

Determination of kinetic parameters for biomass combustion

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ABSTRACT

The aim of this work is to provide a wide database of kinetic data for the most common biomass by thermogravimetric analysis (TGA) and differential thermogravimetry (DTG). Due to the characteristic parameters of DTG curves, a two-stage reaction model is proposed and the kinetic parameters obtained from model-based methods with energy activation values for first and second stages in the range $1.75 \cdot 10^4 - 1.55 \cdot 10^5$ J/mol and $1.62 \cdot 10^4 - 2.37 \cdot 10^5$ J/mol, respectively. However, it has been found that Flynn-Wall-Ozawa and Kissinger-Akahira-Sunose model-free methods are not suitable to determine the kinetic parameters of biomass combustion since the assumptions of these two methods were not accomplished in the full range of the combustion process.

Keywords

Biomass, combustion, kinetic parameters, Coats-Redfern method, thermogravimetric analysis

1. INTRODUCTION

25 The importance of waste biomass as an energy source is likely to increase
26 during the coming years as a result of European energy policy targets
27 (European Environment Agency (EEA), 2010). The total amount of potential
28 biomass in Spain is about 88,677,193 t/year (data from Spanish Renewable
29 Energies Plan 2011-2020 referencing in (Álvarez et al., 2015)), belonging to the
30 agricultural and harvesting residues the largest quantity (up to 37.8% of the total
31 potential biomass).

32 There are still some problems in current biomass combustion furnaces, such
33 as low thermal efficiency, instability of heat load, and slagging (Szemmelveisz
34 et al., 2009; Yang et al., 2004). Computational Fluid Dynamics (CFD) could be
35 useful in solving these problems (Dixon et al., 2005; Ma et al., 2007), but it is
36 absolutely essential having a deep knowledge of the composition (proximate,
37 ultimate and structural analysis) and thermal behaviour as well as the kinetics of
38 the combustion process of biomass.

39 The aim of this article is to determine the combustion kinetics parameters of
40 the most commonly used types of biomass in Spain using a thermogravimetric
41 analyser (TGA), since this technique is widely used in the analysis of weight
42 loss characteristics of biomass fuels (Garcia-Maraver et al., 2015; Kok and
43 Özgür, 2013; Maia and de Morais, 2016)

44

45 **2. MATERIALS AND METHODS**

46 **2.1 Materials**

47 Twenty eight different biomass samples were tested to obtain their activation
48 energy, E_a , and pre-exponential Arrhenius factor, k_0 , values for combustion.

49 These samples were selected trying to track a wide variety of different biomass
50 origins such as commercial fuels, industrial and forest wastes, energy crops and
51 cereals. Their proximate and ultimate analysis data and other properties are
52 available in a database previously published by this research group (García et
53 al., 2014a, 2014b) . These samples were pre-treated to assure homogeneity
54 and reproducibility of the carried-out tests and to that aim they were air-dried for
55 a day at room temperature, grinded and sieved to 250-500 μm .

56

57 **2.2. TG method**

58 10 mg of the sample were subjected to thermal decomposition at 4 different
59 low heating rates (5, 10, 15 and 20 K/min) in a Perkin-Elmer STA 6000, using
60 40 ml/min of both purge (N_2) and carrier (air) gas.

61 Particle diameter and, consequently, heating rates must be low, particle size
62 should be smaller than 500 μm (Garcia-Maraver et al., 2015; Parthasarathy et
63 al., 2013; Shen et al., 2009), while oxidizing gas flux high in order to guarantee
64 chemical-kinetic reaction control, avoiding as possible temperature and
65 concentration gradients (Parthasarathy et al., 2013).

66

67 **2.3. Kinetic models**

68 In the case of combustion some authors consider just one global reaction
69 divided in three different stages (drying, pyrolysis and char combustion) (Fang
70 et al., 2013; Gangavati et al., 2005), others consider two parallel reactions with
71 three reaction stages (Wang et al., 2014). Finally (Gil et al., 2010) considers a
72 two stage reaction, with a first step between 200-365 $^{\circ}\text{C}$ (oxidative degradation)

73 followed by combustion of char between 365-500 °C. A similar model is
74 proposed by (Shen et al., 2009) and (Fang et al., 2006), who apply those
75 methods to a two reaction oxidation-reduction pyrolysis.

76 There are two main mathematical approaches to obtain the descriptors of
77 combustion kinetics of biomass samples: (a) model-free methods (iso-
78 conversional methods) and (b) model-based methods. Both approaches depart
79 from a general conversion-time relationship:

$$\frac{d\alpha}{dt} = k(T) \cdot f(\alpha) \quad (1)$$

80 Where $f(\alpha)$ is the mechanistic term and $k(T)$ the thermal dependence term
81 that can be defined by Arrhenius law:

$$k(T) = k_0 \cdot e^{-E_a/RT} \quad (2)$$

82 Conversion rate can be defined as a relation between initial (m_0), final
83 (m_∞) and instantaneous (m_t) sample mass. These data can be obtained from
84 each sample TG profile.

$$\alpha = \frac{m_0 - m_t}{m_0 - m_\infty} \quad (3)$$

85 The kinetic term $f(\alpha)$ depends on the conditions and the stage of the reaction
86 to study, but it can be usually expressed as $(1-\alpha)$ (Bahng et al., 2009; Fang et
87 al., 2006; Shen et al., 2009), if first reaction order is considered. If other reaction
88 model is required it should be substituted by one of the expressions shown at
89 Table 1. Combining both expressions, the experimental rate of reaction may be
90 formulate as:

$$\frac{d\alpha}{dt} = k_0 \cdot e^{-E_a/RT} \cdot f(\alpha) \quad (4)$$

91 If the heating rate $\beta = dT/dt$, is included in the previous differential equation,
92 a new expression is obtained following a simple mathematical procedure which
93 can be seen in previous articles such as (Gil et al., 2010; Maia and de Morais,
94 2016):

$$\frac{d\alpha}{dT} = \frac{1}{\beta} \cdot k_0 \cdot e^{-E_a/RT} \cdot f(\alpha) \quad (5)$$

