

1 Article

## 2 A SAR-based technique for microwave imaging and 3 material characterization

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11 **Abstract:** This contribution presents a simple and fast SAR-based technique for microwave imaging  
12 and material characterization from microwave measurements acquired in tomographic systems.  
13 Synthetic Aperture Radar (SAR) backpropagation is one of the simplest and fastest techniques for  
14 microwave imaging. However, in the case of heterogeneous objects and media, a priori information  
15 about the constitutive parameters (conductivity, permittivity) is needed for an accurate imaging. In  
16 some cases, a first guess of the constitutive parameters can be extracted from an uncorrected SAR  
17 image, and then, the estimated parameters can be introduced in a second step to correct the SAR  
18 image. The main advantage of this methodology is that little or no need of a priori information about  
19 the object to be imaged is needed. Besides, calculation time is not significantly increased with respect  
20 to conventional SAR, thus allowing real-time imaging capabilities. The methodology has been  
21 validated by means of measurements acquired in a cylindrical setup.

22 **Keywords:** Synthetic Aperture Radar (SAR); microwave imaging; constitutive parameters;  
23 conductivity; permittivity; tomography.  
24

### 25 1. Introduction

26 Electromagnetic imaging is one of the most widespread techniques for nondestructive testing  
27 thanks to the capability of the electromagnetic waves to penetrate through different media. The  
28 different responses of these media depending on the working frequency band (terahertz [2],  
29 millimeter waves [3], etc.) have resulted in a wide variety of electromagnetic imaging systems, not  
30 only in terms of hardware, but also concerning processing techniques.

31 Electromagnetic inverse scattering and imaging techniques are able to provide the geometry of  
32 the object/area under inspection, the constitutive parameters (permittivity, conductivity), or both.  
33 The capability of recovering these parameters with a certain degree of accuracy depends not only on  
34 the setup/hardware of the imaging system and the working frequency band(s), but also on the post-  
35 processing algorithms. Factors such as the dynamic range or processing time have to be taken into  
36 account when selecting an imaging system that best fits the requirements for a particular  
37 nondestructive testing application. As an example, detecting 15-20 cm size metallic targets buried 30  
38 cm in dry sand [4], imaging of targets behind a 10 cm thick wall [5], or locating tumors in breast tissue  
39 [6] require different microwave imaging hardware and methods.

40 In general, inverse scattering and imaging techniques can be classified in two main groups: on  
41 the one hand, those based on scattered field backpropagation and, on the other hand, model-based  
42 imaging techniques.

43 In the first group, standard Synthetic Aperture Radar (SAR) imaging, also known as  
44 backpropagation or range migration techniques, [4]-[8], are the most common techniques for radar  
45 applications, due to their simplicity, which makes these techniques computationally efficient thanks  
46 to the use of FFTs. Their main limitation is the amount of spatial and frequency bandwidth required  
47 for accurate imaging. Nevertheless, improvements in microwave and radiofrequency hardware have  
48 made affordable the development of ultrawideband systems for imaging applications.

49 The second group includes model-based techniques that require setting an electromagnetic  
50 model of the scenario-under-test. Then, a cost function relating the measured scattered field and the  
51 calculated one for the model, is defined. Global minimum of the cost function corresponds to the best  
52 fit between the true and the modelled target/object-under-test (OUT). Equivalent currents [9],[10],  
53 level-set [11], linear sampling method [12], local optimization strategies [13], and global optimization  
54 based on evolutionary algorithms [3],[14] fall within this second group. As opposed to  
55 backpropagation techniques, the strength of model-based inverse scattering lies on the little amount  
56 of information needed, being capable of reconstructing the profile accurately using a single frequency  
57 and few field-of-views. The price to pay is a high calculation time, mainly due to the iterative nature  
58 of algorithms.

59 Hybrid backpropagation and model-based techniques have been also considered in order to  
60 obtain accurate imaging results [15]. In these cases, the former is used to provide a first guess of the  
61 profile of the target/OUT for the latter method.

62 In the area of nondestructive testing for detection of targets/objects embedded in a surrounding  
63 opaque medium (e.g. detection of tumors in breast tissue [6]), the aforementioned techniques require  
64 a priori information about the problem, which varies depending on the inverse scattering or imaging  
65 technique to be applied. For example, those based on multilayered Green's Function formulation  
66 need an initial guess of the constitutive parameters of the surrounding medium [16],[17]. Inverse  
67 scattering techniques based on cost function minimization [3],[14] require a set of first guess solutions  
68 and the definition of the search space boundaries.

69 Sometimes, having an accurate estimate of the constitutive parameters of the surrounding  
70 medium can be difficult, such as in Ground Penetrating Radar (GPR) and Through-The-Wall Imaging  
71 (TTWI) applications, where ground and wall composition is not homogeneous, and conductivity and  
72 permittivity can be affected by moisture levels. In these cases, additional measurements (and  
73 hardware) are required for a proper estimation of these parameters, mostly reflectometry [18] and  
74 transmission/reflection-based techniques [19],[20]. Besides, these constitutive parameters can be also  
75 the unknown of the inverse scattering problem, as in security screening systems for detecting  
76 weapons and explosives.

77 Aiming to reduce the need for additional measurements to characterize the constitutive  
78 parameters, SAR-based techniques have been proved to be successful in recovering the geometry and  
79 also getting an estimate of the conductivity and permittivity of the OUT and/or the surrounding  
80 medium [21],[22]. The theoretical background is the different velocity of the electromagnetic waves  
81 when passing through different media, so that the reflectivity of the imaged targets is displaced  
82 backwards with respect to their expected position. In order to detect this shifting, a reference  
83 background is needed (the human body surface in the case of [21], a reference metallic plate in [22]  
84 and [23]).

85 This contribution extends the SAR-based imaging techniques presented in [21]-[23] to provide a  
86 better recovery of geometry and constitutive parameters, making a more efficient use of the imaging  
87 information. More precisely, the proposed methodology takes advantage of the reflections at the  
88 interfaces between different media to obtain an estimate of the permittivity and the conductivity,  
89 avoiding the need of a reference target or a background medium.

