

# The role of reaction kinetics and mass transfer on the selective catalytic reduction of NO with NH<sub>3</sub> in monolithic reactors

Emilio Muñoz, Pablo Marín, Salvador Ordóñez\*, Fernando V. Díez

Department of Chemical and Environmental Engineering, University of Oviedo, Facultad de Química, Julián Clavería 8, 33006 Oviedo, SPAIN

## Abstract

### Background

Environmental regulations are moving to a tighter control of NO<sub>x</sub> emissions produced at both stationary and mobile sources. Selective catalytic reduction (SCR) of NO<sub>x</sub> with NH<sub>3</sub> is an efficient treatment technique capable of operating at high gas flow rates (e.g. using monolithic catalysts) and a wide range of NO concentrations. The aim of this work is to provide guidelines for designing this kind of reactors taking into account both intrinsic kinetics and mass transfer.

### Results

The experiments have been done in lab-scale (0.5 g) and bench-scale (430 g) reactors operating at different conditions: temperature (150-320°C), space velocity (WHSV 5360-16100 mol h<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup>), oxygen concentration (0-21%) and NH<sub>3</sub>/NO ratio (0.2-1.2). Temperature has a great influence in the reaction rate, and at least 300°C is required at a WHSV of 16100 mol h<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup>. Oxygen is required in the feed because participates as reactant in the SCR.

### Conclusions

Data obtained in the lab-scale reactor in the absence of mass transfer limitations have been used to fit an intrinsic kinetic model of the SCR reaction. A more complex model has been

1 used for the bench-scale reactor accounting for reaction kinetic and mass transfer (internal  
2 effectiveness factor was determined) in the monolithic catalyst.

3

#### 4 **Key words:**

5 NOx emissions, air pollution control, monolithic catalyst, transient methods, mass transfer in  
6 monolithic reactors.

7

#### 8 **Notation**

##### 9 *List of symbols*

10	a	specific surface area ( $\text{m}^2 \text{m}_{\text{bed}}^{-3}$ )
11	c	gas mole concentration ( $\text{mol m}^{-3}$ )
12	$D_h$	hydraulic diameter (m)
13	$D_{\text{im}}$	mixture molecular diffusion coefficient ( $\text{m}^2 \text{s}^{-1}$ )
14	$D_{\text{iz}}$	effective axial dispersion coefficient ( $\text{m}^2 \text{s}^{-1}$ )
15	$E_a$	activation energy ( $\text{J mol}^{-1}$ )
16	k	kinetic constant ( $\text{m}^3 \text{mol}^{-1} \text{s}^{-1}$ or $\text{s}^{-1}$ )
17	$K_g$	mass transfer coefficient ( $\text{m s}^{-1}$ )
18	n	catalyst ammonia adsorption capacity ( $\text{mol kg}_{\text{cat}}^{-1}$ )
19	$Q_g$	gas flow rate ( $\text{m}^3 \text{s}^{-1}$ )
20	r	reaction rate ( $\text{mol kg}_{\text{cat}}^{-1} \text{s}^{-1}$ )
21	Sh	Sherwood number (-)
22	t	time (s)
23	T	temperature (K)
24	$t_{\text{sw}}$	switching time (s)
25	v	gas interstitial velocity ( $\text{m s}^{-1}$ )
26	w	relative weight of catalyst (-)
27	W	total weight of catalyst (kg)
28	z	spatial coordinate (m)
29		bed porosity (-)
30	$\eta_{\text{int}}$	internal effectiveness factor
31	$\theta$	solid fraction of adsorbed specie (-)
32	$\rho_c$	catalyst density ( $\text{kg m}^{-3}$ )

33

##### 34 *Sub indexes and super indexes*

35 in inlet

- 1 ads adsorption
- 2 red reduction
- 3 s catalyst surface

4

5 *Acronyms*

- 6 BAT best available techniques
- 7 FIC flow indicator and controller
- 8 PI pressure indicator
- 9 SCR selective catalytic reduction
- 10 SNCR selective non-catalytic reduction
- 11 TIC temperature indicator and controller
- 12 WHSV gas-hourly space velocity ( $\text{mol h}^{-1} \text{kg}_{\text{cat}}^{-1}$ )

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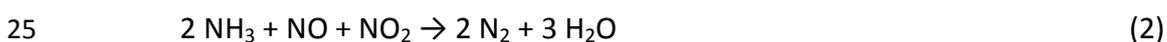
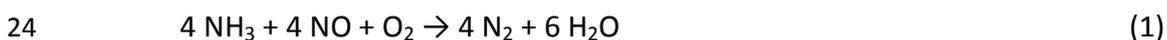
# 1 Introduction

2 Nitric oxides (NO<sub>x</sub>), including nitrogen oxide (NO), nitrogen dioxide (NO<sub>2</sub>) and nitrous oxide  
3 (N<sub>2</sub>O), are emitted to the atmosphere mainly as a result of transportation and industrial  
4 processes. They are among the most dangerous air pollutants, as they contribute to the  
5 greenhouse effect, participate in photochemical reactions that cause acid rain and the  
6 formation of troposphere ozone ('photochemical smog'), and have an important role in lakes  
7 and rivers eutrophication. In addition, they are harmful to human health, as they can  
8 damage the respiratory system.<sup>1-3</sup>

9 Due to their quantitative importance and harmful nature, NO<sub>x</sub> abatement has been studied  
10 widely during the last decades,<sup>4-7</sup> and their emissions in industrialized countries are  
11 restrictively regulated, e.g. in the UE by Directive 2001/81/EC.

12 NO<sub>x</sub> emissions can be reduced by means of primary or secondary measures. Primary  
13 measures decrease NO<sub>x</sub> formation, e.g. by controlling temperature, excess air or mixing in  
14 combustion process, while secondary emissions separate or destroy NO<sub>x</sub> from effluents.  
15 Selective Catalytic Reduction (SCR) and Selective Non Catalytic Reduction (SNCR) are  
16 secondary processes considered in the EU as Best Available Techniques (BAT) for treating  
17 NO<sub>x</sub> in emissions from large stationary sources, such as large combustion plants.<sup>8</sup> NO<sub>x</sub>  
18 selective reduction processes are based on the reaction of NO<sub>x</sub> with a reducing agent  
19 (ammonia or urea), forming molecular nitrogen and water. When performed in the presence  
20 of a catalyst (SCR), the process takes place at lower temperature, is able of working with  
21 load variations or variable fuel quality, and is substantially more efficient than when the  
22 process is non-catalytic (SNCR). On the other hand, the inversion required for SNCR is lower.

23 The main reactions taking place for ammonia, the most common SCR reducing agent, are:



1 Since NO/NO<sub>2</sub> ratio in NO<sub>x</sub> emissions is larger than 10, the first reaction, called 'standard  
2 SCR', is largely the most important. When temperature is low, the third reaction, called 'fast-  
3 SCR', should be also taken into consideration.