95 Therefore:

$$\frac{d\alpha}{f(\alpha)} = \frac{k_0}{\beta} \cdot dT \rightarrow \frac{d\alpha}{f(\alpha)} = \frac{k_0}{\beta} \cdot e^{-E_a/RT} dT \quad (6)$$

96 Then the following integral, that must be numerically solved, is obtained:

$$g(\alpha) = \int_0^\alpha \frac{d\alpha}{f(\alpha)} = \frac{k_0}{\beta} \int_{T_0}^T e^{-E_a/RT} dT = \frac{k_0 E_a}{\beta R} P\left(\frac{E_a}{RT}\right) \quad (7)$$

97 The function $P(E_a/RT)$ has no exact solution. Thus Eq. (7) can be solved by
98 numerical methods or approximations as can be seen in (White et al., 2011).

99 2.3.1. Model-free methods

100 The model-free methods allow for evaluating the Arrhenius parameters
101 without choosing the reaction order (Janković et al., 2009; Ravi et al., 2012).
102 These methods rest upon the isoconversional principle, which states that, at a
103 constant extent of conversion, the reaction rate is a function only of the
104 temperature (Vyazovkin and Sbirrazzuoli, 2006).

105 2.3.1.1. Flynn-Wall-Ozawa method

106 The solution of Eq. 7 using Doyle's approximation (Eq. 8) (Doyle, 1961), is
107 the Flynn-Wall-Ozawa (FWO) method (Eq. 9) (Flynn and Wall, 1966; Ozawa,
108 1965).

$$\ln \left[p \left(\frac{E_a}{RT} \right) \right] \approx -5.331 - 1.052 \frac{E_a}{RT} \quad (8)$$

109

$$\ln(\beta) = \ln \left(\frac{k_0 E_a}{Rg(\alpha)} \right) - 5.331 - 1.052 \frac{E_a}{RT} \quad (9)$$

110 Eq. 8 is valid only if $20 \leq E_a/RT \leq 60$ (Flynn and Wall, 1966). For a series of
 111 measurements with different heating rates at the fixed conversion value $\alpha=\alpha_i$,
 112 the plot of $\ln(\beta)$ vs. T^{-1} is a straight line with the slope $m = -1.052 E_a/R$.

113 2.3.1.2. Kissinger-Akahira-Sunose method

114 The Kissinger–Akahira–Sunose method (KAS) is obtained using Eq. 10,
 115 which is valid for $20 \leq E_a/RT \leq 50$ (Sbirrazzuoli et al., 2009).

$$p \left(\frac{E_a}{RT} \right) \approx \frac{e^{-E_a/RT}}{\left(\frac{E_a}{RT} \right)^2} \quad (10)$$

116 In KAS method, the relation between the temperature and heating rate is
 117 given by Eq. 11 (Kissinger, 1957).

$$\ln \left(\frac{\beta}{T^2} \right) = \ln \left(\frac{k_0 R}{E_a g(\alpha)} \right) - \frac{E_a}{RT} \quad (11)$$

118 The plot of the left side of Eq. 11 vs. T^{-1} at constant conversion value is a
 119 straight line with the slope $m=-E_a/R$.

120 2.3.2. Model-based methods. Coats-Redfern method.

121 Coats-Redfern method uses the asymptotic series expansion for
 122 approximating the exponential integral in Eq. 7 (Coats and Redfern, 1964).

$$\ln \left(\frac{g(\alpha)}{T^2} \right) = \ln \left(\frac{k_0 R}{\beta E_a} \left(1 - \frac{2RT}{E_a} \right) \right) - \frac{E_a}{RT} \quad (12)$$

123 If term $2RT/E_a$ is much lower than one it can be ignored, being the right
124 logarithmic term constant:

$$\ln\left(\frac{g(\alpha)}{T^2}\right) = \ln\left(\frac{k_0R}{\beta E_a}\right) - \frac{E_a}{RT} \quad (13)$$

125 Plotting the left side of Eq. 13 vs. T^{-1} , E_a and k_0 are obtained from the slope
126 and intercept respectively. Finally, the model that gives the best linear fit is
127 selected as the chosen model.

128 Several reaction model for $g(\alpha)$ and $f(\alpha)$ are listed at Table 1. With these
129 mathematical approach the kinetic triplet (decomposition model/reaction order,
130 pre-exponential Arrhenius factor and activation energy) can be obtained from
131 thermal decomposition data in a thermobalance scale (Bahng et al., 2009).

132

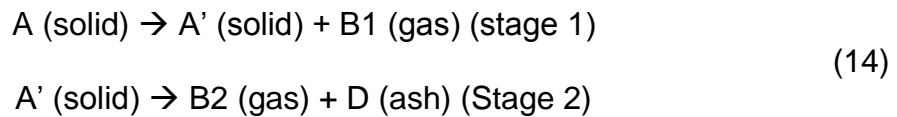
133 **3. RESULTS AND DISCUSSION**

134 **3.1 Parameters of DTG curves**

135 The characteristic parameters of DTG plots, which are presented in Fig. 1,
136 are shown in Table 2. As shown in Table 2, the combustion behaviour of
137 biomass samples studied is almost the same. There are two steps in
138 combustion of biomass, except for charcoal, lignin and cellulose which
139 presented only one step. The first step is related with combustion of cellulose
140 and hemicelluloses and the second one is related with the lignin fraction. All the
141 temperatures at maximum DTG (T_{peak}) of first stage are in the range between
142 249-353 °C, while the range for second stage is 414-627 °C. Temperature at
143 maximum weight loss rate of cellulose is 338 °C, which correspond to the first
144 stage while in the case of lignin this temperature is 548 °C belonging to second

145 stage. Thus, the first step is related with combustion of cellulose and
146 hemicelluloses and the second one is related with the lignin fraction.