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95 **2. Methodology**

96 *2.1. Synthetic Aperture Radar imaging*

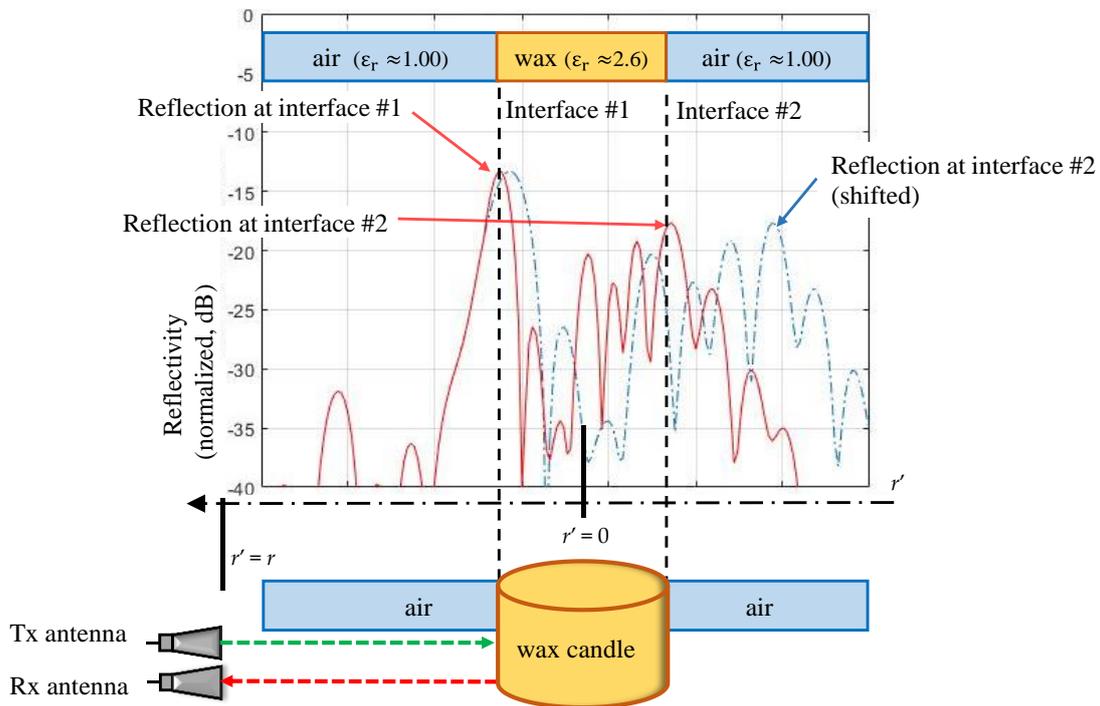
97 The basics of SAR processing are presented in this section. For the sake of simplicity, a two-  
 98 dimensional (2D) scenario in the XY plane is considered. A 3D scenario with translation symmetry  
 99 along z-axis could be assumed as well without loss of generality. Given the scattered field  $E_{scatt}(f,r,\varphi)$   
 100 measured at the position  $(r,\varphi)$  over a certain bandwidth  $BW=[f_1 f_2]$ , the reflectivity  $\rho(x', y')$  evaluated  
 101 at the position  $(x', y')$  of the scenario-under-test is defined in Equation (1), assuming an homogeneous  
 102 propagation medium:

$$\rho(x', y') = \sum_{f=f_1:f_2} E_{scatt}(f,r,\varphi) \exp(j k_{medium} R) \quad (1)$$

103 Where  $k_{medium}$  is the wavenumber defined as  $k_{medium} = 2 \pi f / v_{prop,medium}$ ,  $f$  being the frequency and  
 104  $v_{prop,medium}$  the propagation velocity of the electromagnetic wave in a particular medium.  $R$  is the  
 105 Euclidean distance between  $(r,\varphi)$  and  $(x', y')$ . In case the medium is vacuum or air,  $k_0 = 2 \pi f / c$ . The  
 106 center of the scenario-under-test (e.g. the center of a rotary platform in the case of a tomographic  
 107 imaging system) is defined as the origin of the coordinate system. A monostatic or quasi-monostatic  
 108 setup is considered, so that the transmitting and receiving antennas are placed at  $(r,\varphi)$ . Image  
 109 resolution in the radial (range) direction,  $\Delta r$ , is given by Equation (2):

$$\Delta r = 0.5 v_{prop,medium} / (f_2 - f_1) \quad (2)$$

110 The problem can be even reduced to a one-dimensional case in the range direction, for those  
 111 points satisfying  $x' = r' \cos(\varphi)$ ,  $y' = r' \sin(\varphi)$ , so  $R = r - r'$ .  
 112



113 **Figure 1.** Illustration of the reflectivity delay due to the consideration of propagation in free-  
 114 space, and comparison with corrected reflectivity when considering true permittivity ( $\epsilon$ ).  
 115  
 116

117 Let us consider now the imaging scenario depicted in Figure 1, where the OUT is a cylindrical  
 118 wax candle of diameter  $d_{OUT}$ . The axis of the OUT is aligned with the axis of the rotary table, so that  
 119 the distance between the Tx/Rx antennas is  $r - d_{OUT}/2$  for any rotation angle  $\varphi$ . The medium  
 120 surrounding the wax candle is air ( $k_{medium} = k_0$ ). Thus, the reflectivity at any point  $r' \in [d_{OUT}/2, r]$  is  
 121 given by Equation (3). The range  $[d_{OUT}/2, r]$  will be denoted as Region #1.

$$\rho(r', \varphi) = \sum_{f=f_1:f_2} E_{\text{scatt}}(f, r, \varphi) \exp(j k_0 (r - r')), r' \in [d_{\text{OUT}}/2, r] \quad (3)$$

122 Next, the reflectivity for a point *inside* the wax candle has to be calculated taken into account the  
 123 different propagation velocity inside the wax,  $v_{\text{prop,OUT}} = c / (\epsilon_{r,\text{OUT}})^{1/2}$ . Reflectivity in the interval  $r' \in [-$   
 124  $d_{\text{OUT}}/2, d_{\text{OUT}}/2]$  (Region #2) is then calculated as indicated in Equation (4):

$$\rho(r', \varphi) = \sum_{f=f_1:f_2} E_{\text{scatt}}(f, r, \varphi) \exp(j k_0 (r - d_{\text{OUT}}/2)) \exp(j k_{\text{OUT}} (d_{\text{OUT}}/2 - r')), r' \in [-d_{\text{OUT}}/2, d_{\text{OUT}}/2] \quad (4)$$

125 And finally, for those points behind the wax candle (Region #3), the reflectivity is given by  
 126 Equation (5), where the interval within the wax candle is taken into account:

$$\rho(r', \varphi) = \sum_{f=f_1:f_2} E_{\text{scatt}}(f, r, \varphi) \exp(j k_0 (r - d_{\text{OUT}} - r')) \exp(j k_{\text{OUT}} d_{\text{OUT}}), r' < -d_{\text{OUT}}/2 \quad (5)$$

127 Now, let us assume that neither the position nor the constitutive parameters of the OUT (the  
 128 wax candle) are known. In this case, one could make use of Equation (3) to evaluate the reflectivity  
 129 at any point  $r'$ . If free-space propagation is considered, a first peak of the reflectivity should appear  
 130 at the interface between the air and the OUT (denoted as interface #1 in Figure 1). Similarly, a  
 131 reflectivity peak should appear at any position  $r'$  where there is an interface between two media with  
 132 different constitutive parameters. But, as free-space propagation is assumed for evaluating the  
 133 reflectivity at any position (Equation (1),  $k_{\text{medium}}=k_0$ ), reflectivity peaks will be shifted backwards, as  
 134 illustrated in Figure 1 (dashed blue line). If the position of the interfaces and the permittivity values  
 135 of the different media were known, Equations (3)-(5) could be used, resulting in a proper recovery of  
 136 the reflectivity (Figure 1, solid red line).

137 Inaccurate recovery of the permittivity may result in inaccurate location of embedded targets in  
 138 homogeneous media (e.g. tumors in breast tissue [6], or landmines buried in the ground [4]).  
 139 Furthermore, depending on the imaging setup, free-space SAR approach could result in the  
 140 concealed targets to be imaged *outside* the object where they are embedded, as it will be shown in a  
 141 latter example.

## 142 2.2. Constitutive parameters estimation and range correction

143 Under the assumption that the outer profile/geometry of the OUT is known, it is possible to  
 144 recover the conductivity and permittivity of the OUT from the shifted reflectivity peaks. For the sake  
 145 of simplicity, let us consider again the example presented in Figure 1 (a wax candle of diameter  $d_{\text{OUT}}$ ).