4 Different catalysts have been used for ammonia SCR, including noble metals, metal oxides  
5 and zeolites,<sup>3, 9-11</sup> operating temperature being an important factor for catalyst selection. For  
6 high temperatures (345-590°C), zeolites are more durable, active and SO<sub>2</sub> tolerant.<sup>12</sup>  
7 Operating at lower temperature (typically 150-300°C), allows saving fuel used for re-heating  
8 the flue gas in some installations. Noble metals have shown better performance at low  
9 temperature, but are expensive, **the temperature operation range is narrow and present low**  
10 **sulphur tolerance. Pd and Ag are both noble metals that present good performance for the**  
11 **SCR reaction.<sup>12, 13</sup> Pd is usually supported on perovskites or zirconia. Ag supported on Al<sub>2</sub>O<sub>3</sub>**  
12 **shows high efficiency, particularly when using hydrocarbons.**

13 Metal oxide catalysts (oxides of copper, iron or vanadium, either unsupported or supported  
14 on alumina, silica or titania)<sup>2, 8</sup> are cheaper, and work well in the typical temperature range  
15 of industrial applications. One of the most common industrial SCR catalyst types consists on  
16 vanadium oxide, promoted by MoO<sub>3</sub> or WO<sub>3</sub>, and supported on titania (in the anatase form).  
17 WO<sub>3</sub>-V<sub>2</sub>O<sub>5</sub>/TiO<sub>2</sub> catalysts show tolerance to SO<sub>2</sub> poisoning and provide high NO<sub>x</sub> conversion,  
18 the TiO<sub>2</sub> support providing high surface area and increased catalyst activity.<sup>8</sup> **In the last**  
19 **years, the research in this field has focused in the development of vanadium-free catalysts**  
20 **with high activity, selectivity and stability.<sup>12, 13</sup> Fe containing mixed oxides and Fe-exchanges**  
21 **zeolites were found to present high activity. The selection of an adequate support is critical**  
22 **for the activity and stability of the catalyst.<sup>12, 14</sup> Under rich oxygen conditions, Cu/ZSM-5 was**  
23 **found to present reduction capability using hydrocarbons.<sup>13, 15</sup>**

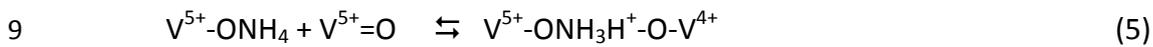
24 SCR catalysts are generally used as structured beds, as this type of bed produces lower  
25 pressure drop through the reactor, helps to keep process conditions uniform along the bed,  
26 and presents higher resistance to attrition and lower tendency to fly ash plugging. **A recent**  
27 **review about the catalyst and reactor configuration is presented by Cheng et al.<sup>16</sup>**

28 Several mechanisms have been proposed for ammonia SCR on vanadia catalysts, including  
29 Langmuir-Hinsewood, Elay-Rideal and Mars Van Krevelen.<sup>17-23</sup> Most researchers have found  
30 that Elay-Rideal mechanisms fit better experimental results. Such models suppose that in

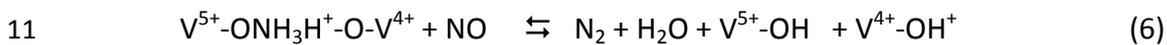
1 one step of the reaction mechanism, NO from the gas phase reacts with chemisorbed  
 2 ammonia, but published works differ on the nature of the involved active sites and reaction  
 3 intermediates.<sup>24-26</sup> Topsoe et al.<sup>27, 28</sup> observed in FTIR studies that, while at reaction  
 4 conditions NO adsorbed is negligible, ammonia adsorbs in large amounts on both Lewis and  
 5 Bronsted acid sites. Based on these studies, they proposed a mechanism according to which  
 6 ammonia adsorbs in equilibrium on  $V^{5+}$ -OH sites:



8 Adsorbed ammonia is activated by adjacent  $V^{5+}=\text{O}$  sites:



10 Activated ammonia reacts with NO:



12 And finally, the active sites regenerate:



15 The kinetics of the ammonia SCR on vanadium catalysts has been widely studied in the  
 16 literature, using equations either derived from reaction mechanisms or empirical.<sup>22, 24, 26</sup>

17 The aim of this work is to characterize the kinetics of ammonia SCR over a commercial  
 18 monolithic metal oxide (vanadium on titania) catalyst, in order to get a comprehensive  
 19 kinetic model adequate for simulating and optimizing the operation of steady and, specially,  
 20 un-steady state SCR reactors. Firstly, a parametric study is carried out to determine the most  
 21 important variables affecting the reaction kinetics. Then, an intrinsic kinetic model is  
 22 proposed and fitted to lab-scale experiments. Finally, a model for the commercial monolith  
 23 that takes into account the different mass transfer steps is tested and fitted to bench-scale  
 24 experiments.

25

## 1 **Methodology**

### 2 **Materials**

3 High purity gaseous reactants ( $N_2$ , 2.5 % vol.  $NH_3$  in nitrogen and 2.5 % vol. NO in nitrogen)  
4 were provided by PRAXAIR, and air by a compressor provided with a filter to separate  
5 humidity.

6 The catalyst used is a commercial DeNOx cordierite monolith, based on metal oxides, kindly  
7 supplied by ARGILLON with square channels and 64 cpsi of cell density. The main  
8 characteristics of the monolith, measured photographically, are: channel size  $2.7 \cdot 10^{-3}$  m, wall  
9 thickness  $4.7 \cdot 10^{-4}$  m, washcoating thickness  $9.6 \cdot 10^{-5}$  m. The bed porosity of the monolith  
10 block was calculated to be 73%. The solid density of the catalyst was experimentally  
11 determined to be  $2500 \text{ kg m}^{-3}$ .

12

### 13 **Lab-scale fixed-bed reactor**

14 The lab-scale fixed-bed reactor has been used to study the kinetics of the catalytic reaction  
15 in absence of diffusional limitations, e.g. using the catalyst ground to a small particle size.  
16 The reactor consists of a stainless steel tube of 9 mm inside diameter and 440 mm length. A  
17 weight of 0.5 g of catalyst, ground and sieved to 250-355  $\mu\text{m}$ , is mixed with 1 g of 355-710  
18  $\mu\text{m}$  glass particles and introduced inside the tube. The bed is set in position using stainless  
19 steel foil. The geometry of this bed is adequate to minimize axial dispersion and channelling,  
20 bed length/particle diameter =  $54 > 50$  and bed diameter/particle diameter =  $30 > 10$ ,  
21 respectively. Hence, a gas flow pattern close to plug flow may be achieved inside the reactor.  
22 Upstream the catalytic fixed-bed, the reactor tube is filled with 1 mm glass spheres to ensure  
23 a uniform pre-heating of the gas feed. The reactor temperature was controlled by an electric  
24 furnace and an electronic temperature controller that used the temperature measured by a  
25 thermocouple placed inside the reactor as set point. The small reactor diameter and  
26 catalytic bed length allowed assuming isothermal operation and negligible radial  
27 temperature profiles.

28 The reactor feed is prepared by mixing streams from the ammonia and NO cylinders with air  
29 or nitrogen in adequate proportions. The gas flow is measured and controlled by

1 BRONKHORST mass-flow controllers. The concentration of the reactor influent and effluent  
2 are analysed using a quadrupole mass spectrometer, PFEIFFER VACUUM OMNISTAR. This  
3 device is capable of analysing nitrogen monoxide and ammonia every few seconds. For each  
4 experiment, the device is re-calibrated to ensure reliable quantitative measurements.

5

## 1 **Bench-scale fixed-bed reactor**

2 The bench-scale fixed-bed reactor allows the study of the reaction using the catalyst in the  
3 commercial monolithic shape. The reactor consists of a stainless steel flanged tube of 57 mm  
4 inside diameter and 450 mm length. A piece of monolith 250 mm long (430 g weight) was  
5 cut to exactly fit inside the reactor. The monolith is maintained in place by means of a holey  
6 stainless steel support. Upstream the monolith inside the reactor tube, a bed of 4 mm glass  
7 spheres is used to obtain a feed of uniform temperature. The feed is heated up to the  
8 operating temperature outside the reactor in an electrically-heated compact heat  
9 exchanger. The temperature of the gas inside the reactor is measured before and after the  
10 monolith. The reactor tube is housed in the middle of an electrically-heated furnace that is  
11 responsible of achieving isothermal conditions. This is done by means of temperature  
12 controllers that use the temperature measurements of the reactor inside to exert the  
13 control action.

14 The preparation of the feed gas mixture and the analysis of the gases are carried out in the  
15 same way as in the lab-scale reactor.

