS, so the PHS value $Q = 0$ is dual to the PHS value $Q = N/2$, and increasing $|Q|$ corresponds to increasing $|Q - N/2|$.

The large- N Kondo interaction $-\lambda_K \mathcal{O}^\dagger \mathcal{O}$ is classically marginal, hence \mathcal{O} has UV dimension $\Delta = 1/2$, which fixes M^2 and hence Φ 's near-boundary expansion, $\Phi \sim \sqrt{z}(\alpha \log z + \beta)$. Introducing the Kondo interaction amounts to adding a boundary term $\propto -\lambda_K \mathcal{O}^\dagger \mathcal{O}/2$ to S , which changes Φ 's boundary condition from $\alpha = 0$ to $\alpha = -\lambda_K \beta$ [18,49,50]. For more details about the boundary terms, see [19,44]. A holographic scaling analysis reveals that λ_K runs logarithmically, $\lambda_K = 1/\log(T/T_K)$, diverging at the dynamically-generated Kondo temperature, $T_K \equiv \Lambda e^{-1/\lambda_K}/(2\pi)$, with λ_K evaluated at the UV cutoff, Λ . A holographic antiferromagnetic UV Kondo coupling, $\lambda_K > 0$, is thus marginally relevant, breaks conformal invariance, and triggers an RG flow.

As mentioned above, our model has a mean-field phase transition [18]: $\langle \mathcal{O} \rangle = 0$ ($\Phi = 0$) when $T > T_c$ and $\langle \mathcal{O} \rangle \neq 0$ ($\Phi \neq 0$) when $T \leq T_c$. Condensate formation $\langle \mathcal{O} \rangle \neq 0$ breaks the charge and auxiliary $U(1)$'s to the diagonal, and signals the Kondo effect, including a phase shift of ψ_L , dual to a Wilson line of A , and impurity screening, dual to reduction of f flux between $z = 0$ and $z = z_H$. We refer to the $T > T_c$ and $T \leq T_c$ phases as ‘‘unscreened’’ and ‘‘screened,’’ respectively. In [18–21] we computed T_c numerically. Below we obtain an exact formula for T_c .

III. FANO RESONANCES

If a retarded Green's function of complex frequency ω , $G(\omega)$, has a pole at ω_p , $G(\omega) \sim \frac{Z}{\omega - \omega_p}$, with complex residue $Z = Z_R + iZ_I$, then near the pole the spectral function $\rho(\omega) \equiv -2\text{Im}(G(\omega))$ will have a Fano resonance [28,29] (setting $\text{Im}(\omega) = 0$),

$$\rho_{\text{Fano}}(\omega) = \frac{(\omega - \omega_0 + q\Gamma/2)^2}{(\omega - \omega_0)^2 + (\Gamma/2)^2}, \quad (2)$$

with position $\omega_0 = \text{Re}(\omega_p)$, width $\Gamma = 2|\text{Im}(\omega_p)|$, and asymmetry parameter $q = -Z_R/Z_I + \sqrt{1 + Z_R^2/Z_I^2}$. Fano resonances are antisymmetric when $q = 1$, meaning $\rho(\omega)$ is odd under PHS, and symmetric when $q = 0$ (an anti-resonance) or ∞ (a Lorentzian), meaning $\rho(\omega)$ is even. Fano resonances arise when a Lorentzian resonance is

immersed in a continuum (in energy), due to interference between the two. The asymmetry parameter q contains key dynamical information, specifically, $q^2 \propto$ the ratio of probabilities of resonant and non-resonant scattering.

In our model, the AdS_2 subspace inherits scale invariance from AdS_3 , or in dual field theory language, the impurity inherits scale invariance from the CFT, so $\rho(\omega)$ of impurity operators must be a featureless continuum. Our marginally-relevant Kondo coupling then breaks scale invariance and produces a resonance, while $Q \neq 0$ breaks PHS. We will show that $\rho(\omega)$ of \mathcal{O} then indeed generically exhibits asymmetric Fano resonances.