146 If the permittivity of the wax is not known, then, the reflectivity calculated according to Equation  
 147 (1) for all  $r'$  with  $k_{\text{medium}}=k_0$  corresponds to the dashed blue line in Figure 2. From the theoretical  
 148 analysis presented in Section 2.1, it is known that the reflectivity peak corresponding to the interface  
 149 #2 (rear side of the candle) has to be shifted, as  $k_0$  instead of  $k_{\text{OUT}}$  was used to calculate the reflectivity.  
 150 Although its exact position cannot be estimated a priori, a search region can be defined taking into  
 151 account the size of the OUT. For this example, it can be expected the reflectivity peak corresponding  
 152 to the interface #2 to appear at  $r' < -d_{\text{OUT}}$ . The distance between the shifted reflectivity peak of interface  
 153 #2 and the reflectivity peak of interface #1 is denoted as  $d_{\text{echo}}$  (Figure 2).

154 Next, the relationship between the delay (or phase shift) considering free-space propagation  
 155 (Equation (1),  $k_{\text{medium}}=k_0$ ) and propagation through the OUT considering a permittivity estimate  $\epsilon_{r,\text{est}}$ ,  
 156 yields Equation (6). An explanation about how to obtain this equation is given in [21],[22]:

$$\epsilon_{r,\text{est}} = (d_{\text{echo}} / d_{\text{OUT}})^2 \quad (6)$$

157 Note that, for the scenario considered to illustrate this methodology, no additional reference  
 158 targets are required for recovering the permittivity. In this case, the shifted reflection at the interface  
 159 #2 corresponds to the OUT-air interface.

160 Once the permittivity is estimated, Equations (3)-(5) can be applied to recover the reflectivity  
 161 with the corrected propagation velocity within the OUT, so that the reflectivity peak of the interface  
 162 #2 will appear at the correct position, that is, without shifting (solid red line in Figure 2).

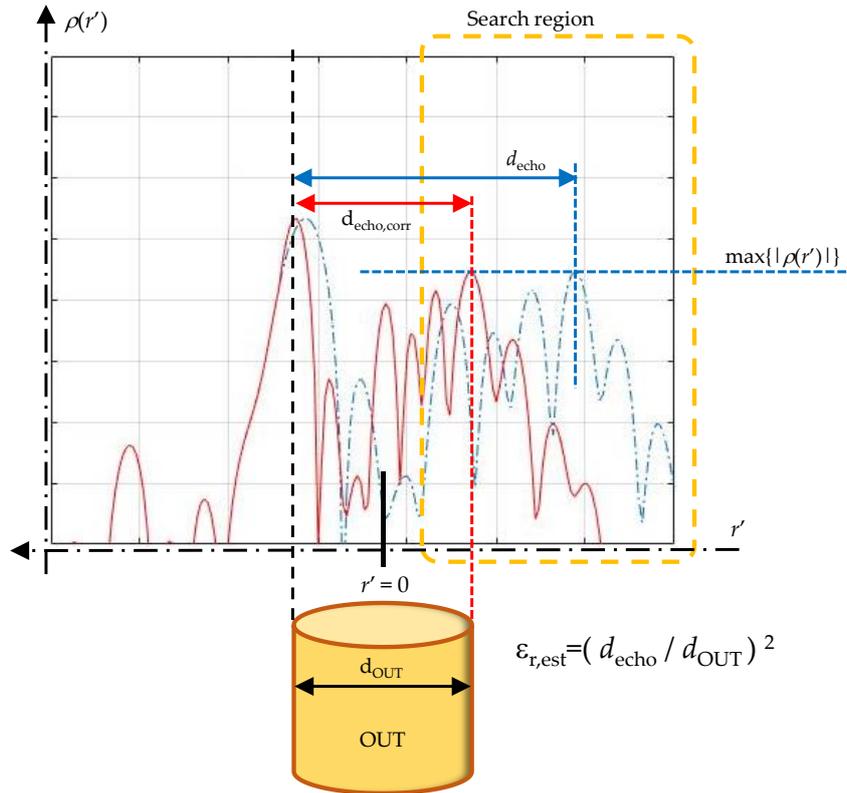
163 In addition to the permittivity, an estimate of the conductivity ( $\sigma_{OUT}$ ) can be obtained as well, by  
 164 measuring the difference on the reflectivity levels at interfaces #1 and #2. The attenuation constant  $\alpha$   
 165 (measured in Np/m) is given by Equation (7) [22]:

$$\alpha = \ln(|\rho(r'_{interface \#1})| / |\rho(r'_{interface \#2})|) / d_{OUT} \quad (7)$$

166  $\alpha$  is related to the conductivity according to Equation (8) [22]:

$$\sigma \approx \text{Im}\{ (\epsilon_r)^{1/2} + j \alpha c / (2\pi f_c) \}^2, \quad f_c = (f_1 + f_2) / 2 \quad (8)$$

167 A summary of the methodology described in this section is illustrated in Figure 3.



168  
 169 **Figure 2.** Methodology to estimate the permittivity of the OUT ( $\epsilon_{r,est}$ ) from scattered field  
 170 measurements given the thickness of the OUT ( $d_{OUT}$ ).

171 **3. Results**

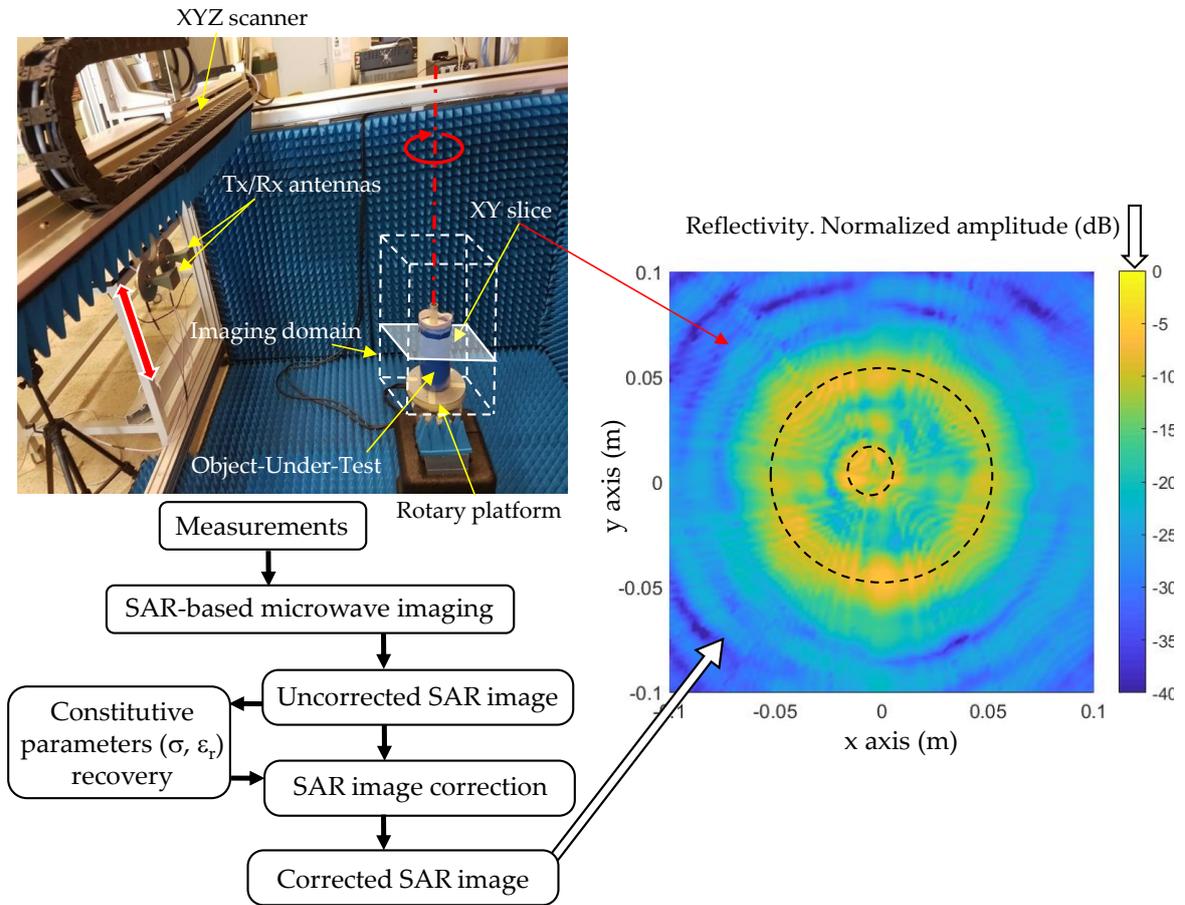
172 Validation of the proposed methodology for fast and simple estimation of constitutive  
 173 parameters from SAR images is conducted in this section.