16 A scheme of the experimental units is shown in Figure 1.

17

## 18 **Modelling**

19 The aim of the modelling is to provide an appropriate model of the reactor capable of  
20 predicting the dynamics of outlet concentrations. A 1D heterogeneous dynamic model has  
21 been used. The model is heterogeneous, which means that accounts separately for the gas  
22 and solid phases by means of the corresponding species mass balances. This allows the  
23 prediction of the dynamics of the ammonia adsorbed on the catalyst.<sup>29</sup>

24 The model of the lab-scale fixed-bed reactor is shown in Table 1. This model is composed by  
25 accumulation, convection and (intrinsic) reaction terms. The reaction mechanism assumed in  
26 this work is a simplification of the one presented by Topsoe and Dumesic, in which only the  
27 adsorption of ammonia and adsorbed ammonia reaction with NO are supposed to be  
28 kinetically relevant (equations 4 and 6).<sup>28, 29</sup> Additionally, ammonia reaction with NO is

1 assumed to be irreversible. For the ammonia adsorption, a Temkin-type isotherm with zero  
2 activation energy is supposed. As explained in the previous section, the gas flow pattern of  
3 this reactor is close to plug flow, so no axial dispersion term is required. Moreover, the  
4 catalyst was ground to small particles, so that diffusion limitations can be neglected.

5 The bench-scale fixed-bed reactor is modelled with the same type of model, Table 2, formed  
6 by accumulation, convection, dispersion and mass transfer terms. In this case, the gas flow  
7 through the monolithic catalyst cannot be considered to follow a plug-flow pattern, so axial  
8 dispersion terms are included. Dispersion coefficients are calculated using a correlation  
9 specific for monolith catalysts,<sup>30</sup> .

10 An issue that should be considered carefully in the modelling of monolithic catalysts is mass  
11 transfer. Gas to solid surface mass transfer is accounted for by means of the film theory  
12 using mass transfer coefficients, , where Sherwood number, , is 2.977  
13 for square monolithic channels at isothermal conditions.<sup>30</sup> The specific surface is calculated  
14 from geometrical considerations using the hydraulic diameter of the monolith, .  
15 The interphase mass balances correlate gas to solid surface mass transfer and reaction  
16 terms. Additionally, mass transfer inside the monolith washcoating is modelled using  
17 internal effectiveness factor. This parameter, which depends on the textural properties of  
18 the washcoating, the intrinsic kinetics and the operating conditions, will be fitted to the  
19 experimental data.<sup>31</sup>

20 Both reactor models, lab-scale and bench-scale, are formed by a set of partial differential  
21 and algebraic equations. The models are solved by the 'method of lines', which consists of  
22 the approximation of the spatial derivatives (convection and dispersion terms) by finite  
23 differences in a grid of 400 points (this value was found to be high enough to obtain grid-  
24 independent solution). The resulting set of ordinary differential and algebraic equations is  
25 solved using the MATLAB function ode15s, especially suited for stiff problems. The whole  
26 problem is formulated in a code written in MATLAB.<sup>32</sup>

27 The fitting of model parameters has been done using the least-square technique, based on  
28 the minimization of the sum of the square residuals. The problem has been solved in  
29 MATLAB with the help of the lsqcurvefit function, using a trust-region-reflective algorithm.

# 1 Results and discussion

## 2 Parametric study of the SCR kinetics

3 The aim of this section is to conduct a systematic study of the main variables affecting the  
4 SCR reaction kinetics. Kinetic parameters have been measured by the transient response  
5 method.<sup>4-6</sup> The following variables were selected after preliminary works: temperature,  
6 oxygen concentration and NH<sub>3</sub>/NO ratio.

7 Experiments consisted of measuring the evolution with time of the reactor effluent  
8 composition for different changes in the inlet composition, at constant flow rate and  
9 temperature. The experiments have been carried out in the lab-scale fixed-bed reactor  
10 described in the methodology section. Before all the experiments, the catalyst was saturated  
11 with ammonia at the corresponding temperature by flowing air with 500 ppm NH<sub>3</sub>. At t = 0,  
12 this stream was substituted by the corresponding to each experiment.

### 13 *Influence of temperature*

14 Temperature is one of the main operating variables affecting the performance of the SCR  
15 reaction. This variable was studied by feeding to the reactor, with the catalyst previously  
16 saturated with ammonia, a stream containing of 500 ppm NO and NH<sub>3</sub> in air. The flow rate  
17 was 3 L min<sup>-1</sup> n.t.p. (WHSV = 16100 mol h<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup>) and experiments were isothermal in the  
18 temperature range 150-320°C. After the transient, the new steady state was achieved in 3-4  
19 min in all the tests. Figure 2 shows the transient of NO and NH<sub>3</sub> outlet concentrations.

20 The transient behaviour of NO and NH<sub>3</sub> outlet concentrations are strictly related to each  
21 other. Thus, the introduction of NO produces a marked peak in the measured NH<sub>3</sub> exit  
22 concentration. This can be caused by wrong signal from the mass detector when the inlet  
23 stream is changed, by NH<sub>3</sub> desorption from the catalyst, or by both. After the maximum,  
24 ammonia concentration goes down to the corresponding steady state value. NO  
25 concentration rises steadily at low temperatures (150-190°C), whereas at high temperatures  
26 (220-320°C) exhibits a small maximum before going down to the steady state value.

27 The influence of temperature in the steady state NO conversion can be examined in Figure  
28 3a. Conversion is lower than 60% below 200°C, so operation at these conditions is not  
29 interesting from an industrial point of view. For temperatures above 300°C, the reaction of

1 NH<sub>3</sub> oxidation becomes important. This causes a reduction in NH<sub>3</sub> concentration and affects  
2 NO conversion, which actually decreases at higher temperature, as reported elsewhere.<sup>33, 34</sup>

3

#### 4 *Influence of oxygen concentration*

5 The role of oxygen is crucial in the SCR reaction, as it participates in the stoichiometric  
6 equation as reactant, it is always present in these emissions, and it competes as oxidant  
7 reactant with the NO. In the most accepted mechanism for this reaction, oxygen is  
8 responsible of re-oxidizing the catalyst active sites.<sup>21, 28</sup> In this work, the effect of oxygen in  
9 the performance of the reaction is assessed by varying the oxygen concentration (0, 0.08  
10 and 0.21 mole fraction), while maintaining constant the other variables: 250°C, inlet  
11 concentrations 286 ppm NH<sub>3</sub>, 500 ppm NO and balance nitrogen, and flow rate 2 L min<sup>-1</sup>  
12 n.t.p. (WHSV = 10700 mol h<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup>). The transients for NO and NH<sub>3</sub> concentrations are  
13 depicted in Figure 4. The steady state NO conversions obtained for the different oxygen  
14 concentrations are shown in Figure 3b. This plot corroborates the role of oxygen in this  
15 reaction.<sup>35</sup> When there is no oxygen in the feed, steady state conversion falls to zero, and at  
16 conditions of excess oxygen (> 8 %), the concentration of oxygen does not affect steady state  
17 NO conversion.

18 The unsteady state behaviour observed in this set of experiments is very useful to explain  
19 the mechanism of this reaction. In all cases, NO concentration increases steadily up to the  
20 steady state value, achieved after 8-10 minutes. The experiments with 8% and 21% oxygen  
21 present similar behaviour with some differences. Thus, the presence of a higher oxygen  
22 concentration delays the increase of NO outlet concentration. In the experiment with 8% of  
23 oxygen, NH<sub>3</sub> exit concentration falls after the peak, which means a faster decrease in the  
24 NH<sub>3</sub> catalyst surface coverage. It is well known that adsorbed NH<sub>3</sub> has a great impact on the  
25 reaction rate.<sup>10, 28</sup> For this reason, the premature decrease in adsorbed NH<sub>3</sub> would cause the  
26 observed increase on NO outlet concentration. It can be noted that for the test with 21% of  
27 oxygen the amount of NO reacted and the amount of NH<sub>3</sub> desorbed (NH<sub>3</sub> spill) are both  
28 higher than for the experiment with 8% of oxygen. This means that a higher amount of NH<sub>3</sub>  
29 was adsorbed during the saturation stage of the experiment with 21% of oxygen. More  
30 adsorbed NH<sub>3</sub> means high NO conversion for more time and also a higher NH<sub>3</sub> spill.