147 Due to the data in Table 2, a two-stage reaction kinetic scheme has been
148 proposed in this article:



149

150 **3.2 Kinetic parameters**

151 The samples of biomass fuels were subjected to four heating ramps at 5, 10,
152 15 and 20 K/min. Obtained data was adjusted using previously described FWO,
153 KAS and Coats-Redfern method as well as numerically using Scientist software,
154 supposing first reaction order in all cases, which showed a really good
155 mathematical adjust. In that way, a four point straight line was obtained for each
156 conversion value from 10 to 90%, so a value of E_a is obtained for each
157 conversion (FWO and KAS methods) while only one heating ramp data (15
158 K/min) were necessary when Coats-Redfern or numerical methods were used
159 to obtain the kinetic triplet. The obtained kinetic data are shown at Table 3 and
160 Table 4 for Coats-Redfern and numerical solutions respectively.

161 When FWO or KAS method were applied, their particular assumptions were
162 only accomplished in the a range of conversion belonging to hemicelluloses and
163 cellulose fractions, while at the level of conversion for which the combustion of
164 lignin starts the assumptions were not accomplished (Fig 2). In Fig 2 the values
165 of E_a/RT for FWO and KAS methods are plotted against temperature as well as
166 dotted lines for maximum and minimum E_a/RT values for both methods. It can

167 be seen clearly that the assumptions of FWO and KAS methods were only
 168 accomplished in the first stage with E_a/RT values (red and green lines) between
 169 dotted lines while these coloured lines are below minimum dotted line when the
 170 second stage takes place. In commercial lignin and charcoal samples, the
 171 assumptions were not accomplished at all. Taking into account that charcoal is
 172 mainly composed of lignin, it is clear that FWO and KAS methods cannot
 173 predict activation energy of biomass combustion when lignin decomposition
 174 takes place.

175 Regarding Coats-Redfern and numerical method kinetic data, the activation
 176 energy in both stages is almost the same although it must be stated that in most
 177 samples this value is slightly higher in second stage. However, the activation
 178 energy of lignin is lower than cellulose, this is thought to be because of the
 179 synergistic effect. Since both stages are overlapped, in the Coats-Redfern
 180 method a γ -factor is used in order to link both stages:

$$\frac{d\alpha}{dT} = \gamma \left(\frac{d\alpha}{dT} \right)_{\text{stage 1}} + (1 - \gamma) \left(\frac{d\alpha}{dT} \right)_{\text{stage 2}} \quad (15)$$

181

182 The γ -factor is modelled as a modified Gompertz function (Collado et al.,
 183 2016):

$$\gamma = 1 - A \exp \left\{ - \exp \left(\frac{\mu e}{A} (T_c - T) + 1 \right) \right\} \quad (16)$$

184 Figures 3a and 3b show the simulations of the Coats-Redfern method. As it
 185 can be seen in Table 5, where the Gompertz parameters are shown, A values
 186 are close to 1 and T_c is the turning point between both stages, while μ values
 187 are related with the rate of change of the γ -factor.

188 **4. CONCLUSIONS**

189 There were determined the kinetic parameters (activation energy and the
190 pre-exponential factor of Arrhenius expression) for 28 biomass samples by
191 Coats-Redfern method. All of them showed good adjust to first global reaction
192 order. It was experimentally demonstrated that FWO and KAS method are not
193 suitable for getting the kinetic parameters of the combustion of biomass.

194

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210

211

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314 **TABLES**

315 Table 1. Solid state rate equations

316 Table 2. DTG data of biomass samples

317 Table 3. Kinetic parameters obtained by means of Coats-Redfern method.

318 Table 4. Kinetic parameters obtained by numerical solution.

319 Table 5. Gompertz model parameters of the biomass samples analysed

Table 1. Solid state rate equations

| Abbreviation | Reaction model | $f(\alpha)$ | $g(\alpha)$ |
|---|--------------------|--------------------------------------|---------------------------|
| Nucleation models | | | |
| P2 | Power Law | $2\alpha^{1/2}$ | $\alpha^{1/2}$ |
| P3 | Power Law | $3\alpha^{2/3}$ | $\alpha^{1/3}$ |
| P4 | Power Law | $4\alpha^{3/4}$ | $\alpha^{1/4}$ |
| A2 | Avrami-Erofe'ev | $2(1-\alpha)[- \ln(1-\alpha)]^{1/2}$ | $[- \ln(1-\alpha)]^{1/2}$ |
| A3 | Avrami-Erofe'ev | $3(1-\alpha)[- \ln(1-\alpha)]^{2/3}$ | $[- \ln(1-\alpha)]^{1/3}$ |
| A4 | Avrami-Erofe'ev | $4(1-\alpha)[- \ln(1-\alpha)]^{3/4}$ | $[- \ln(1-\alpha)]^{1/4}$ |
| Reaction orders and geometrical contractions | | | |
| F1 | First order | $1-\alpha$ | $-\ln(1-\alpha)$ |
| F2 | Second order | $(1-\alpha)^2$ | $(1-\alpha)^{-1}-1$ |
| F3 | Third order | $(1-\alpha)^3$ | $[(1-\alpha)^{-2}-1]/2$ |
| R2 | Contracting area | $2(1-\alpha)^{1/2}$ | $1-(1-\alpha)^{1/2}$ |
| R3 | Contracting volume | $3(1-\alpha)^{2/3}$ | $1-(1-\alpha)^{1/3}$ |