174 *3.1. Measurement setup*

175 A 3D tomographic measurement setup is proposed, consisting of a rotary platform where the  
 176 OUT is placed, and an XYZ positioner [24]. The Tx/Rx probe antennas (Standard Gain Horn, SGH  
 177 [25]) are mounted in a quasi-monostatic configuration on a vertical slider of the XYZ positioner.  
 178 Vertical (z-axis) motion is allowed along 27 cm, in 1 cm steps, while the OUT can be rotated 360°,  
 179 with 1° step. With these parameters, the entire measurement of the OUT takes around 1 hour and 30  
 180 minutes. Alignment of the Tx/Rx antennas with respect to the center of the rotary platform was  
 181 conducted using a laser leveler. The distance from the rotation axis of the rotary platform to the  
 182 aperture plane of the Tx/Rx antenna is 89 cm.

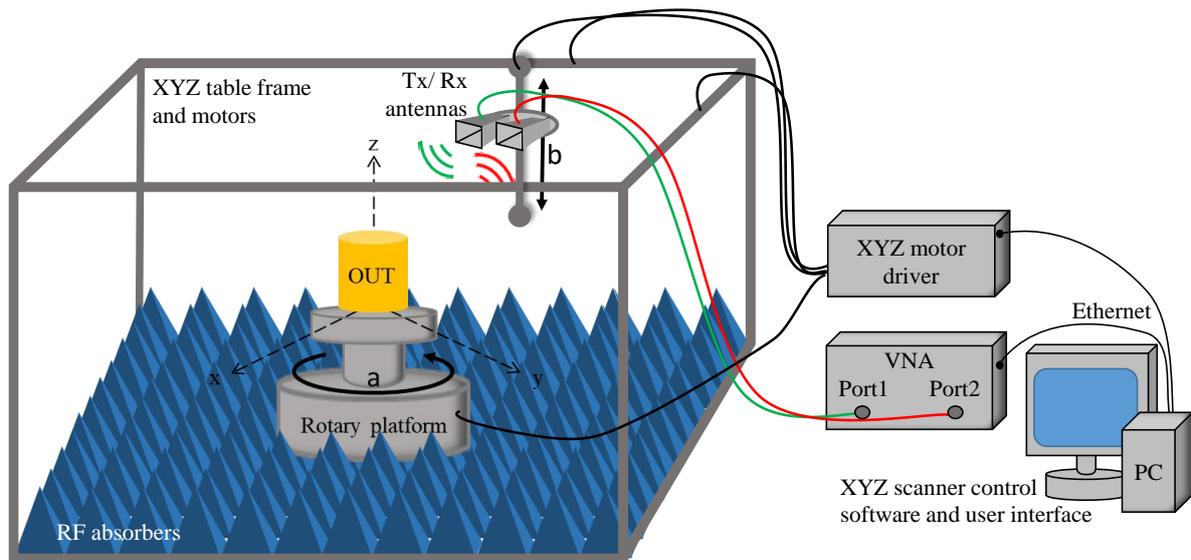
183 Tx/Rx antennas are connected to a Microwave Vector Network Analyzer (VNA) [26], as shown  
 184 in the scheme of Figure 4 and in the picture of Figure 3. In order to set a reference phase for SAR  
 185 imaging, calibration is done at the end of the cables connecting the VNA and the SGH antennas. A  
 186 frequency band from  $f_1 = 12$  GHz to  $f_2 = 18$  GHz is selected as a trade-off between resolution and

187 penetration of the electromagnetic waves in the targets to be tested. This bandwidth yields  $\Delta r' = 2.5$   
 188 cm resolution in range.



189 **Figure 3.** Picture of the measurement setup and flowchart of the SAR-based technique for microwave  
 190 imaging and constitutive parameters characterization.

191



192 **Figure 4.** Scheme of the measurement for dielectric objects imaging using a rotary platform and  
 193 vertical slider. Tx and Rx antennas are placed according to a quasi-monostatic configuration with  
 194 respect to the OUT. Full (360°) angular rotation ( $a$ ) is allowed. Vertical motion range is  $b = 27$  cm.  
 195

196 3.2. Wax candle

197 The first OUT selected for testing the proposed methodology for accurate SAR imaging and  
 198 constitutive parameters retrieval was a wax candle, with 40 cm length and 10 cm diameter, as  
 199 depicted in Figure 5. The fact of having both rotation and translation symmetry around vertical (z-)  
 200 axis motivated the choice of this OUT.  
 201

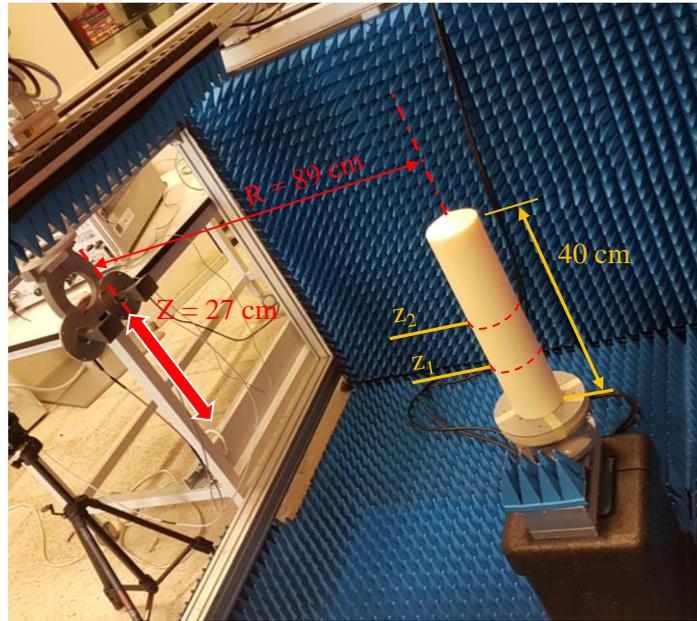
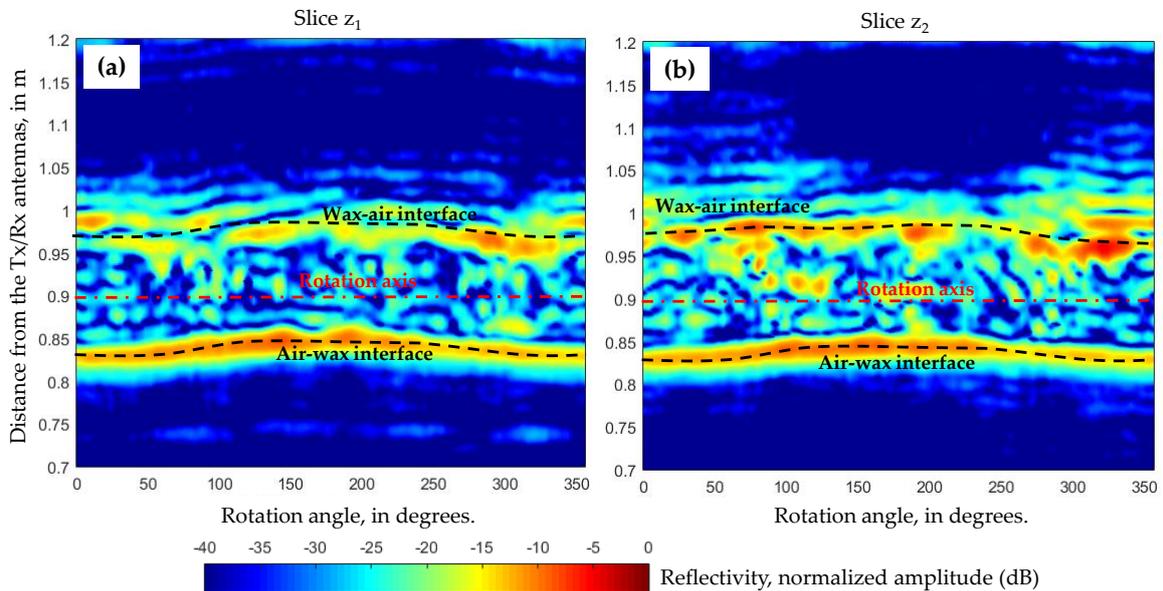