1 As in the experiments of the previous section, when NO is fed to the reactor, a peak in NH<sub>3</sub>  
2 outlet concentration is observed, followed by a marked decrease. When no oxygen is fed to  
3 the reactor, the dynamics shown in Figure 4b is more complex, and can be explained based  
4 on the reaction mechanism. After the ammonia spill, reaction proceeds on the oxidized  
5 catalyst active sites, but the lack of oxygen in the gas phase avoids re-oxidation of the  
6 reduced catalyst active sites so, as the catalyst is depleted of oxidized active sites, the  
7 reaction rate decreases and eventually drops to 0 (NO concentration rises to the feed value,  
8 t = 4-6 min). However, the catalyst is still able of adsorbing NH<sub>3</sub> from the gas phase, causing  
9 the observed decrease in the NH<sub>3</sub> outlet concentration (t = 2-5 min). Finally, when the  
10 catalyst is saturated, NH<sub>3</sub> exit concentration increases again up to the feed value (t > 6 min).  
11 The dynamics of NH<sub>3</sub> concentration for the experiments with 0% and 21% of oxygen are  
12 similar, but as explained the consequences of this behaviour are different. At 21% oxygen,  
13 NH<sub>3</sub> is reacting with NO, whereas at 0% oxygen is adsorbing in the catalyst.

14

#### 15 *Influence of NH<sub>3</sub>/NO ratio*

16 The NH<sub>3</sub>/NO ratio is an important operating variable in industrial scale reactors, which must  
17 be adjusted carefully to avoid slips of un-reacted NH<sub>3</sub>. The stoichiometric NH<sub>3</sub>/NO ratio for  
18 the SCR reaction is 1, but depending on the operating conditions, higher ratios can be used  
19 to compensate the loss of NH<sub>3</sub> by oxidation and other side reactions. The influence of the  
20 NH<sub>3</sub>/NO ratio has been studied in the range 0.3-1.2 at different operating conditions: 250-  
21 300°C and 1-2 L min<sup>-1</sup> n.t.p. (WHSV = 5360-10700 mol h<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup>).

22 As an illustration, Figure 5 shows the transient of a set of experiments, where NO feed  
23 concentration is kept constant at 500 ppm and NH<sub>3</sub> feed concentration is increased step-  
24 wise from 0 to 500 ppm. Hence, NH<sub>3</sub> is the limiting reactant, outlet NH<sub>3</sub> concentration being  
25 close to zero during the whole test. On the contrary, NO concentration decreases as NH<sub>3</sub>  
26 concentration increases, to reaction completion. The corresponding steady state NO  
27 conversions are depicted in Figure 3c for different operating conditions. The maximum NO  
28 conversion calculated from the stoichiometry, assuming complete NO reaction is indicated  
29 by a straight line. Thus, for NH<sub>3</sub>/NO ratios lower than 0.8 nearly the maximum attainable NO  
30 conversion is achieved. For higher ratios, NO conversion tends to be independent of the

1 NH<sub>3</sub>/NO ratio and highly dependent on temperature: an increase of 14% in NO conversion is  
2 **observed** when temperature increases from 250 to 300°C. The influence of space time is less  
3 marked, only a 3% increase in NO conversion is obtained when the space time is halved. This  
4 behaviour is in agreement when previous studies that reported a critical NH<sub>3</sub>/NO ratio of 0.7.  
5 <sup>35</sup>

## 6 **Kinetic modelling**

7 The experiments carried out at different operating conditions (temperature, flow rate and  
8 concentration) have been used to characterize the kinetics of the SCR reaction. As indicated  
9 in the methodology section, the monolithic catalyst was ground and sieved to a small size, in  
10 order to eliminate the influence on the kinetics of the diffusional steps. In that section, a  
11 model for the lab-scale fixed reactor based on gas and solid phase mass balances was also  
12 presented. This model must be completed with the kinetic equations, as show in Table 1.  
13 The mechanism of the reaction suggests the form of the kinetic equations: NH<sub>3</sub> adsorbs and  
14 desorbs in the catalyst active sites according to first order elementary steps (net adsorption  
15 rate, ) and NO from the gas phase reacts with adsorbed NH<sub>3</sub> ( ). The kinetic constants  
16 are assumed to vary with temperature according to Arrhenius dependence. The  
17 corresponding equations are included in Table 1.

18 The model parameters are calculated by fitting the model to the results of two types of  
19 experiments. The first type consists of NH<sub>3</sub> dynamic adsorption and desorption experiments  
20 on the catalyst. These tests were carried by flowing 500 ppm of ammonia in nitrogen in the  
21 adsorption, or nitrogen in the desorption experiments, in the range 150-300°C and 1-3 L  
22 min<sup>-1</sup> n.t.p. (WHSV 5360-16100 mol h<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup>). Figure 6 (symbols) shows typical experimental  
23 results obtained in this case at 1 and 3 L min<sup>-1</sup> n.t.p. and 300°C.

24 In the adsorption experiment, a step of NH<sub>3</sub> is fed to the reactor and a breakthrough curve is  
25 obtained in the effluent. The existence of this sigmoidal breakthrough curve, instead of a  
26 straight step, indicates that the adsorption is not instantaneous, and hence equilibrium is  
27 only achieved at the end of the experiment, when the catalyst is completely saturated with  
28 NH<sub>3</sub>. On increasing the gas flow rate, the transient of the experiment is modified, producing  
29 a decrease in the breakthrough time. Desorption experiments were carried out after the  
30 adsorption, when the NH<sub>3</sub> of the feed was replaced by nitrogen. This leads to the desorption

1 of most of the  $\text{NH}_3$  previously adsorbed. Part of the  $\text{NH}_3$  is adsorbed strongly, and can be  
2 desorbed only at higher temperature. The shape of the effluent concentration curve  
3 depends on the desorption reaction rate.

4 The dynamic  $\text{NH}_3$  adsorption and desorption experiments allow the determination of the  
5 kinetic parameters of the net adsorption rate equation, e.g. adsorption and desorption  
6 kinetic constants (      and      ) and total adsorption capacity (      ). These parameters have  
7 been obtained by fitting the un-steady state  $\text{NH}_3$  outlet concentration predicted by the lab-  
8 scale fixed-bed reactor model to all the experimental data (adsorption and desorption) at  
9 once. It should be noted that in the model considered, adsorption and desorption curves are  
10 affected by both adsorption and desorption kinetic constants. Results are summarized in  
11 Table 3. Model predictions are depicted in Figure 6 (lines) together with the experimental  
12 data, in order to evaluate the goodness of the fitting. As shown, the model is able to predict  
13 the breakpoint of the adsorption tests accurately, small discrepancies being observed in the  
14 vicinity of the saturation.

15 The second type of experiments consists of NO reduction studies, in which NO and  $\text{NH}_3$  are  
16 fed to the reactor, containing the catalyst previously saturated with  $\text{NH}_3$ . Experiments have  
17 been done at the following range of operating conditions: 220-320°C, 1-3  $\text{L min}^{-1}$  n.t.p.  
18 (WHSV 5360-16100  $\text{mol h}^{-1} \text{kg}_{\text{cat}}^{-1}$ ) and 500 ppm NO and 290-500 ppm  $\text{NH}_3$ . The unsteady  
19 state NO and  $\text{NH}_3$  outlet concentrations are compared for experiments at 1  $\text{L min}^{-1}$  n.t.p.,  
20 500 ppm NO and  $\text{NH}_3$  and different temperatures in Figure 7. At the beginning of the  
21 experiment, NO conversion is complete because of the high reaction rate achieved when the  
22 catalyst is saturated with  $\text{NH}_3$ . As the reduction reaction proceeds, adsorbed  $\text{NH}_3$  decreases,  
23 which is only partially replaced by  $\text{NH}_3$  from the gas phase, so reaction rate decreases  
24 gradually (and hence NO concentration increases), until reaching the steady state.