Table 2. DTG data of biomass samples

| Sample | First stage | | Second stage | |
|----------------------------------|------------------------|------------------------|------------------------|------------------------|
| | T _{peak} (°C) | Temperature range (°C) | T _{peak} (°C) | Temperature range (°C) |
| Cellulose | 338 | 300-360 | - | - |
| Lignin | - | - | 548 | 450-600 |
| Almond shell | 298 | 250-390 | 477 | 400-720 |
| Apple tree leaves | 311 | 220-350 | 414 | 410-600 |
| Beetroot pellets | 342 | 210-380 | 541 | 400-640 |
| Briquette | 343 | 260-400 | 509 | 410-550 |
| Charcoal | - | - | 490 | 400-900 |
| Chestnut tree chips | 335 | 260-370 | 473 | 400-520 |
| Cocoa bean husk | 312 | 225-350 | 627 | 425-634 |
| Coffee bean husk | 319 | 220-360 | 502 | 440-520 |
| Corn cob | 289 | 250-340 | 454 | 400-550 |
| Eucalyptus tree chips | 340 | 250-370 | 486 | 420-520 |
| Extracted olive pomace | 328 | 230-360 | 550 | 400-725 |
| Gorse | 339 | 250-390 | 560 | 450-570 |
| Grape seed flour | 340 | 255-375 | 546 | 400-775 |
| Miscanthus | 307 | 240-340 | 550 | 450-550 |
| Olive stone | 340 | 260-360 | 418 | 400-820 |
| Olive tree pruning | 342 | 250-375 | 469 | 430-570 |
| Pepper plant | 311 | 220-374 | 460 | 400-807 |
| Pine and pineapple leave pellets | 324 | 250-360 | 422 | 400-740 |
| Pine kernel shell | 249 | 270-370 | 515 | 400-820 |
| Pineapple leaf | 344 | 250-380 | 496 | 420-570 |
| Rice husk | 334 | 260-360 | 450 | 400-540 |
| Sainfoin | 301 | 230-330 | 456 | 390-522 |
| Scrubland pruning | 334 | 260-370 | 538 | 400-760 |
| Thistle | 345 | 240-400 | 473 | 420-550 |
| Vine shoot | 318 | 250-380 | 468 | 420-500 |
| Wheat straw | 312 | 260-360 | 543 | 420-650 |
| Wheat straw pellets | 300 | 230-365 | 458 | 400-528 |

Table 3. Kinetic parameters obtained by means of Coats-Redfern method.

| Sample | Stage 1 | | | Stage 2 | | |
|----------------------------------|----------|---------------|--------|----------|---------------|-------|
| | k_0 | E_a (J/mol) | R^2 | k_0 | E_a (J/mol) | R^2 |
| Cellulose | 9.47E+17 | 2.12E+05 | 0.997 | - | - | - |
| Lignin | - | - | - | 6.87E+03 | 6.95E+04 | 0.98 |
| Almond shell | 2.07E+03 | 4.82E+04 | 0.994 | 1.00E+00 | 1.71E+04 | 0.94 |
| Apple tree leaves | 3.54E+01 | 2.94E+04 | 0.997 | 2.65E+00 | 2.06E+04 | 0.996 |
| Beetroot pellets | 5.36E+00 | 2.16E+04 | 0.998 | 3.99E+00 | 2.32E+04 | 0.98 |
| Briquette | 4.65E+02 | 4.28E+04 | 0.997 | 2.24E+03 | 5.55E+04 | 0.96 |
| Charcoal | - | - | - | 9.17E-01 | 2.29E+04 | 0.98 |
| Chestnut tree chips | 1.35E+03 | 4.66E+04 | 0.998 | 2.83E+03 | 5.38E+04 | 0.98 |
| Cocoa bean husk | 2.86E+01 | 2.90E+04 | 0.995 | 6.28E-01 | 1.51E+04 | 0.99 |
| Coffee bean husk | 1.06E+02 | 3.46E+04 | 0.998 | 7.10E+03 | 6.25E+04 | 0.96 |
| Corn cob | 1.65E+07 | 8.69E+04 | 0.994 | 3.20E+00 | 1.95E+04 | 0.93 |
| Eucalyptus tree chips | 4.60E+02 | 4.18E+04 | 0.9995 | 1.03E+04 | 6.30E+04 | 0.98 |
| Extracted olive pomace | 5.96E+01 | 3.23E+04 | 0.993 | 5.08E-01 | 1.46E+04 | 0.92 |
| Gorse | 3.07E+01 | 3.07E+04 | 0.997 | 3.31E+02 | 4.71E+04 | 0.95 |
| Grape seed flour | 8.85E+00 | 2.56E+04 | 0.995 | 3.09E+02 | 5.70E+04 | 0.96 |
| Miscanthus | 2.56E+02 | 3.79E+04 | 0.996 | 6.76E+02 | 5.09E+04 | 0.97 |
| Olive stone | 1.37E+03 | 4.63E+04 | 0.98 | 7.33E+01 | 4.76E+04 | 0.91 |
| Olive tree pruning | 1.48E+02 | 3.64E+04 | 0.9991 | 2.26E+00 | 1.92E+04 | 0.92 |
| Pepper plant | 4.58E+00 | 2.14E+04 | 0.9993 | 7.02E+01 | 4.73E+04 | 0.95 |
| Pine and pineapple leave pellets | 1.05E+03 | 4.51E+04 | 0.994 | 1.09E-01 | 7.35E+03 | 0.97 |
| Pine kernel shell | 2.84E+02 | 4.05E+04 | 0.996 | 7.91E+01 | 4.81E+04 | 0.97 |
| Pineapple leaf | 1.31E+02 | 3.69E+04 | 0.997 | 5.33E+02 | 4.92E+04 | 0.95 |
| Rice husk | 7.31E+03 | 5.39E+04 | 0.9991 | 4.13E+01 | 3.28E+04 | 0.92 |
| Sainfoin | 1.64E+02 | 3.49E+04 | 0.996 | 1.88E+02 | 4.09E+04 | 0.995 |
| Scrubland pruning | 2.26E+01 | 2.90E+04 | 0.995 | 2.86E+00 | 2.09E+04 | 0.92 |
| Sorghum | 2.93E+03 | 4.99E+04 | 0.998 | 2.01E+00 | 1.81E+04 | 0.98 |
| Thistle | 9.64E+01 | 3.46E+04 | 0.998 | 5.61E+01 | 3.50E+04 | 0.99 |
| Vine shoot | 5.12E+03 | 5.16E+04 | 0.998 | 8.68E+02 | 4.82E+04 | 0.96 |
| Wheat straw | 1.93E+06 | 7.75E+04 | 0.96 | 4.13E+00 | 2.34E+04 | 0.92 |
| Wheat straw pellets | 1.35E+04 | 5.46E+04 | 0.995 | 1.51E+01 | 2.75E+04 | 0.96 |