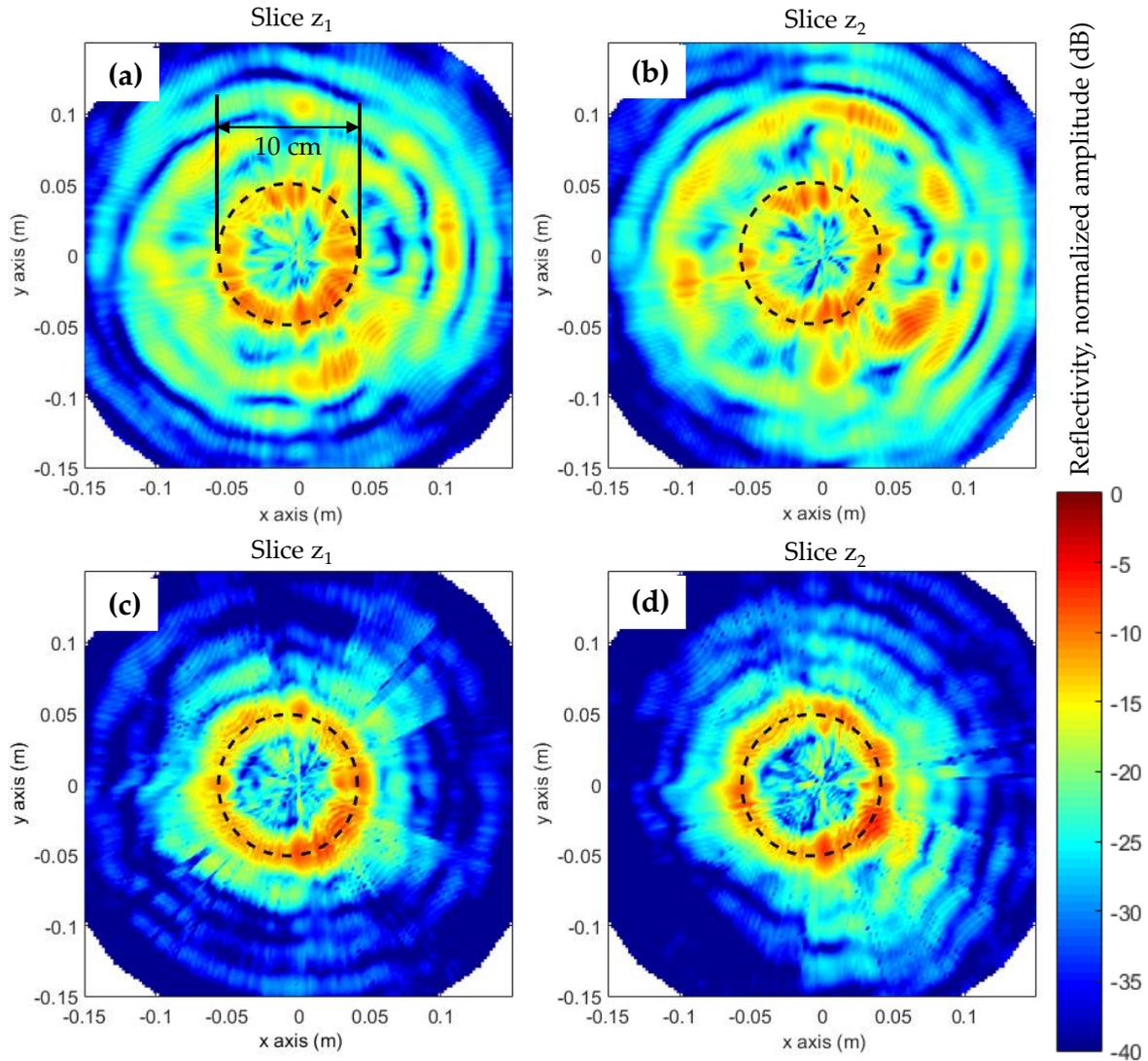
Figure 5. Picture of the wax candle placed on the rotary platform.



204  
 205 **Figure 6.** Reflectivity calculated for each observation angle as a function of the distance from the Tx/Rx  
 206 antennas, for two different XY slices ((a)  $z_1 = -12$  cm and (b)  $z_2 = -5$  cm with respect to the top of the  
 207 wax candle). Air-wax (front reflection) and wax-air (rear reflection) interfaces are noticed.

208 Once the scattered field for each Tx/Rx position and rotation angle was measured, it was  
 209 processed according to the flowchart depicted in Figure 3. The recovered reflectivity of the OUT for  
 210 each rotation angle  $\varphi$  in the range  $r' = [0.7, 1.15]$  at two different XY planes –slices–  $z_1$  and  $z_2$  is shown  
 211 in Figure 6. Range  $r'$  is defined from the position of the Tx/Rx antennas, being the center of rotation  
 212 (rotation axis in Figure 6) located at  $r' = 0.89$  m. As the constitutive parameters of the wax are not

213 known, reflectivity is calculated using Equation (1) ( $k_{\text{medium}}=k_0$ ). The reflection at the air-wax interface  
 214 (#1) can be clearly visible in Figure 6, having a mean value of  $|\rho_{(\text{interface \#1})}| \approx -10 \text{ dB} = 0.32$ . Note that  
 215 the wax candle was not perfectly centered at the rotation axis, so the reflectivity peak of the air-wax  
 216 interface fluctuates between  $r' = [0.83, 0.85] \text{ m}$ . As the wax diameter is  $d_{\text{OUT}} = 10 \text{ cm}$ , the reflectivity  
 217 peak of the wax-air interface (#2) can be expected to be found for  $r' > [0.83+d_{\text{OUT}}, 0.85+d_{\text{OUT}}] \text{ m}$ . For  
 218 each rotation angle ( $\varphi$ ) the maximum of the reflectivity in the range  $r' = [0.95, 1.15]$  is registered. As  
 219 observed in Figure 6, the reflectivity peak of the interface #2 ranges between  $r' = [0.97, 1.01] \text{ m}$ , with  
 220 an average amplitude of  $|\rho_{(\text{interface \#1})}| \approx -15 \text{ dB} = 0.18$ . Finally,  $d_{\text{echo}}$  is calculated as the distance between  
 221 the first and second reflectivity peaks. As the OUT has a cylindrical shape,  $d_{\text{echo}}$  can be calculated  
 222 individually for each rotation angle, then averaging the result, yielding  $d_{\text{echo}} = 0.15 \text{ m}$ .