25 The results of these experiments were used for fitting the kinetic parameters corresponding  
26 to the SCR reaction. As before, all the unsteady state concentration data have been used  
27 together in the fitting. The values used for the adsorption parameters were the ones  
28 determined in the adsorption experiments. Results can be found in Table 3.

29

## 1 **Reactor modelling**

2 The experiments carried out in the lab-scale fixed-bed reactor are useful to get insight into  
3 the catalyst kinetics, but give no information on the influence of mass transfer processes in  
4 the monolith. For this reason, additional experiments have been carried out in the bench-  
5 scale fixed-bed reactor, in which the catalyst is used in its commercial monolithic shape.  
6 Information obtained in this way represents better the behaviour of the catalyst in  
7 industrial-scale reactors. The range of operating conditions in these experiments  
8 corresponds to temperature 180-300°C and flow rate 8-12 L min<sup>-1</sup> n.t.p. (WHSV 35.6-53.4  
9 mol kg<sub>cat</sub><sup>-1</sup> h<sup>-1</sup>). NO and NH<sub>3</sub> feed concentrations have been fixed to 500 ppm.

10 As explained in the methodology section, external and internal mass transfer must be  
11 accounted for in the model of the bench-scale reactor (see equations in Table 2). External  
12 mass transfer in the monolithic channels was modelled using a literature correlation.<sup>30</sup> On  
13 the contrary, internal mass transfer in the monolithic washcoating, modelled by the internal  
14 effectiveness factor (  $\eta$  ), was fitted to the data obtained in this set of experiments. The  
15 fitting has been done by least-square regression of the NO conversion obtained at steady-  
16 state. This way, the risk of misleading internal mass transfer due to transient phenomena  
17 (e.g. NH<sub>3</sub> adsorption and desorption dynamics) is eliminated.

18 For each experiment, the internal effectiveness factor that fits the experimental NO  
19 conversion was determined. It was found that the internal effectiveness factors obtained  
20 from experiments at the same temperature but different flow rates were not significantly  
21 different. This is in agreement with a phenomenological analysis of internal mass transfer,  
22 which suggests that the rate of mass transfer depends on the textural properties of the  
23 washcoating, the physical properties of the gas (diffusion coefficients) and the intrinsic  
24 kinetics. These properties may depend on temperature, but not on gas flow rate. Regarding  
25 temperature, it was found that the internal effectiveness factor is highly influenced by this  
26 parameter; an exponential decrease with temperature was observed. Thus, the data were fit  
27 to the following expression, found to provide the best fit:  $\eta = \exp(-k_p/k_d)$ . The  
28 goodness of the fitting can be observed in Figure 8; the correlation coefficient R<sup>2</sup> was 0.993.

29 The performance of the reactor model, completed with the internal effectiveness factor, was  
30 tested at steady and unsteady state conditions by comparison with experimental data. In

1 Figure 9, the steady state NO conversion used to calculate the internal effectiveness factors  
2 (symbols) are depicted together with the predictions of the reactor model (line). It can be  
3 observed that the model is able to predict the experimental data successfully within the  
4 temperature range considered.

5 The performance of the model in unsteady state is evaluated in Figure 10 in terms of the  
6 evolution of NO concentration at the reactor exit. The conditions of the experiment, which  
7 influence the interpretation of the results, are the following: first, only NO is fed to the  
8 reactor and when the outlet concentration is constant, NH<sub>3</sub> is added in stoichiometric  
9 proportion. For this reason, a transient decrease of NO is observed, until the steady state  
10 value is reached. Figure 10 shows that the reactor model is able of predicting this transient  
11 in the temperature range considered in this work. As shown, on increasing temperature the  
12 decrease is more pronounced and the steady state is reached faster.

13

## 14 **Conclusions**

15 The kinetics of NO SCR has been studied in two fixed-bed reactors, a lab-scale reactor using  
16 ground catalyst and a bench-scale reactor using the catalyst in its commercial monolithic  
17 shape.

18 The parametric study of the reaction carried out with the most important variables has  
19 revealed the following conclusions. Temperature has a great influence in the reaction rate,  
20 and at least 300°C is required at a WHSV of 16100 mol h<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup>. Oxygen is required in the  
21 feed because participates as reactant in the SCR, having a positive effect on the reaction rate  
22 below 8% oxygen.

23 The experiments done at the lab-scale reactor have been used for the fitting of a kinetic  
24 model, based on a reaction mechanism considering the adsorption of NH<sub>3</sub> on the catalyst,  
25 followed by the reaction between NO and adsorbed NH<sub>3</sub> with satisfactory results.

26 Additional experiments carried out in the bench-scale reactor were used for the modelling of  
27 mass transfer in the monolithic catalyst. Thus, the internal effectiveness factor was  
28 calculated and correlated with temperature. Overall, the reactor model is able of predicting  
29 both steady and unsteady state experiments.

1

## 2 **Acknowledgements**

3 This work was financed by the Spanish Council of Environment (ref. 165/PC08/1-13.1). Emilio  
4 Muñoz thanks the Government of the Principality of Asturias for a Ph.D. fellowship (Severo  
5 Ochoa Program). Catalysts samples were a generous gift from ARGILLON

6

7

1

## 2 Caption to figures

3

4 Figure 1 Diagram of the bench-scale reactor.

5 Figure 2 Influence of temperature. Transient in NO (a) and NH<sub>3</sub> (b) outlet  
6 concentrations. Flow rate = 3 L min<sup>-1</sup> n.t.p. NO and NH<sub>3</sub> inlet concentration =  
7 500 ppm. Temperature: 150°C (—), 170°C (— —), 190°C (• —), 220°C (- -),  
8 280°C (• —) and 320°C (•••).

9 Figure 3 Steady state NO conversion. Influence of operating variables:

10 (a) Temperature. 3 L min<sup>-1</sup> n.t.p., NH<sub>3</sub>/NO=1.

11 (b) Oxygen concentration. 2 L min<sup>-1</sup> n.t.p., 250°C, NH<sub>3</sub>/NO=0.6.

12 (c) NH<sub>3</sub>/NO ratio. (■) 2 L min<sup>-1</sup> n.t.p., 250°C. (◆) 2 L min<sup>-1</sup> n.t.p., 300°C. (▲) 1  
13 L min<sup>-1</sup> n.t.p., 300°C. **The straight line indicates the maximum stoichiometric**  
14 **NO conversion.**

15 Figure 4 Influence of oxygen concentration. Transient in NO (a) and NH<sub>3</sub> (b) outlet  
16 concentrations. Flow rate = 2 L min<sup>-1</sup> n.t.p., temperature = 250°C,  
17 NH<sub>3</sub>/NO=0.6. Oxygen concentration: 0% (—), 8% (— —) and 21% (- -).

18 Figure 5 Influence of NH<sub>3</sub>/NO feed ratio. Variation of NH<sub>3</sub> feed concentration (•••) and  
19 the corresponding evolution in NO (—) and NH<sub>3</sub> (— —) outlet concentrations.  
20 Flow rate = 2 L min<sup>-1</sup> n.t.p., temperature = 250°C.

21 Figure 6 Fitting of NH<sub>3</sub> adsorption (a) and desorption (b) transient experiments. Feed  
22 concentration: 500 ppm. Temperature: 300°C. Flow rate: 1 (●) and 3 L min<sup>-1</sup>  
23 n.t.p. (▲). Symbols: experiments. Lines: model fitting.