Table 4. Kinetic parameters obtained by numerical solution.

| Sample | Stage 1 | | | Stage 2 | | |
|----------------------------------|----------|----------|----------|----------|----------|-------------|
| | k_0 | E_a | R^2 | k_0 | E_a | R^2 |
| Cellulose | 3.24E+10 | 1.26E+05 | 0.997 | - | - | - |
| Lignin | | | | 4.49E+05 | 9.73E+04 | 0.99993 |
| Almond shell | 2.97E+02 | 3.83E+04 | 0.9997 | 7.11E+01 | 4.36E+04 | 0.999996 |
| Apple tree leaves | 1.29E+02 | 3.42E+04 | 0.9998 | 2.57E+01 | 3.23E+04 | 0.999998 |
| Beetroot pellets | 3.26E+00 | 1.75E+04 | 0.999996 | 1.26E+03 | 6.04E+04 | 0.9999995 |
| Briquette | 1.98E+04 | 5.98E+04 | 0.99996 | 3.90E+09 | 1.48E+05 | 0.9999997 |
| Charcoal | | | | 1.09E+00 | 2.10E+04 | 0.9996 |
| Chestnut tree chips | 1.76E+05 | 6.88E+04 | 0.9998 | 3.01E+08 | 1.24E+05 | 0.99995 |
| Cocoa bean husk | 2.48E+02 | 3.77E+04 | 0.9998 | 9.87E+00 | 2.91E+04 | 0.999997 |
| Coffee bean husk | 9.03E+02 | 4.35E+04 | 0.999996 | 4.70E+10 | 1.62E+05 | 0.999997 |
| Corn cob | 3.99E+07 | 9.06E+04 | 0.998 | 1.30E+03 | 5.29E+04 | 0.999996 |
| Eucalyptus tree chips | 2.02E+03 | 4.79E+04 | 0.99995 | 3.69E+11 | 1.72E+05 | 0.9999997 |
| Extracted olive pomace | 2.04E+02 | 3.69E+04 | 0.9994 | 4.11E+01 | 4.11E+04 | 0.99998 |
| Gorse | 1.28E+03 | 4.72E+04 | 0.999995 | 3.64E+08 | 1.38E+05 | 0.999997 |
| Grape seed flour | 1.19E+02 | 3.64E+04 | 0.99991 | 5.80E+00 | 2.84E+04 | 0.99997 |
| Miscanthus | 3.11E+03 | 4.87E+04 | 0.9998 | 4.30E+07 | 1.22E+05 | 0.999998 |
| Olive stone | 2.00E+02 | 3.63E+04 | 0.9995 | 1.80E+00 | 2.09E+04 | 0.99998 |
| Olive tree pruning | 2.31E+03 | 4.85E+04 | 0.99995 | 2.15E+03 | 5.89E+04 | 0.999991 |
| Pepper plant | 2.10E+01 | 2.68E+04 | 0.999993 | 3.58E+11 | 2.37E+05 | 0.999999994 |
| Pine and pineapple leave pellets | 7.78E+04 | 6.46E+04 | 0.99995 | 1.20E+00 | 1.62E+04 | 0.999994 |
| Pine kernel shell | 7.07E+03 | 5.51E+04 | 0.99997 | 2.03E+02 | 5.66E+04 | 0.999998 |
| Pineapple leaf | 3.53E+03 | 5.15E+04 | 0.999995 | 3.13E+04 | 7.61E+04 | 0.9999991 |
| Rice husk | 1.57E+04 | 5.69E+04 | 0.99991 | 1.85E+04 | 6.95E+04 | 0.99997 |
| Sainfoin | 2.00E+03 | 4.53E+04 | 0.9998 | 2.11E+04 | 6.88E+04 | 0.999994 |
| Scrubland pruning | 4.09E+03 | 5.24E+04 | 0.99998 | 3.57E+03 | 6.21E+04 | 0.99998 |
| Sorghum | 1.09E+04 | 5.54E+04 | 0.9997 | 1.79E+01 | 2.81E+04 | 0.999980 |
| Thistle | 3.65E+03 | 5.08E+04 | 0.999991 | 2.35E+05 | 8.64E+04 | 0.999998 |
| Vine shoot | 3.24E+04 | 5.97E+04 | 0.99992 | 3.31E+10 | 1.54E+05 | 0.9999992 |
| Wheat straw | 2.59E+13 | 1.55E+05 | 0.9998 | 1.25E+01 | 3.06E+04 | 0.99997 |
| Wheat straw pellets | 6.25E+06 | 8.21E+04 | 0.99992 | 3.90E+04 | 1.54E+05 | 0.999998 |