IV. SPECTRAL FUNCTIONS

We compute $G(\omega)$ holographically by solving for linearized fluctuations about solutions for the unscreened and screened phases [44,51,52]. At all T , we find that the Kac-Moody current's $G(\omega)$ is unaffected by the impurity. In the unscreened phase, we find that all charged $G(\omega)$ vanish, i.e. $G_{\mathcal{O}\mathcal{O}}(\omega) \equiv \langle \mathcal{O}(\omega)\mathcal{O}(-\omega) \rangle = 0$, while

$$G_{\mathcal{O}^\dagger \mathcal{O}}(\omega) \equiv \langle \mathcal{O}^\dagger(\omega)\mathcal{O}(-\omega) \rangle = \frac{N}{\lambda_K} \left(1 - \frac{1}{\lambda_K D(\omega)} \right),$$

$$D(\omega) \equiv H \left[-\frac{1}{2} + iQ - \frac{i\omega}{2\pi T} \right] + H \left[-\frac{1}{2} - iQ \right] + \ln \left(\frac{2T}{T_K} \right),$$

with Harmonic number $H[x]$, and λ_K evaluated at Λ . The form of $G_{\mathcal{O}\mathcal{O}^\dagger}(\omega)$ is the same, but with $Q \rightarrow -Q$. Scale invariance in $(0+1)$ -dimensions and $\Delta = 1/2$ imply a trivial UV continuum: $\lim_{\omega \rightarrow \infty} \rho_{\mathcal{O}^\dagger \mathcal{O}}(\omega) = 0$.

For given Q and T , $G_{\mathcal{O}^\dagger \mathcal{O}}(\omega)$ has poles in ω when $D(\omega) = 0$. Figure 1 shows our numerical results for the

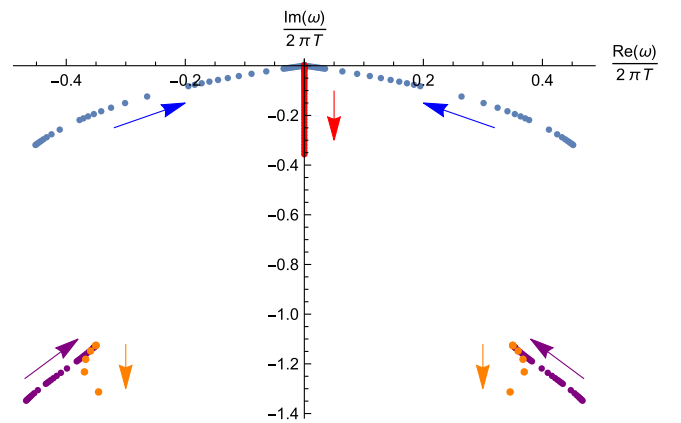


FIG. 1. Positions of poles in the complex $\omega/(2\pi T)$ plane for $Q = 1/2$. Blue and purple denote lowest and next-lowest poles, respectively, of $G_{\mathcal{O}^\dagger \mathcal{O}}(\omega)$ ($\text{Re}(\omega) > 0$) and $G_{\mathcal{O}\mathcal{O}^\dagger}(\omega)$ ($\text{Re}(\omega) < 0$), for T/T_c from 100 down to 1.001. Red and orange denote the same for $G_{\mathcal{O}^\dagger \mathcal{O}}(\omega)$ for T/T_c from 1 down to 0.2. Arrows indicate movement of poles as T decreases.