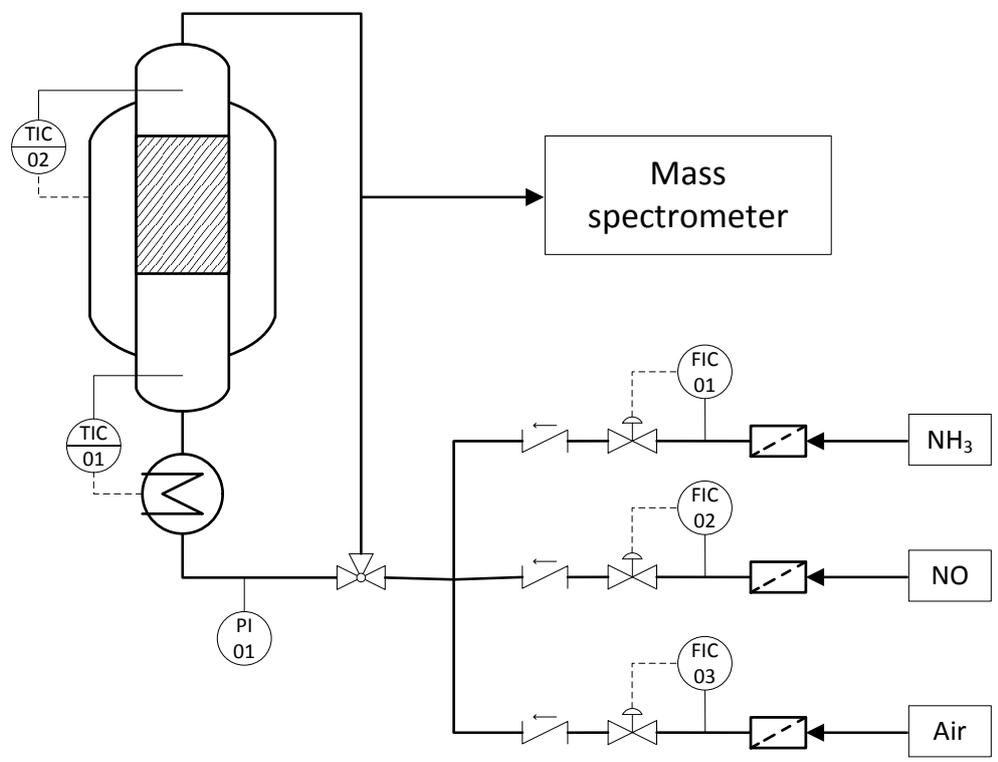
24 Figure 7 Fitting of NO transient reduction experiments: NO (a) and NH<sub>3</sub> (b) effluent  
25 concentrations. Feed concentration: 500 ppm NO and NH<sub>3</sub>. Flow rate: 1 L min<sup>-1</sup>  
26 n.t.p. Temperature: 220 (◆), 280 (▲) and 320°C (●). Symbols: experiments.  
27 Lines: model fitting.

- 1 Figure 8 Influence of temperature in the internal effectiveness factor. Symbols:  
2 internal effectiveness factor fit from experiments. Line: fitting.
- 3 Figure 9 Comparison of model simulations (line) and experiments (symbols) in terms of  
4 NO steady state conversion. Flow rate: 8-12 L min<sup>-1</sup> n.t.p. Inlet concentration:  
5 500 ppm NO and NH<sub>3</sub>.
- 6 Figure 10 Evaluation of the performance of the model to predict the unsteady state  
7 experiments in the bench scale reactor. Flow rate: 8 L min<sup>-1</sup> n.t.p.  
8 Concentrations: 500 ppm NO and NH<sub>3</sub>. Temperature: 180 (◆), 250 (▲) and  
9 300°C (●). Symbols: experiments. Lines: simulations.
- 10
- 11

1

2 **Figure 1**

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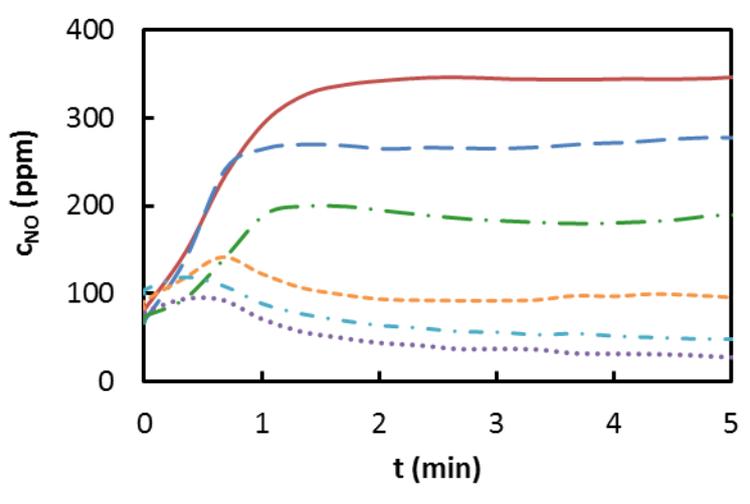
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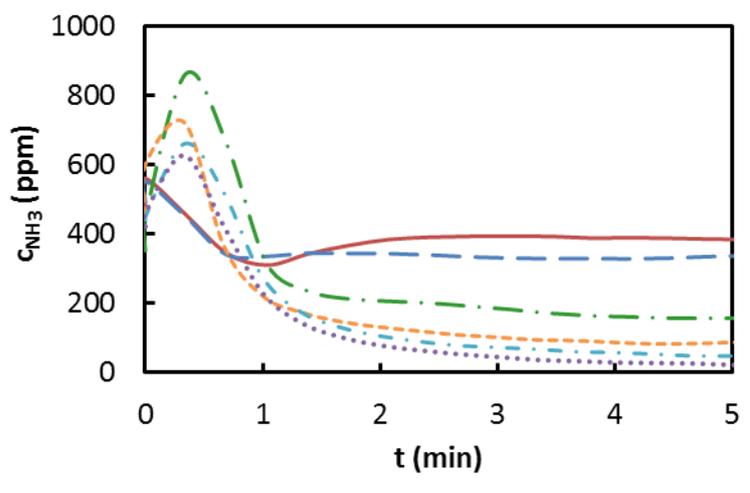
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2 **Figure 2**



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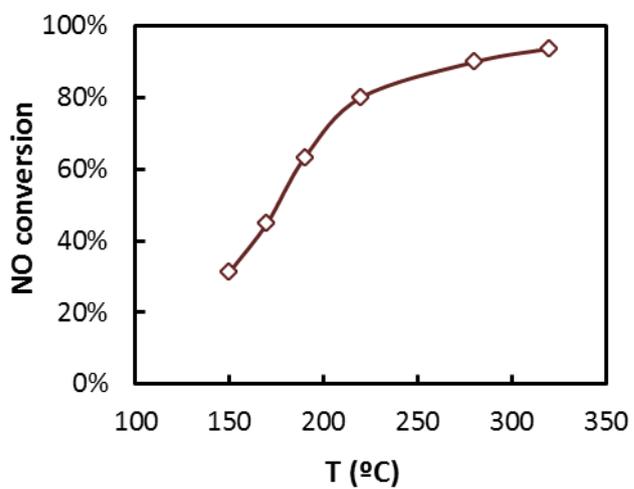