328 Table 5. Gompertz model parameters of the biomass samples analysed.

| Sample | A | μ (K ⁻¹) | T _c (K) |
|----------------------------------|-------|--------------------------|--------------------|
| Almond shell | 0.999 | 0.016 | 597.9 |
| Apple tree leaves | 1.292 | 0.074 | 591.3 |
| Beetroot pellets | 0.852 | 0.029 | 638.8 |
| Briquette | 0.957 | 0.031 | 637.8 |
| Charcoal | - | - | - |
| Chestnut tree chips | 1.000 | 0.064 | 633.7 |
| Cocoa bean husk | 1.000 | 0.145 | 594.5 |
| Coffee bean husk | 0.879 | 0.032 | 606.9 |
| Corncob | 1.014 | 0.028 | 573.2 |
| Eucalyptus tree chips | 0.949 | 0.019 | 621.2 |
| Extracted olive pomace | 0.996 | 0.017 | 589.7 |
| Gorse | 0.976 | 0.012 | 603.6 |
| Grape seed flour | 1.372 | 0.018 | 603.2 |
| Miscanthus | 1.000 | 0.017 | 583.0 |
| Olive stone | 1.011 | 0.035 | 616.0 |
| Olive tree pruning | 1.016 | 0.023 | 605.2 |
| Pepper plant | 0.677 | 0.050 | 593.6 |
| Pine and pineapple leave pellets | 1.251 | 0.029 | 595.8 |
| Pine kernel shell | 1.000 | 0.011 | 595.2 |
| Pineapple leaf | 0.988 | 0.021 | 613.0 |
| Rice husk | 1.002 | 0.029 | 606.9 |
| Sainfoin | 1.509 | 0.056 | 586.2 |
| Scrubland pruning | 1.031 | 0.019 | 600.4 |
| Sorghum | 1.000 | 0.052 | 600.5 |
| Thistle | 1.944 | 0.016 | 612.1 |
| Vine shoot | 0.991 | 0.018 | 593.9 |
| Wheat straw | 1.000 | 0.068 | 588.7 |
| Wheat straw pellets | 0.976 | 0.023 | 570.8 |

329

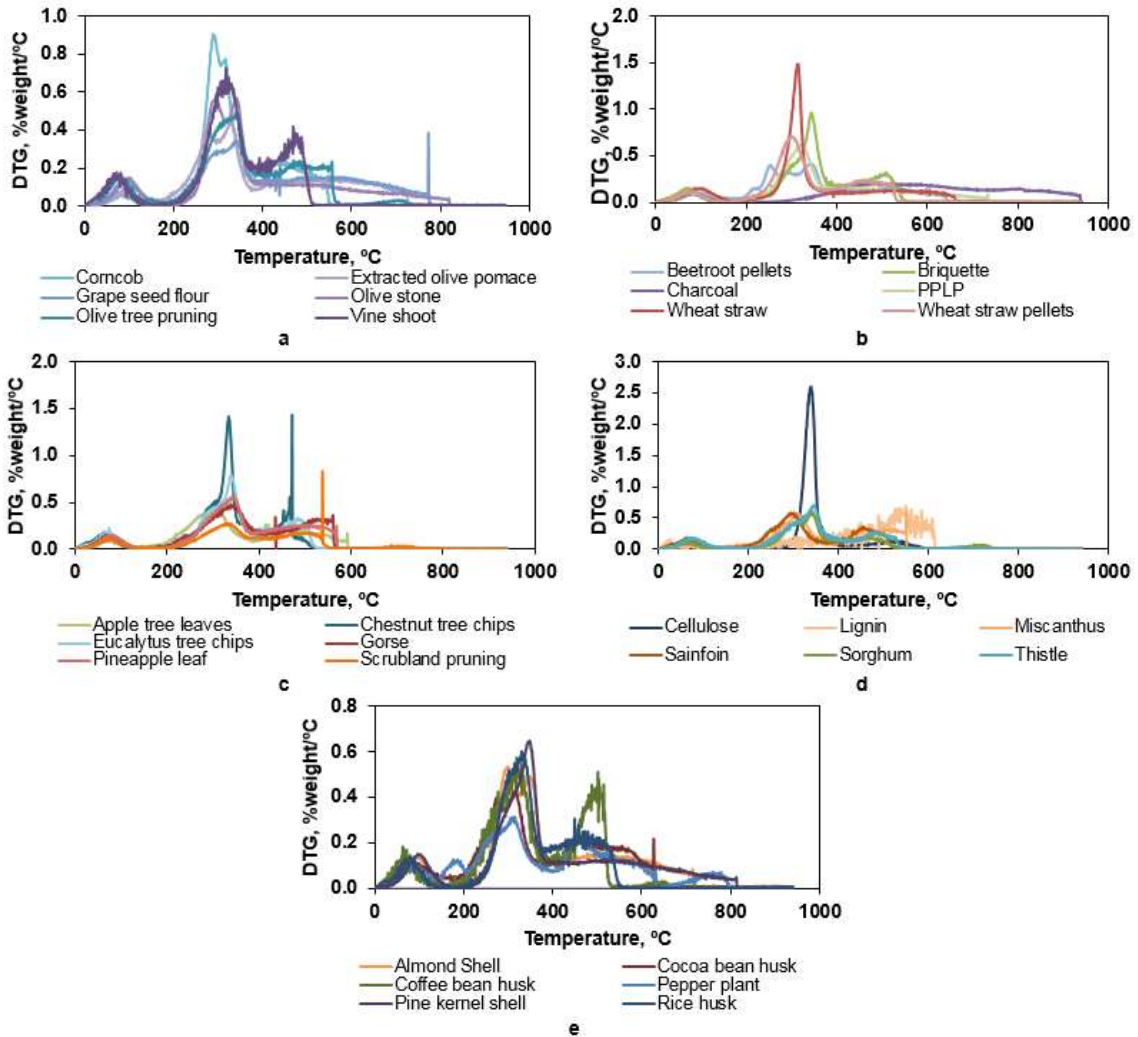
330 **FIGURE CAPTIONS**

331 Fig. 1. DTG curves of the combustion process ($\beta = 15$ K/min) of biomass
332 samples analysed. (PPLP in b is the pine and pineapple leave pellet sample).