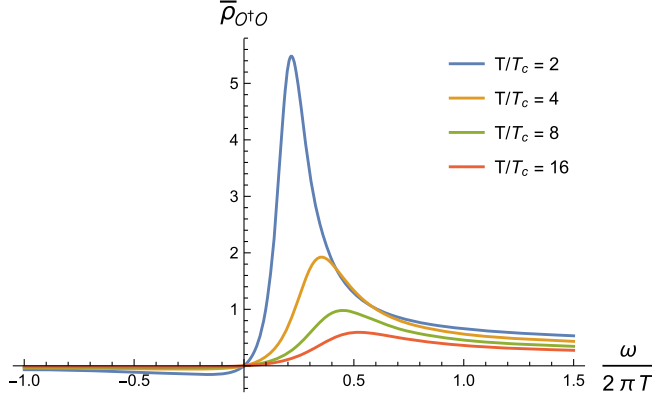


FIG. 2. The normalized spectral function $\bar{\rho}_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$ versus real $\omega/(2\pi T)$ for $Q = 1/2$ and, from shortest to tallest, $T/T_c = 16$ (red), 8 (green), 4 (orange), and 2 (blue).

positions of the lowest (closest to $\omega = 0$) and next-lowest poles of $G_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$ and $G_{\mathcal{O}\mathcal{O}^\dagger}(\omega)$ in the complex $\omega/(2\pi T)$ plane, for $Q = 1/2$. Other Q give similar results. As $T \rightarrow T_c^+$, the lowest pole moves towards the origin, arrives there at T_c , and when $T < T_c$, crosses into the $\text{Im}(\omega) > 0$ region, signaling instability (not shown). We thus identify T_c as the T where $D(\omega = 0) = 0$,

$$T_c = \frac{1}{2} T_K \exp \left[-2 \text{Re} \left(H \left[\frac{1}{2} + iQ \right] \right) \right].$$

Figure 2 shows the normalized spectral function $\bar{\rho}_{\mathcal{O}^\dagger\mathcal{O}}(\omega) \equiv -2 \frac{\lambda_K^2}{N} \text{Im} G_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$ versus real $\omega/(2\pi T)$ for $Q = 1/2$ and $T/T_c = 16, 8, 4, 2$. We find a Fano resonance, as advertised, with asymmetric minimum and maximum. Numerically, $\omega_0 \approx \text{Re}(\omega_p)$ and $\Gamma \approx 2|\text{Im}(\omega_p)|$, as in (2), where ω_p is $G_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$'s lowest pole. As $T \rightarrow T_c^+$, q grows: $q \approx 1.7$ at $T = 16T_c$ while $q \approx 4$ at $T = 2T_c$.

For T just above T_c , $T \gtrsim T_c$, expanding in T about T_c and in ω about $\omega = 0$ gives, for $G_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$'s lowest pole,

$$\frac{\omega_p}{2\pi T} = -i \frac{T/T_c - 1}{\psi'[\frac{1}{2} + iQ]}, \quad Z = -i \frac{N}{\lambda_K^2} \frac{2\pi T_c}{\psi'[\frac{1}{2} + iQ]}, \quad (3)$$

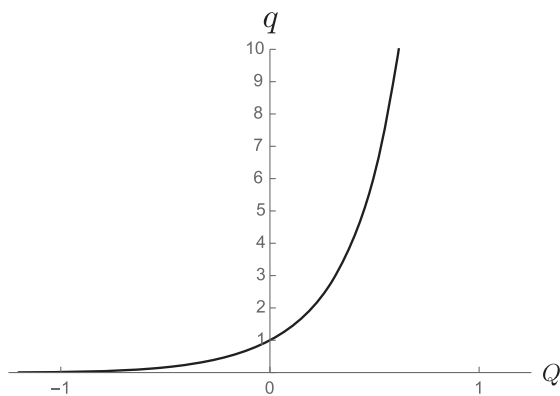


FIG. 3. Asymmetry parameter q versus Q , for $T \gtrsim T_c$.