223  
 224 **Figure 7.** Polar representation of the reflectivity for two different XY slices ( $z_1 = -12 \text{ cm}$  and  $z_2 = -5 \text{ cm}$   
 225 with respect to the top of the wax candle). **(a,b)** Without dielectric delay correction. **(c,d)** After  
 226 dielectric delay correction, considering  $\epsilon_{r,\text{est}} = 2.3$ . Dashed line represent the true contour of the wax  
 227 candle.

228 Now, by applying Equation (6)-(8), an estimate of the permittivity and the conductivity for the  
 229 wax candle can be calculated (Equations (9)-(11)):

$$\epsilon_{r,\text{est}} = (d_{\text{echo}} / d_{\text{OUT}})^2 = (0.15 \text{ m} / 0.1 \text{ m})^2 = 2.3 \quad (9)$$

$$\alpha = \ln(|\rho_{(r' \text{ interface \#1})}| / |\rho_{(r' \text{ interface \#2})}|) / d_{\text{OUT}} = \ln(0.32 / 0.18) / 0.1 = 5.76 \text{ Np/m} = 50 \text{ dB/m} \quad (10)$$

$$\sigma \approx \text{Im}\{((\epsilon_{r,\text{est}})^{1/2} + j \alpha c / (2\pi f_c))^2\} = 0.06 \text{ S/m, with } f_c = (f_1 + f_2) / 2 = 15 \text{ GHz} \quad (11)$$

230 As listed in Table 1, these values are in agreement with the expected ones for paraffin (wax), as  
 231 discussed in [27] (Figure 3, parameter  $x = 0$ ) and in [3] ( $f = 9.4$  GHz:  $\epsilon_{r,\text{est}} = 2.17$ ,  $\sigma_{\text{est}} = 0.03$  S/m), where  
 232 an integral equation-based technique was used to recover these constitutive parameters.

233 Apart from the constitutive parameters, the goal of the proposed methodology is to recover the  
 234 geometry of the OUT. For this purpose, the  $(r', \varphi)$  representation of the reflectivity has to be converted  
 235 into cartesian coordinates. If the rotation axis of the rotary table is defined as  $z$ -axis, then, for each  
 236 slice, the reflectivity in cartesian coordinates is given by Equation (12):

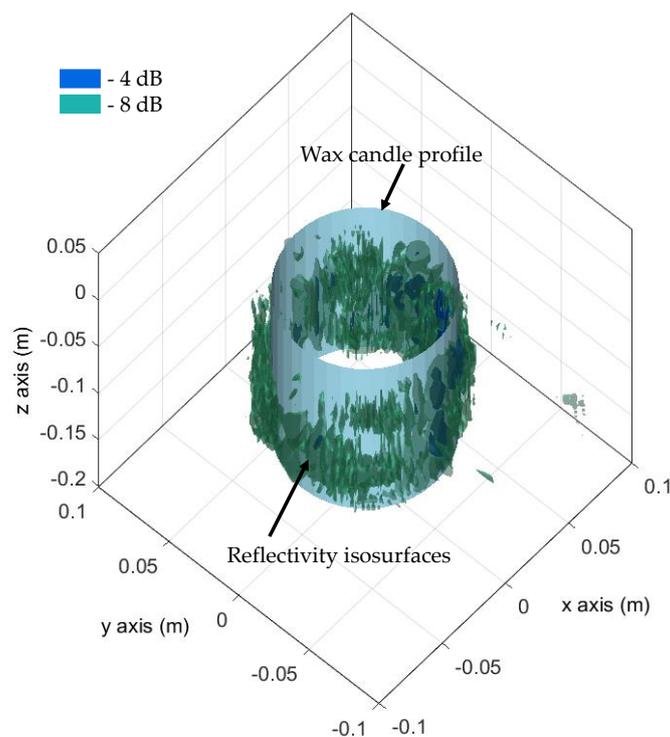
$$\rho(x', y', z') = \rho((r' - R)\cos(\varphi), (r' - R)\sin(\varphi), z'), \text{ with } R = 89 \text{ cm.} \quad (12)$$

237 Figure 7 (a) and Figure 7 (b) corresponds, respectively, to the reflectivity depicted in Figure 6 (a)  
 238 and Figure 6 (b), after applying Equation (12). While the profile of the wax candle can be noticed ( $R$   
 239 = 5 cm), several echoes outside the wax contour are observed as well. These correspond to the  
 240 uncorrected position of the wax-air interface (#2), which is imaged further than its true range distance.

241 SAR image can be corrected by applying Equations (3)-(5), as  $\epsilon_{r,\text{wax}}$  has been already estimated.  
 242 Resulting reflectivity images in cartesian coordinates are depicted in Figure 7 (c) and Figure 7 (d),  
 243 where it can be verified that air-wax (#1) and wax-air (#2) reflections are imaged on the contour of  
 244 the wax candle.

245 Concerning calculation time, the number of measurement points for each slice is 360. For each  
 246 rotation angle, SAR along  $r'$  axis is calculated in  $\sim 5$  ms (7 ms in the case of the corrected SAR) using  
 247 a conventional laptop with no parallelization of the SAR code. Thus, the overall calculation time to  
 248 obtain the SAR image on each slice is 18 s for uncorrected SAR, and 25 s for corrected SAR. As the  
 249 estimation of the conductivity and permittivity values requires less than 2 s, the overall calculation  
 250 time for each slice is approximately 45 s. It must be remarked that the methodology is fully  
 251 parallelizable, so that the calculation time can be decreased proportionally to the number of  
 252 processors used.

253



254

255 **Figure 8.** 3D representation of the recovered reflectivity of the wax candle, after dielectric delay  
 256 correction.

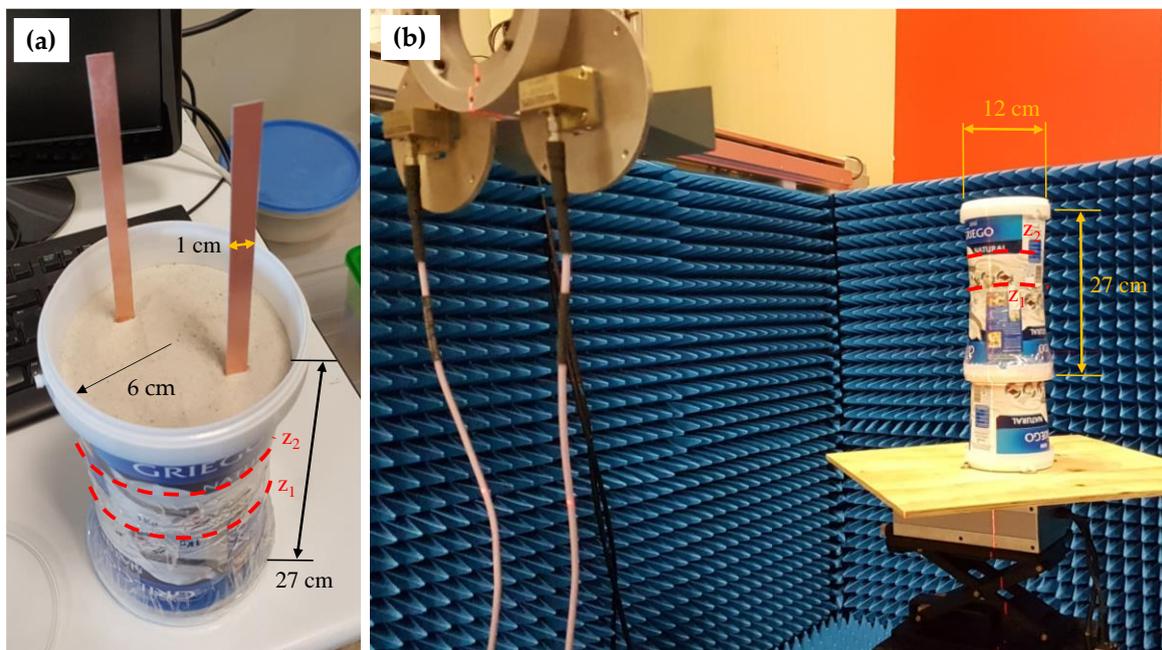
257 It is worth mentioning that all the required information for estimating the conductivity and the  
 258 permittivity, and thus being able to correct the SAR image as proved in Figure 7, is obtained just from  
 259 the representation of the reflectivity assuming free-space propagation condition depicted in Figure 6.