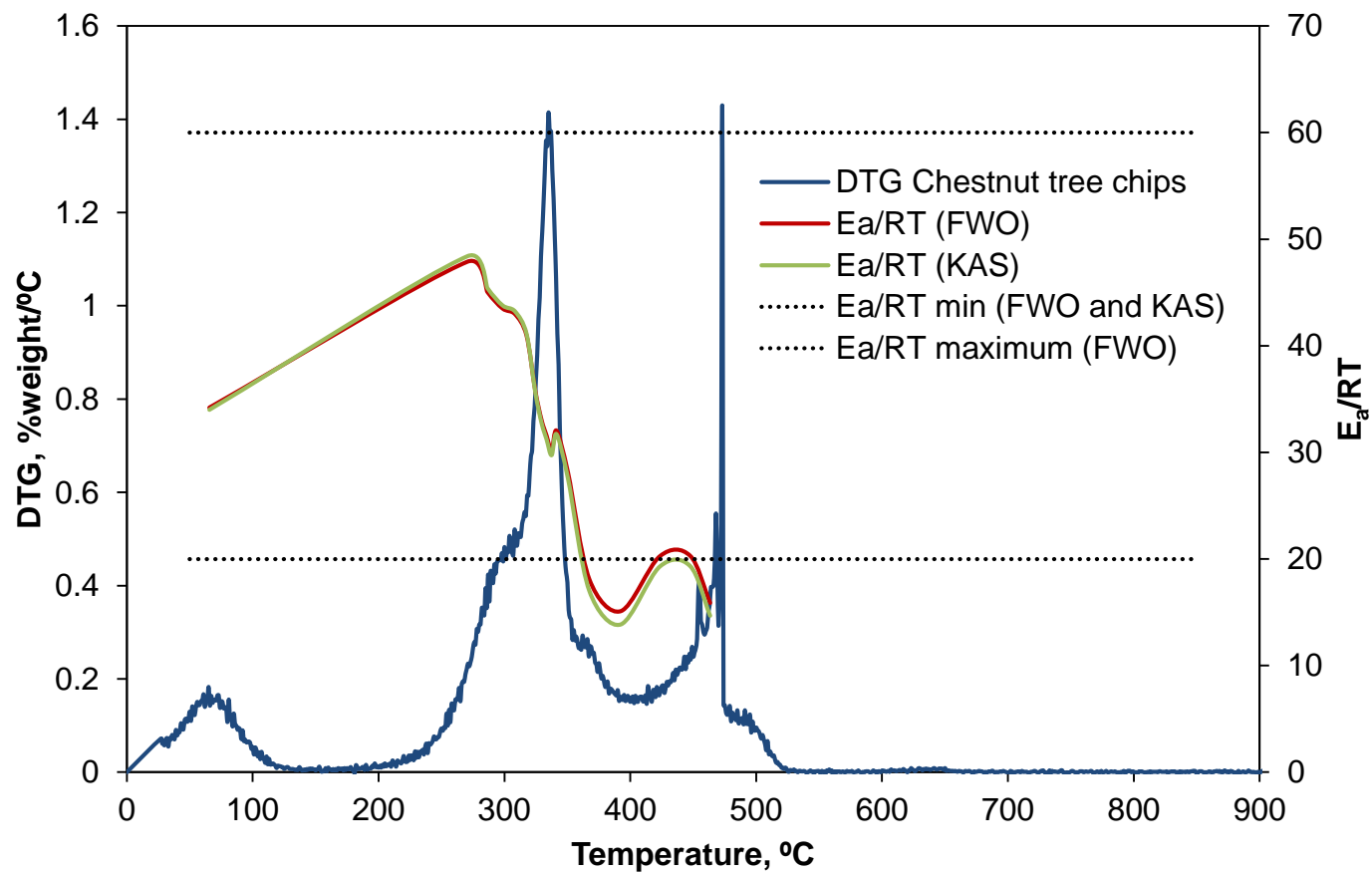
333 Fig. 2. Matches between DTG and E_a values in FWO and KAS methods.

334 Fig. 3a. Simulations for CR method; 1. Almond shell; 2. Apple tree leaves; 3.
335 Beetroot pellets; 4. Briquette; 5. Charcoal; 6. Chestnut tree chips; 7. Cocoa
336 bean husk; 8. Coffee bean husk; 9. Corncob; 10. Eucalyptus tree chips; 11.
337 Extracted olive pomace; 12. Gorse; 13. Grape seed flour; 14. Miscanthus; 15.
338 Olive stone; 16. Olive tree pruning.

339 Fig. 3b. Simulations for CR method; 17. Pepper plant; 18. Pine and pineapple
340 leave pellets; 19. Pine kernel shell; 20. Pineapple leaf; 21. Rice husk; 22.
341 Sainfoin; 23. Scrubland pruning; 24. Sorghum; 25. Thistle; 26. Vine shoot; 27.
342 Wheat straw; 28. Wheat straw pellets.