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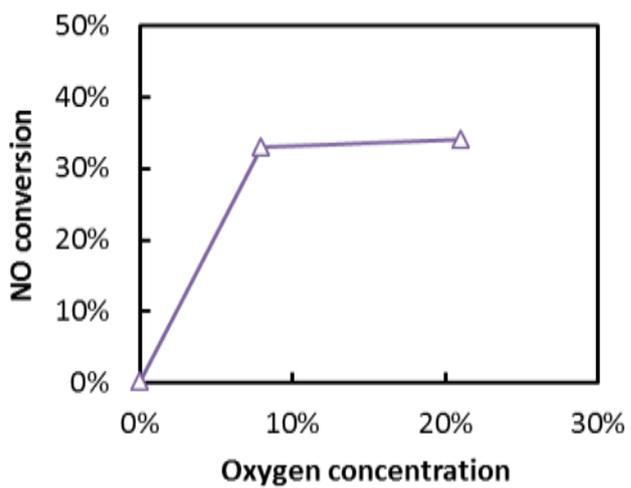
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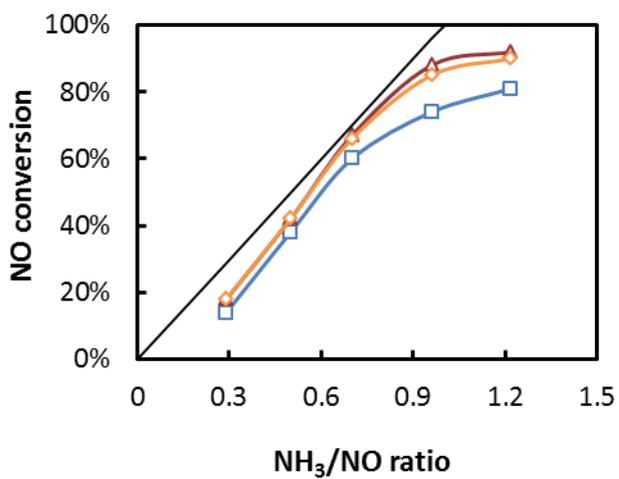
2 **Figure 3**



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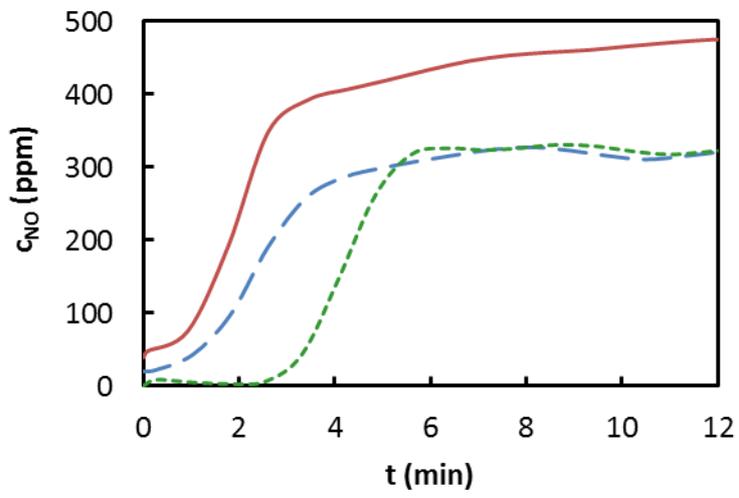
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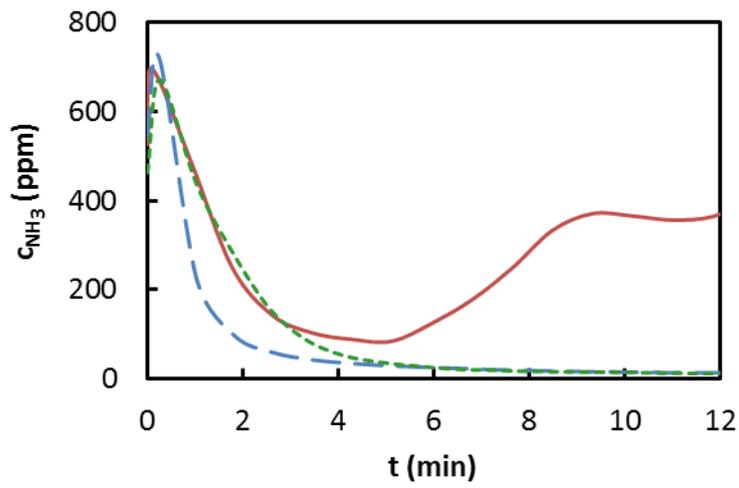
1 **Figure 4**

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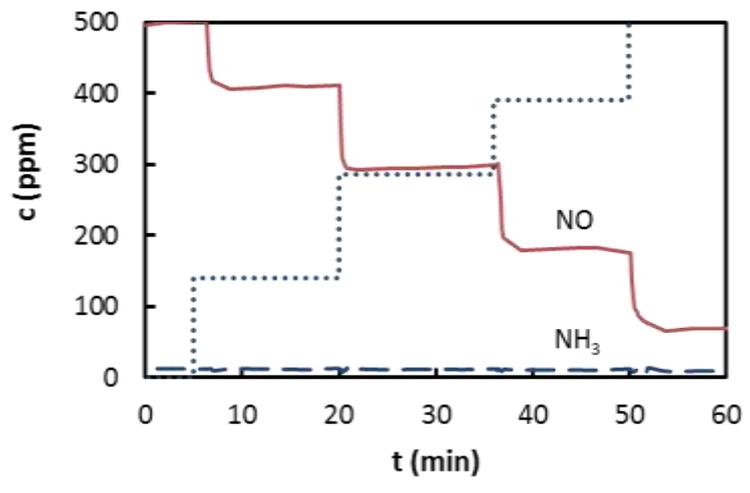
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2 **Figure 5**

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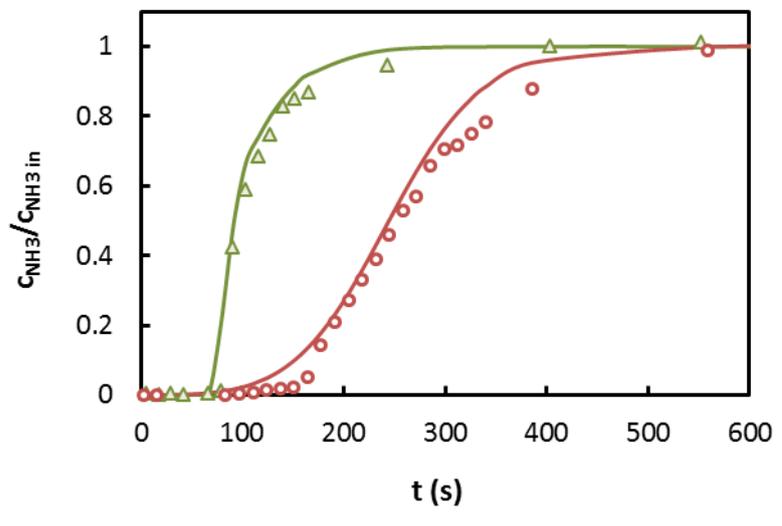
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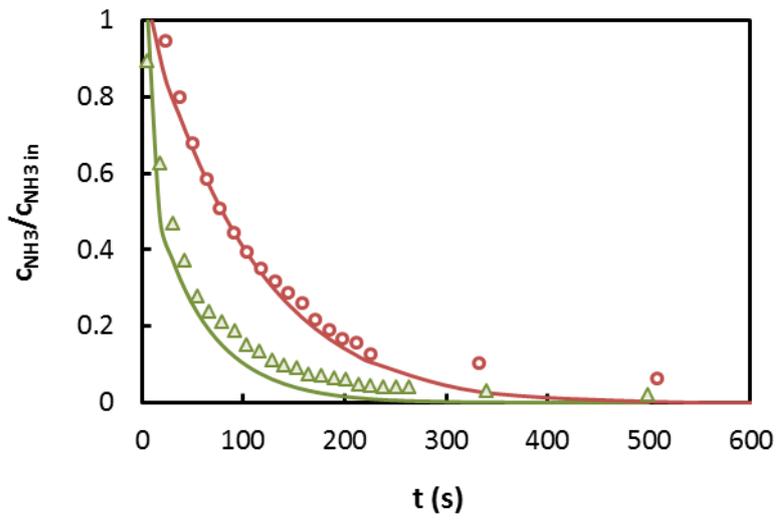
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2 **Figure 6**