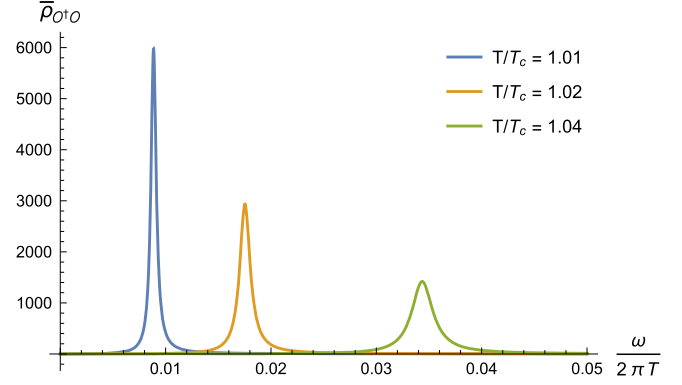


FIG. 4. The normalized spectral function, $\bar{\rho}_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$, versus real $\omega/(2\pi T)$ for $Q = 1$ and, from shortest to tallest, $T/T_c = 1.04$ (green), 1.02 (orange), and 1.01 (blue).

with digamma function $\psi[x]$. The resonance height thus grows as $(T/T_c - 1)^{-1}$ and the width shrinks as $T/T_c - 1$. It is therefore *not* related to a Kondo resonance, which grows *logarithmically* as $T \rightarrow T_K^+$ [22]. Indeed, at large N we expect the Kondo resonance only in the screened phase [23]. Our resonance is presumably a bound state of ψ_L and χ , heralding the nascent screened phase.

The Z in (3) gives q that depends only on Q , shown in Fig. 3. (Anti)symmetric values $q = 1, 0, \infty$ occur when $Q \rightarrow 0, \mp \infty$, respectively. Indeed, Fig. 4 shows that even for relatively modest $Q = 1$, the resonance is nearly Lorentzian, the minimum having practically vanished.

In the screened phase, we have numerical results for $G_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$ [18–21,44]. Figure 1 shows our numerical results for the positions of the lowest and next-lowest poles in $G_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$ for $Q = 1/2$. Other Q give similar results. At $T = T_c$ the poles are coincident with those of $G_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$ and $G_{\mathcal{O}\mathcal{O}^\dagger}(\omega)$ in the unscreened phase. As T decreases below T_c , $G_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$'s lowest pole, ω_p , moves straight down the $\text{Im}(\omega)$ axis.

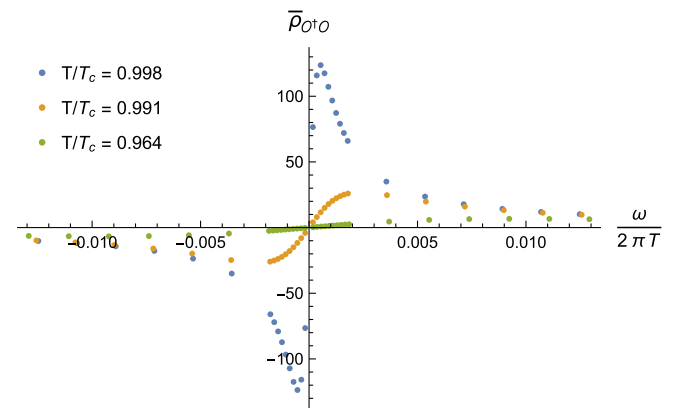


FIG. 5. The normalized spectral function $\bar{\rho}_{\mathcal{O}^\dagger\mathcal{O}}(\omega)$ versus real $\omega/(2\pi T)$ for $Q = 1/2$ and, from tallest to shortest, $T/T_c = 0.998$ (blue), 0.991 (orange), and 0.964 (green).