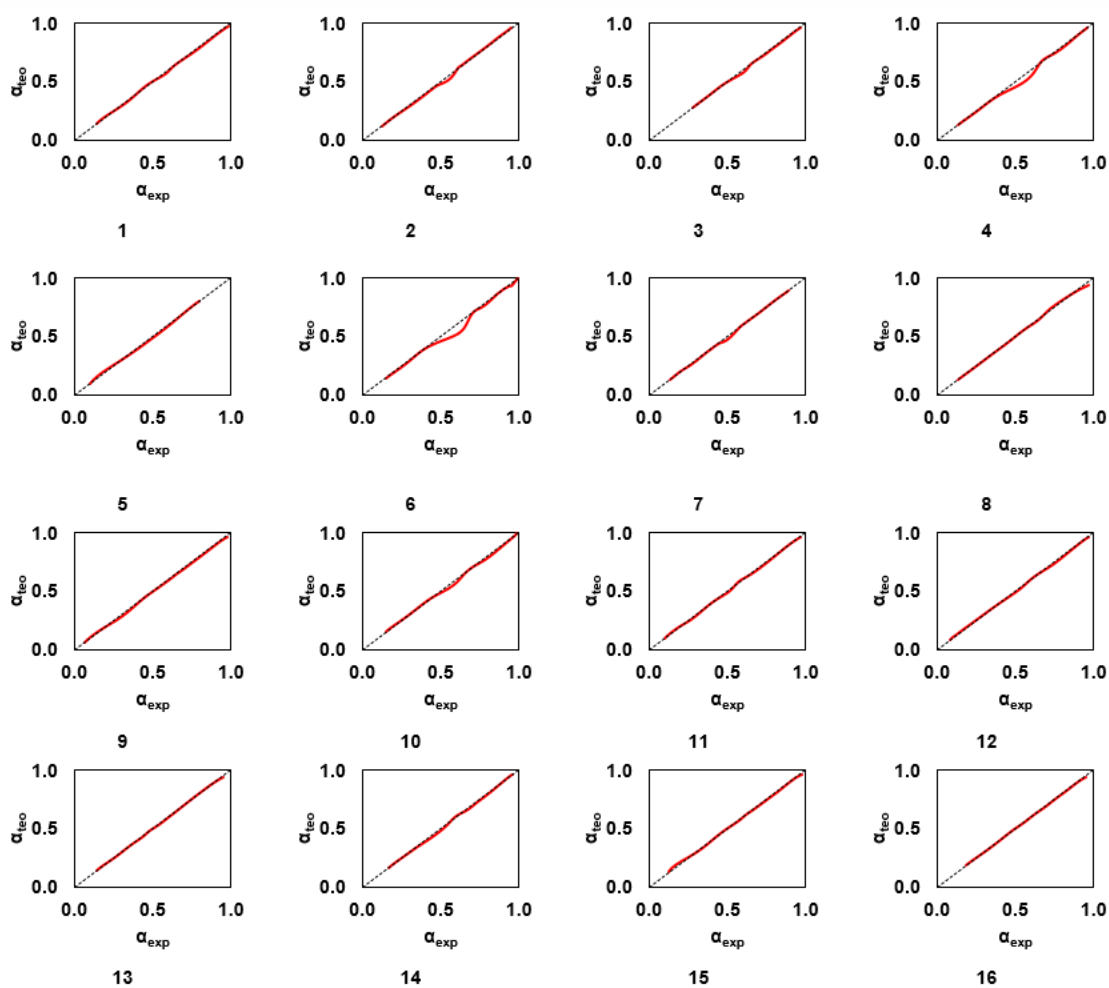


343
 344 Fig. 1. DTG curves of the combustion process ($\beta = 15$ K/min) of biomass
 345 samples analysed. (PPLP in b is the pine and pineapple leaf pellet sample)



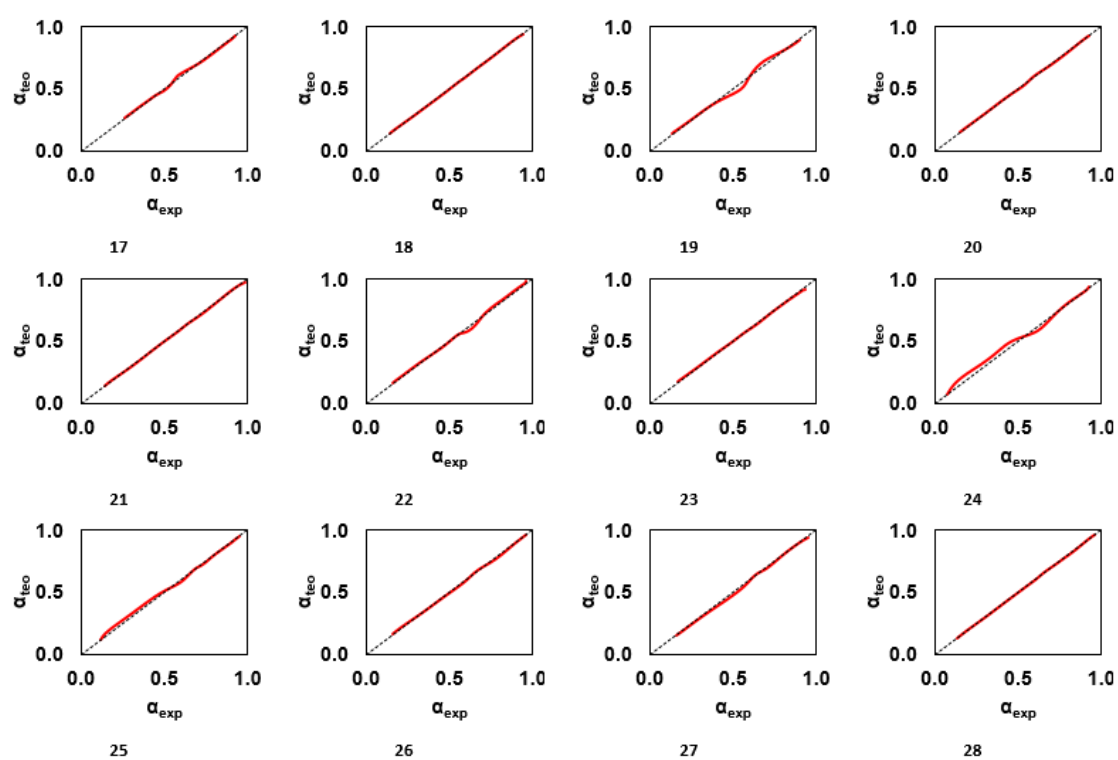
346

347 Fig 2. Matches between DTG and Ea values in FWO and KAS methods



348

349 Fig. 3a. Simulations for CR method; 1. Almond shell; 2. Apple tree leaves; 3.
 350 Beetroot pellets; 4. Briquette; 5. Charcoal; 6. Chestnut tree chips; 7. Cocoa
 351 bean husk; 8. Coffee bean husk; 9. Corncob; 10. Eucalyptus tree chips; 11.
 352 Extracted olive pomace; 12. Gorse; 13. Grape seed flour; 14. Miscanthus; 15.
 353 Olive stone; 16. Olive tree pruning.



354

355 Fig. 3b. Simulations for CR method; 17. Pepper plant; 18. Pine and pineapple
 356 leave pellets; 19. Pine kernel shell; 20. Pineapple leaf; 21. Rice husk; 22.
 357 Sainfoin; 23. Scrubland pruning; 24. Sorghum; 25. Thistle; 26. Vine shoot; 27.
 358 Wheat straw; 28. Wheat straw pellets.