260 Finally, corrected reflectivity images for different XY slices can be stacked to obtain a 3D  
 261 representation of the OUT. For this example, the reconstructed geometry of the wax candle is shown  
 262 in Figure 8. Graphics post-processing techniques could be applied to convert reflectivity isosurfaces  
 263 into a 3D geometry model.

### 264 3.3. Plastic bottle filled with sand

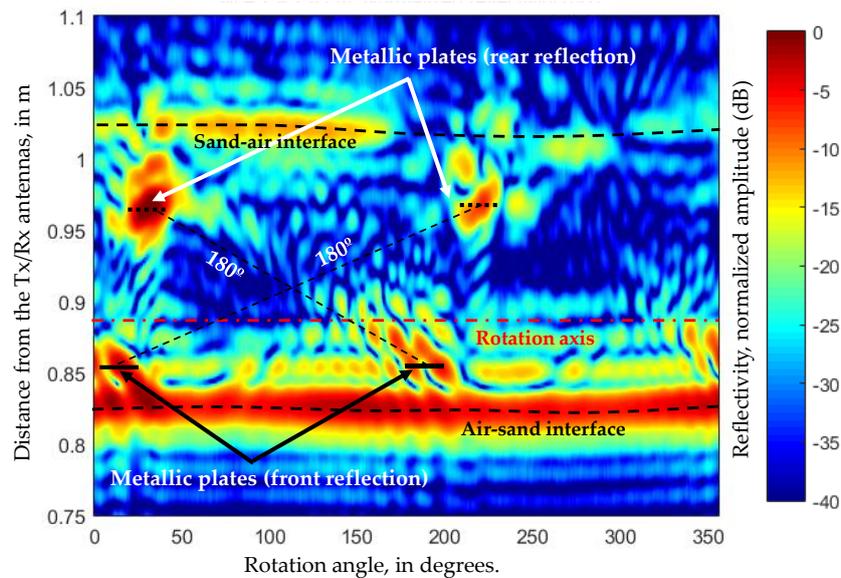
265 In order to remark the consequences of not considering the permittivity of the OUT for SAR  
 266 imaging, the second OUT consists of a  $d_{OUT} = 12$  cm diameter plastic bottle filled with sand, with two  
 267 metallic plates concealed on it, as depicted in Figure 9 (a). The two metallic plates are placed  
 268 approximately symmetrical with respect to the center of the bottle. As in the previous example, the  
 269 OUT is placed on top of the rotary table (Figure 9 (b)).

270 First, SAR algorithm assuming free-space propagation conditions (Equation (1)) is applied.  
 271 Reflectivity for slice  $z_1 = -13$  cm as a function of the rotation angle and the distance from the Tx/Rx  
 272 is depicted in Figure 10. As in the first example, the air-sand (#1) and the sand-air (#2) interfaces can be  
 273 observed, together with the placement of the two metallic plates inside the plastic bottle. Note that  
 274 the two metallic plates are facing the Tx/Rx antennas twice during the  $360^\circ$  acquisition. Thus, two  
 275 main echoes of the same metallic plates (front and rear) appear in the reflectivity image, both shifted  
 276 backwards proportionally to the distance between the air-sand interface and the metallic plate  
 277 placement. The rear echo is more noticeable, as it is further from the air-sand interface which partially  
 278 masks the front reflection of the metallic plates.  
 279



280

281 **Figure 9.** (a) Picture of the plastic box filled with sand, with two metallic plates embedded. (b) Picture  
 282 of the OUT placed on the rotary platform.



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**Figure 10.** Reflectivity calculated for each observation angle as a function of the distance from the Tx/Rx antennas, for a XY slice ( $z_1 = -13$  cm with respect to the top of the plastic box). Air-sand (front reflection) and sand-air (rear reflection) interfaces are noticed, as well as the stronger reflection in the metallic plates.

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If this reflectivity image is converted into cartesian coordinates by applying Equation (12), the image depicted in Figure 11 (a) is obtained. Not only the sand-air interface (#2) is shifted backwards, but also the rear reflection of the metallic plates is imaged *outside* the sand box. The reason is that the displacement of the rear reflection due to free-space propagation conditions is greater than the distance from the metallic plates to the plastic bottle. If another slice is chosen ( $z_2 = -7$  cm) the same effect can be observed (Figure 11 (b)). Thus, it is clear the need of using an estimate of the permittivity of the sand in order to recover a correct reflectivity image of the OUT. As in the previous example, conductivity and permittivity can be estimated from the uncorrected reflectivity depicted in Figure 10.

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Analysis of Figure 10 allows estimating the air-sand interface (#1), located at  $r' = 0.83$  m on average, and the sand-air interface (#2), placed at  $r' = 1.02$  m. Thus,  $d_{\text{echo}} = 19$  cm and, as  $d_{\text{OUT}} = 12$  cm, the relative permittivity estimated using Equation (6) is  $\epsilon_{r,\text{est}} = 2.5$ .

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For the conductivity, values of the reflectivity within the angular range  $\varphi = [60^\circ, 150^\circ]$  can be considered, yielding  $|\rho_{(\text{interface \#1})}| \approx -5$  dB = 0.56,  $|\rho_{(\text{interface \#2})}| \approx -13$  dB = 0.22. From Equation (7), the attenuation is  $\alpha = 7.8$  Np/m = 67.6 dB/m, and, finally, the conductivity is (Equation (8))  $\sigma_{\text{est}} = 0.08$  S/m.

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As a reference, typical values for sand with a moisture content below 1% is  $\epsilon_{r,\text{est}} \approx 2.4$  and  $\sigma = 0.02$  at 10 GHz (Figure 2 of [28]). In this example, the same sand as in [22] was used, where values of  $\epsilon_{r,\text{est}} \approx [2.7, 3.5]$  and  $\sigma = [0.27, 0.40]$  were estimated in the 3 to 6 GHz frequency band. As shown in [28], the value of these constitutive parameters tends to decay with frequency. A summary of the recovered constitutive parameters is shown in Table 1.