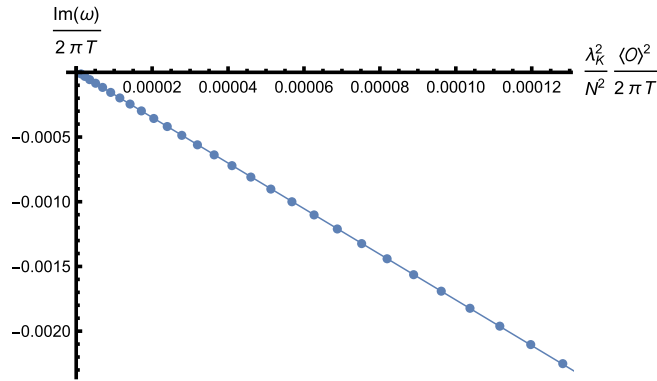


FIG. 6. Dots denote the position of $G_{\mathcal{O}^\dagger \mathcal{O}}(\omega)$'s lowest pole versus $\frac{\lambda_K^2}{N^2} \langle \mathcal{O} \rangle^2 / (2\pi T)$ for $Q = 1/2$. The solid line is a linear fit with slope ≈ -17.6 and intercept at the origin.

From our experience with the unscreened phase, we expect ω_p to produce a Fano resonance in the normalized spectral function, $\bar{\rho}_{\mathcal{O}^\dagger \mathcal{O}}(\omega)$. Crucially, $\text{Re}(w_p) = 0$, so ω_p preserves PHS, $\text{Re}(\omega) \rightarrow -\text{Re}(\omega)$, so we expect an *antisymmetric* Fano resonance at $\text{Re}(\omega) = 0$. Moreover, $|\text{Im}(\omega_p)|$ increases as T decreases, and so should the width Γ . Figure 5 confirms our expectations: $\bar{\rho}_{\mathcal{O}^\dagger \mathcal{O}}(\omega)$'s only significant feature is a Fano resonance at $\text{Re}(\omega) = 0$ with $q = 1$, meaning perfectly antisymmetric minimum and maximum, and whose Γ increases as T decreases. Additionally, the height decreases, and indeed our numerics suggest $\lim_{T \rightarrow 0} \bar{\rho}_{\mathcal{O}^\dagger \mathcal{O}}(\omega) = 0$.

Figure 6 shows our numerical results for the position of ω_p versus small $\frac{\lambda_K^2}{N^2} \langle \mathcal{O} \rangle^2 / (2\pi T)$, or equivalently, T just below T_c , $T \lesssim T_c$, for $Q = 1/2$. Figure 6 also shows a linear fit demonstrating that.¹

$$\omega_p \propto -i \langle \mathcal{O} \rangle^2. \quad (4)$$

Our model's mean-field behavior $\langle \mathcal{O} \rangle \propto (T_c - T)^{1/2}$ then implies $\Gamma \propto T_c - T$ for $T \lesssim T_c$.

¹In [44] we derive (4) without numerics, via a small- $\langle \mathcal{O} \rangle$ expansion.

The behavior in (4) is in fact identical to that in a LFL at large N . In a LFL, the Kondo resonance is formally defined in the LFL fermion spectral function, and at large N appears only in the screened phase, with $\Gamma \propto \langle \mathcal{O} \rangle^2$ [23]. For $T \lesssim T_c$, the mean-field behavior $\langle \mathcal{O} \rangle \propto (T_c - T)^{1/2}$ then implies $\Gamma \propto T_c - T$. Crucially, in the screened phase the Kondo resonance also appears in other spectral functions, due to operator mixing induced by the symmetry breaking [23]. In particular, a Kondo resonance should produce a pole in $G_{\mathcal{O}^\dagger \mathcal{O}}(\omega)$ precisely of the form in (4).² Our result (4) thus proves the existence of a Kondo resonance in our model when $T \lesssim T_c$, with defining features essentially intact despite the strong interactions.

V. CONCLUSION

In a holographic model describing the interaction of a magnetic impurity with a strongly correlated CFT at large N , we discovered a novel mechanism for producing Fano resonances, namely via RG flows between $(0 + 1)$ -dimensional fixed points. The origin and consequences of such Fano resonances, in existing cases that have gone unidentified and in novel cases, deserve further study, particularly of the physics contained in the asymmetry parameter q .