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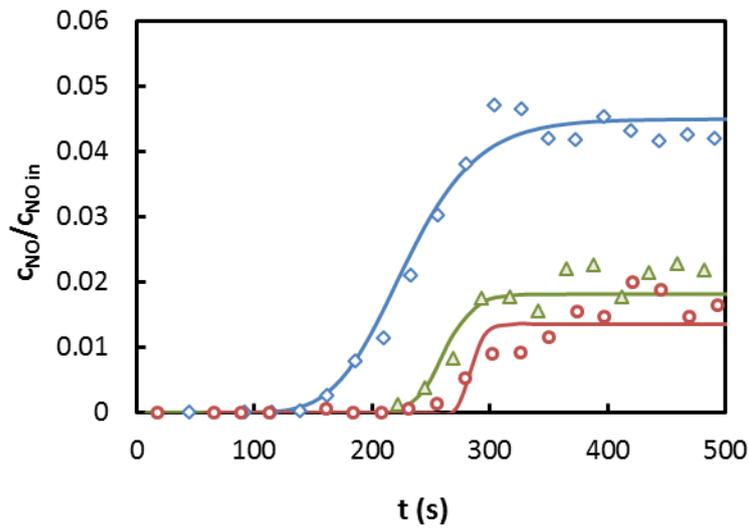
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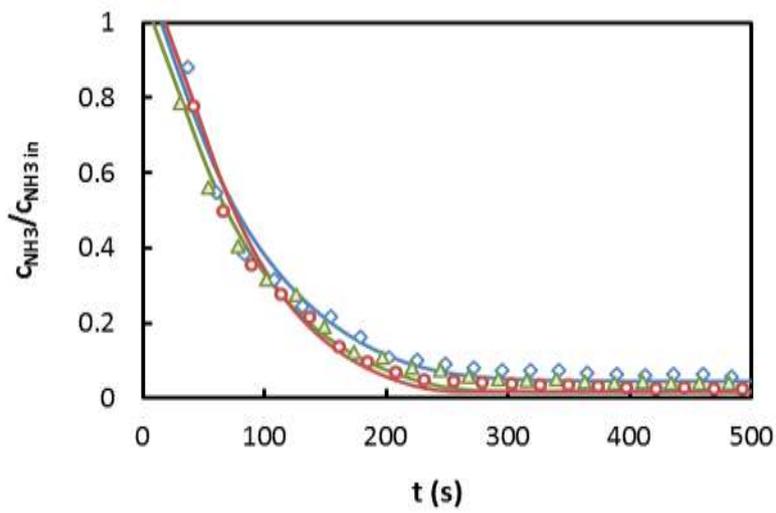
2 **Figure 7**

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4 A

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6 b

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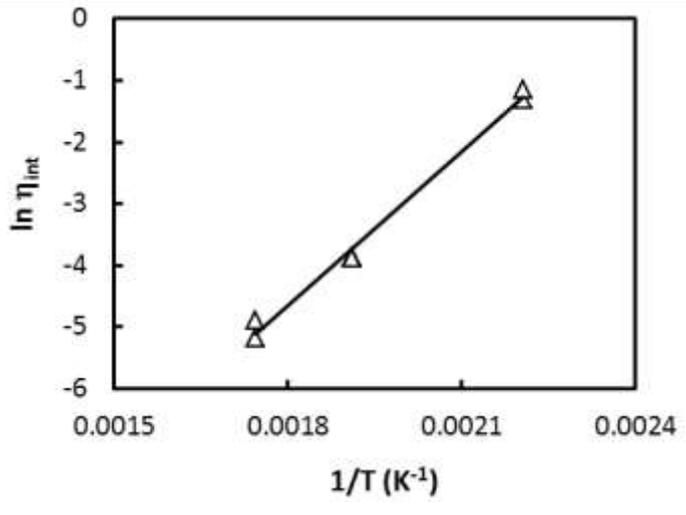
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2 **Figure 8**

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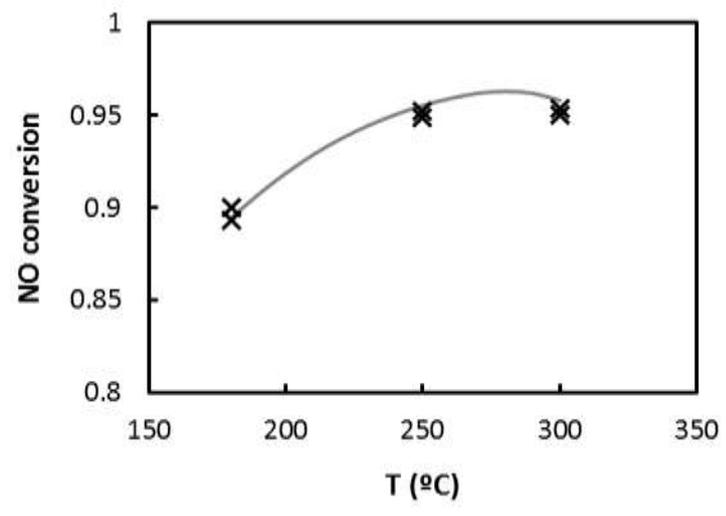
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2 **Figure 9**

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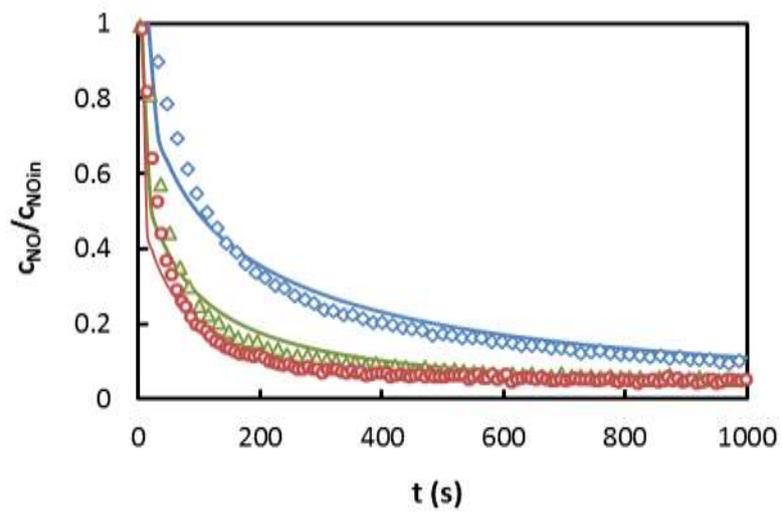
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2 **Figure 10**

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2 **List of tables**

3

4 Table 1 Model for the lab-scale fixed-bed reactor.

5 Table 2 Model for the bench-scale fixed-bed reactor.

6 Table 3 Parameters of the kinetic model obtained by fitting of experimental data of  
7 the lab-scale fixed-bed reactor.

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1 **Table 1**

2

Gas phase mass balances	Boundary conditions
$\frac{dN_A}{dt} = \dots$ $\frac{dN_B}{dt} = \dots$	
Solid phase mass balance	Boundary conditions
$\frac{dN_s}{dt} = \dots$	
Kinetic model	

3 A = NO, B = NH<sub>3</sub>

4

5

1 **Table 2**

2

Gas phase mass balances	Boundary conditions
$\frac{d}{dt} \int_V \rho_A dV = \sum \dot{m}_{A,i} - \sum \dot{m}_{A,e}$	
Solid phase mass balance	Boundary conditions
$\frac{d}{dt} \int_V \rho_B dV = \sum \dot{m}_{B,i} - \sum \dot{m}_{B,e}$	
Interphase equations	
Kinetic equations	

3 A = NO, B = NH<sub>3</sub>

4

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6

1 **Table 3**

2

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Kinetic parameters
0.113 mol NH <sub>3</sub> kg <sub>cat</sub> <sup>-1</sup>
2.75 m <sup>3</sup> mol <sup>-1</sup> s <sup>-1</sup>
0.0278 s <sup>-1</sup> at 280°C
9.8 kJ mol <sup>-1</sup>
260 m <sup>3</sup> mol <sup>-1</sup> s <sup>-1</sup> at 280°C
92.8 kJ mol <sup>-1</sup>

---

3

4

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1

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