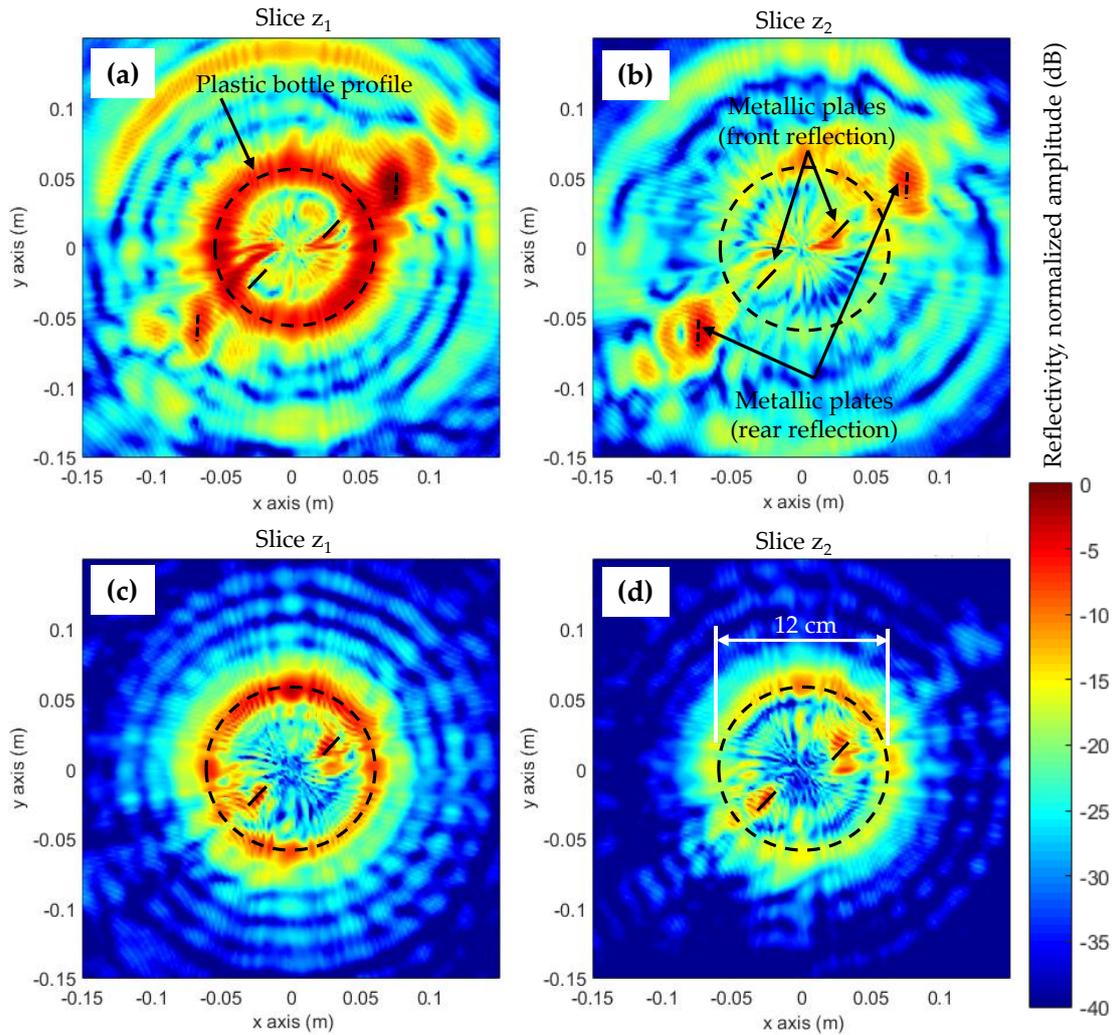
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Once the constitutive parameters have been estimated, the corrected SAR image can be computed. SAR images corresponding to slices  $z_1 = -13$  cm and  $z_1 = -7$  cm are depicted in Figure 11 (c) and Figure 11 (d). Not only the contour of the plastic bottle is correctly imaged, but also the two metallic plates are found inside the area filled with sand.



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**Figure 11.** Polar representation of the reflectivity for two different XY slices ( $z_1 = -13$  cm and  $z_2 = -7$  cm with respect to the top of the wax candle). **(a,b)** Without dielectric delay correction. **(c,d)** After dielectric delay correction, considering  $\epsilon_{r,est} = 2.5$ . Dashed line represent the true contour of the wax candle. Solid line represents the true position of the metallic plates. In **(a,b)**, the straight dashed lines indicate the location of the imaged metallic plates, which appear outside the plastic box contour due to the dielectric delay.

319 **4. Discussion**

320 Results presented in Section 3 confirm the effectiveness of the proposed methodology to recover  
321 the constitutive parameters of the OUT using the imaged reflectivity assuming free-space  
322 propagation conditions. Then, the estimated reflectivity value is introduced into a modified SAR  
323 technique that takes into account the different media that compose the microwave imaging scenario,  
324 so that a corrected SAR image is produced.

325 With respect to similar techniques where conductivity and permittivity were retrieved from  
326 reflectivity images [21],[22], the main novelty is that all the information is extracted from the SAR  
327 image of the OUT, avoiding the need of placing external references such as a metallic plate (buried  
328 or acting as background). In the proposed methodology, the challenge is the development of  
329 processing algorithms capable of extracting the information from the uncorrected SAR image, taking  
330 advantage of the a priori information about the OUT geometry. In the case of the examples presented  
331 in this contribution, rotation symmetry around vertical ( $z$ -) axis made this processing easy, as the  
332 reflectivity could be represented in cylindrical coordinates  $(r', \varphi)$ . For those targets with more complex  
333 geometry, pattern recognition algorithms could be used to identify and extract the position of the  
334 interfaces between media.

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336**Table 1.** Constitutive parameters of the media considered in the examples. Comparison with other techniques at microwave frequencies.

Material	Frequency (GHz)	Permittivity ( $\epsilon_r$ )	Conductivity ( $\sigma$ ) (S/m)	Method	Reference
Wax (paraffin)	12-18	$2.3 \pm 0.2$	$0.06 \pm 0.02$	Backpropagation SAR	This contribution
Wax (paraffin)	9-15	2.2	0.35	X-ray powder diffraction analysis	[27]
Wax (paraffin)	9.4	2.17	0.03	Model-based monochromatic inverse scattering	[3]
Sand	12-18	$2.5 \pm 0.2$	$0.08 \pm 0.02$	Backpropagation SAR	This contribution
Sand	3-6	[2.7, 3.5]	[0.27, 0.4]	Backpropagation SAR, with reference target	[22]
Sand	Up to 10	$2.4 \pm 0.2$	$0.02 \pm 0.005$	Coaxial probe	[28]

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Recovered permittivity and conductivity values are summarized in Table 1. In the case of the permittivity, the estimated values are within the range provided by other methods based on different hardware and processing techniques. Conductivity values are more dependent on the exact composition of the medium (e.g. moisture content), so larger dispersion can be expected.

Calculation time is also a key issue for the development of inverse scattering and imaging systems. Backpropagation SAR-based techniques are by far faster than model-based methods. For the examples presented in this contribution, recovery of the corrected SAR image required around 45 s for each XY slice using a non-parallelized software code. Although this is not real-time imaging, it must be remarked that i) measurement time was around 180 s per slice (360 acquisition points), and ii) the proposed SAR-based technique is fully parallelizable. If the code is run on a 4-core processor (available in most conventional computers nowadays), calculation time would be reduced to less than 12 s per slice. The use of a Graphics Processing Unit (GPU) could result in 60-80 times speedup, as explained in [9], thus enabling real-time imaging.

## 351 5. Conclusions

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A simple, fast method for microwave imaging using a SAR-based technique has been presented. The proposed methodology is capable of providing an estimate of the permittivity and conductivity of the OUT from a SAR image retrieved under free-space propagation conditions, and then, correcting the SAR image by introducing the estimated permittivity value (or, in other words, introducing the correct propagation velocity at each medium on the imaging problem). Results showed the effects of inaccurate SAR imaging, and the capability of the proposed methodology to provide accurate microwave images of the targets under test.

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