ACKNOWLEDGMENTS

We would like to thank Ian Affleck, Nathan Andrei, Piers Coleman, Mario Flory, Henrik Johannesson, Andrew Mitchell, Max Newrzella, and Philip Phillips for helpful conversations and correspondence. C.H. is supported by the Ramon y Cajal fellowship RYC-2012-10370, the Asturian Grant No. FC-15-GRUPIN14-108 and the Spanish national Grant No. MINECO-16-FPA2015-63667-P. A.O'B. is a Royal Society University Research Fellow. J.P. is supported by the Clarendon Fund and St John's College, Oxford, and by the European Research Council under the European Union's Seventh Framework Programme (ERC Grant agreement 307955).

²For details, see for example chapter 18 of [23].

- [1] J. Kondo, *Prog. Theor. Phys.* **32**, 37 (1964).
- [2] A. Hewson, *The Kondo Problem to Heavy Fermions* (Cambridge University Press, 1993).
- [3] D.L. Cox and A. Zawadowski, *Adv. Phys.* **47**, 599 (1998).
- [4] D.-H. Lee and J. Toner, *Phys. Rev. Lett.* **69**, 3378 (1992).
- [5] A. Furusaki and N. Nagaosa, *Phys. Rev. Lett.* **72**, 892 (1994).

- [6] P. Fröjdh and H. Johannesson, *Phys. Rev. Lett.* **75**, 300 (1995).
- [7] P. Fröjdh and H. Johannesson, *Phys. Rev. B* **53**, 3211 (1996).
- [8] A. Furusaki, *J. Phys. Soc. Jpn.* **74**, 73 (2005).
- [9] P. Fulde, V. Zevin, and G. Zwicknagl, *Z. Phys. B* **92**, 133 (1993).
- [10] T. Schork and P. Fulde, *Phys. Rev. B* **50**, 1345 (1994).
- [11] G. Khaliullin and P. Fulde, *Phys. Rev. B* **52**, 9514 (1995).

- [12] J. Igarashi, K. Murayama, and P. Fulde, *Phys. Rev. B* **52**, 15966 (1995).
- [13] S. Tornow, V. Zevin, and G. Zwicknagl, [arXiv:cond-mat/9701137](https://arxiv.org/abs/cond-mat/9701137).
- [14] T. Schork and S. Blawid, *Phys. Rev. B* **56**, 6559 (1997).
- [15] B. Davidovich and V. Zevin, *Phys. Rev. B* **57**, 7773 (1998).
- [16] H. T. Duc and N. T. Thang, *Mod. Phys. Lett. B* **13**, 849 (1999).
- [17] W. Hofstetter, R. Bulla, and D. Vollhardt, *Phys. Rev. Lett.* **84**, 4417 (2000).
- [18] J. Erdmenger, C. Hoyos, A. O'Bannon, and J. Wu, *J. High Energy Phys.* **12** (2013) 086.
- [19] A. O'Bannon, I. Papadimitriou, and J. Probst, *J. High Energy Phys.* **01** (2016) 103.
- [20] J. Erdmenger, M. Flory, C. Hoyos, M.-N. Newrzella, and J. M. S. Wu, *Fortschr. Phys.* **64**, 109 (2016).
- [21] J. Erdmenger, M. Flory, C. Hoyos, M.-N. Newrzella, A. O'Bannon, and J. Wu, *Fortschr. Phys.* **64**, 322 (2016).
- [22] P. Phillips, *Advanced Solid State Physics* (Cambridge University Press, 2012).
- [23] P. Coleman, *Introduction to Many-Body Physics* (Cambridge University Press, 2015).
- [24] P. Coleman and N. Andrei, *J. Phys. C* **19**, 3211 (1986).
- [25] P. Coleman, *Phys. Rev. B* **35**, 5072 (1987).
- [26] T. Senthil, S. Sachdev, and M. Vojta, *Phys. Rev. Lett.* **90**, 216403 (2003).
- [27] T. Senthil, M. Vojta, and S. Sachdev, *Phys. Rev. B* **69**, 035111 (2004).
- [28] U. Fano, *Phys. Rev.* **124**, 1866 (1961).
- [29] A. E. Miroshnichenko, S. Flach, and Y. S. Kivshar, *Rev. Mod. Phys.* **82**, 2257 (2010).
- [30] V. Madhavan, W. Chen, T. Jamneala, M. F. Crommie, and N. S. Wingreen, *Science* **280**, 567 (1998).
- [31] V. Madhavan, W. Chen, T. Jamneala, M. F. Crommie, and N. S. Wingreen, *Phys. Rev. B* **64**, 165412 (2001).
- [32] J. Göres, D. Goldhaber-Gordon, S. Heemeyer, M. A. Kastner, H. Shtrikman, D. Mahalu, and U. Meirav, *Phys. Rev. B* **62**, 2188 (2000).
- [33] O. Parcollet, A. Georges, G. Kotliar, and A. Sengupta, *Phys. Rev. B* **58**, 3794 (1998).
- [34] T. Faulkner, H. Liu, J. McGreevy, and D. Vegh, *Phys. Rev. D* **83**, 125002 (2011).
- [35] T. Faulkner, N. Iqbal, H. Liu, J. McGreevy, and D. Vegh, *Phil. Trans. R. Soc. A* **369**, 1640 (2011).
- [36] S. Sachdev, *Phys. Rev. X* **5**, 041025 (2015).
- [37] S. Sachdev and J.-W. Ye, *Phys. Rev. Lett.* **70**, 3339 (1993).
- [38] A. Kitaev, in *KITP Strings seminar and Entanglement 2015 program*, (2015).
- [39] J. Polchinski and V. Rosenhaus, *J. High Energy Phys.* **04** (2016) 001.
- [40] A. Jevicki, K. Suzuki, and J. Yoon, *J. High Energy Phys.* **07** (2016) 007.
- [41] J. Maldacena and D. Stanford, *Phys. Rev. D* **94**, 106002 (2016).
- [42] A. Jevicki and K. Suzuki, *J. High Energy Phys.* **11** (2016) 046.
- [43] E. Witten, [arXiv:1610.09758](https://arxiv.org/abs/1610.09758).
- [44] J. Erdmenger, C. Hoyos, A. O'Bannon, I. Papadimitriou, J. Probst, and J. M. S. Wu, *J. High Energy Phys.* **03** (2017) 039.
- [45] I. Affleck, *Acta Phys. Pol. B* **26**, 1869 (1995).
- [46] N. Bickers, *Rev. Mod. Phys.* **59**, 845 (1987).
- [47] P. Coleman, in *Handbook of Magnetism and Advanced Magnetic Materials: Fundamentals and Theory*, edited by H. Kronmüller and S. Parkin (John Wiley and Sons, New York, 2007), Vol. 1, p. 95.
- [48] O. Aharony, S. S. Gubser, J. M. Maldacena, H. Ooguri, and Y. Oz, *Phys. Rep.* **323**, 183 (2000).
- [49] E. Witten, [arXiv:hep-th/0112258](https://arxiv.org/abs/hep-th/0112258).
- [50] I. Papadimitriou, *J. High Energy Phys.* **05** (2007) 075.
- [51] D. T. Son and A. O. Starinets, *J. High Energy Phys.* **09** (2002) 042.
- [52] P. K. Kovtun and A. O. Starinets, *Phys. Rev. D* **72**, 086009 (2005).
- [53] T. Brugger, T. Schreiner, G. Roth, P. Adelman, and G. Czjzek, *Phys. Rev. Lett.* **71**, 2481 (1993).